



# Testing of Micromachined Structures

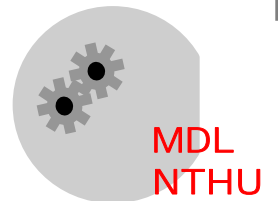
方維倫 教授

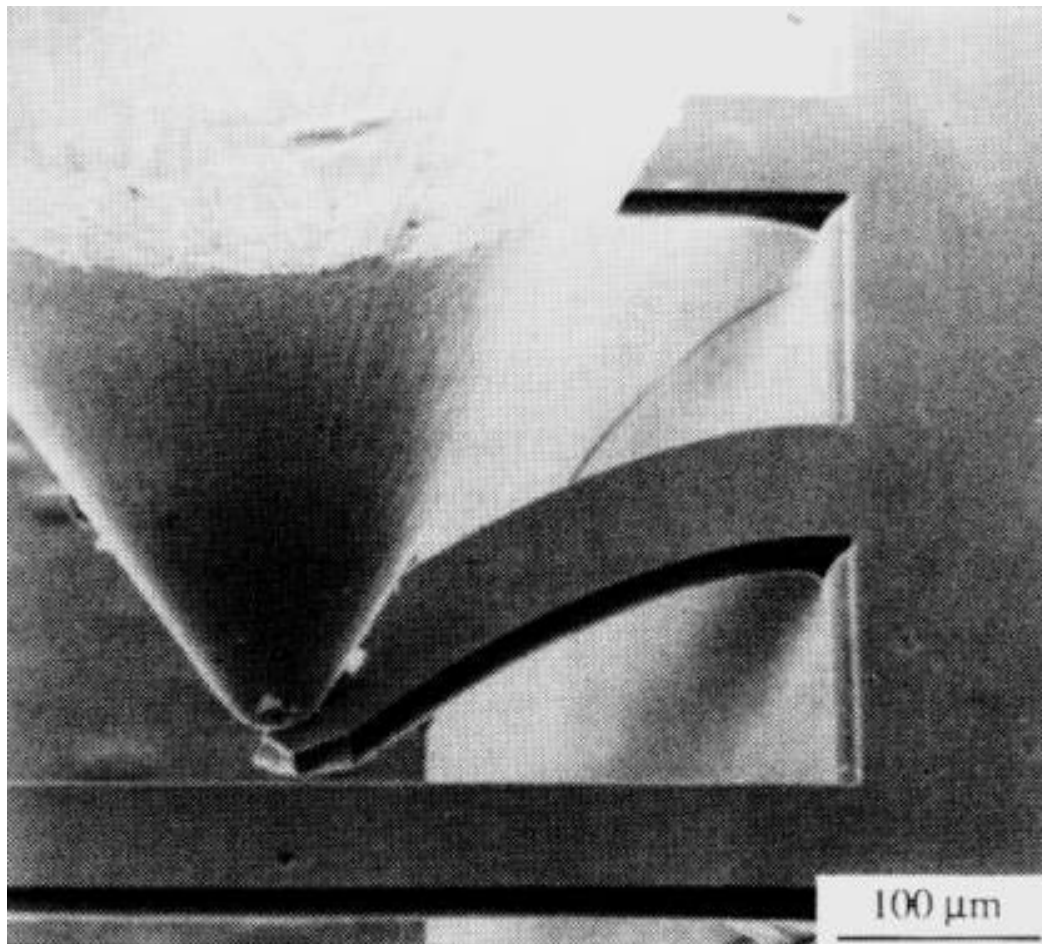
**Weileun Fang, Professor**

**Micro Devices Laboratory**

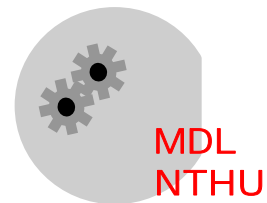
**Power Mechanical Engineering Dept.**

**National Tsing Hua University**





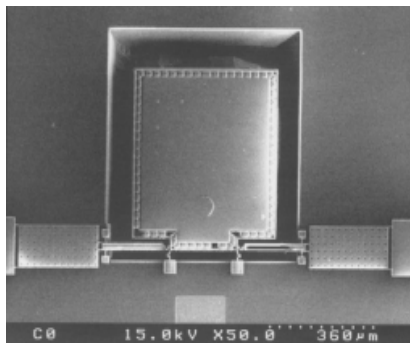
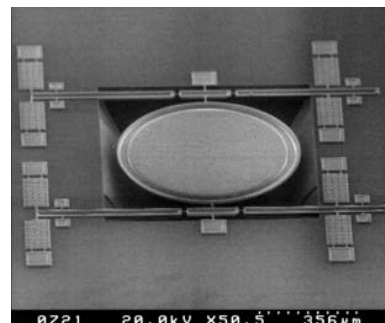
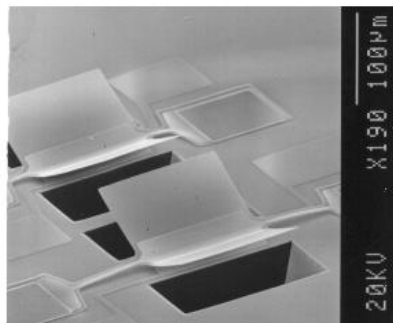
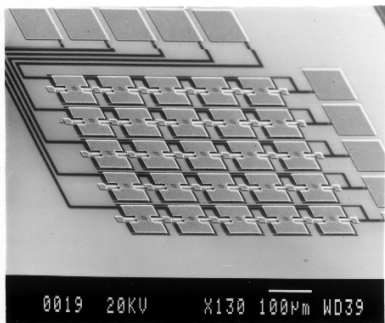
*J.-A. Schweitz, 1992*



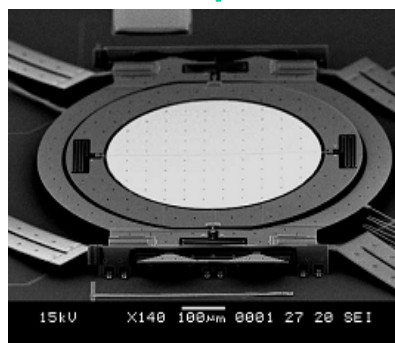


# Thin Film Devices

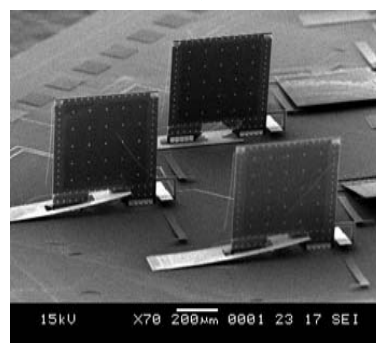
## Scanners for display



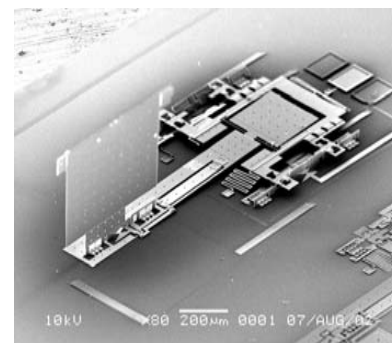
2D Optical Switch



3D Optical Switch



2D Optical Switch



VOA

J. Hsieh and W. Fang, *Transducers'99*, Japan, 1999

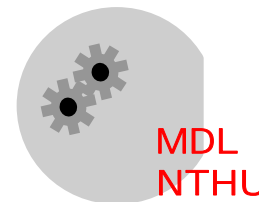
H.-Y. Lin and W. Fang, *IEEE Optical MEMS*, Hawaii, 2000

H.-Y. Lin, H. Hu, and W. Fang, *Transducers'01*, Germany, 2001

H.-Y. Lin, M.-C. Wu, and W. Fang, *Transducers'01*, Germany, 2001

W.-C. Chen, J. Hsieh, and W. Fang, *IEEE MEMS'02*, Las Vegas, NV, 2002

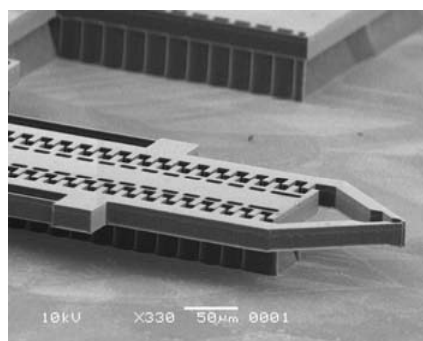
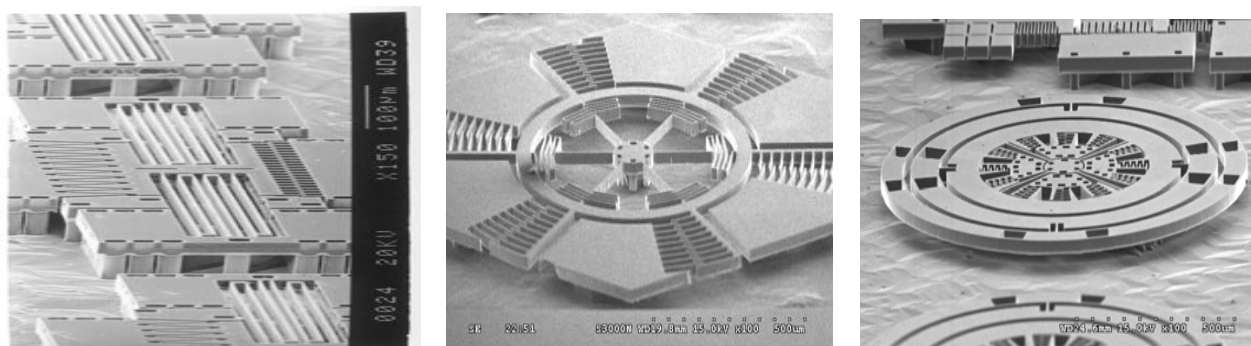
Y.-P. Ho, M. Wu, H.-Y. Lin and W. Fang, *IEEE Optical MEMS*, Switzerland, 2002



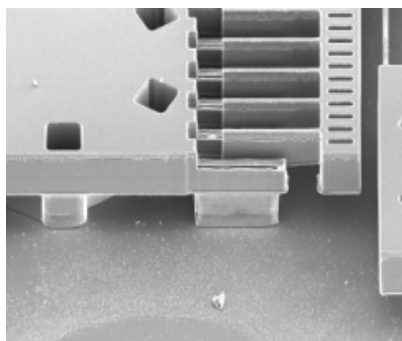


# Thick (HARMs) Devices

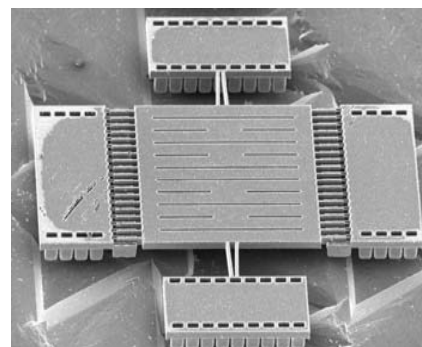
Inertia sensors



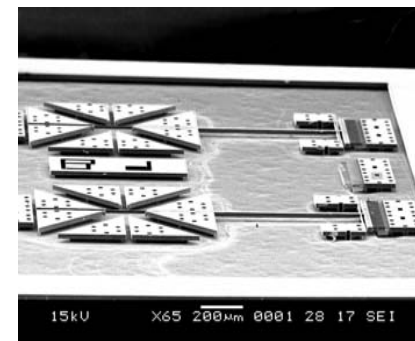
Gripper



Vertical comb



Optical scanner



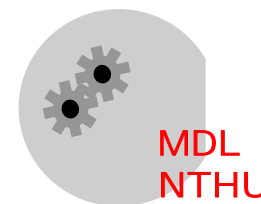
VOA

J. Hsieh and W. Fang, *ASME IMECE*, New York, NT, 2001

J. Hsieh and W. Fang, *JMM*, 2001

J. Hsieh, C.C. Chiu, J.M. Tsai, and W. Fang, *IEEE Optical MEMS*, Switzerland, 2002

J. M. Tsai, J. Hsieh, and W. Fang, *IEEE Optical MEMS*, Switzerland, 2002







- **Static test**

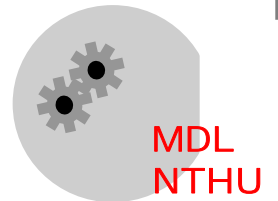
- + **Devices**

- + **Material properties**

- **Dynamic test**

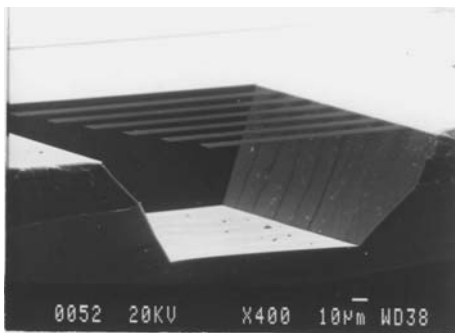
- + **Devices**

- + **Material properties**

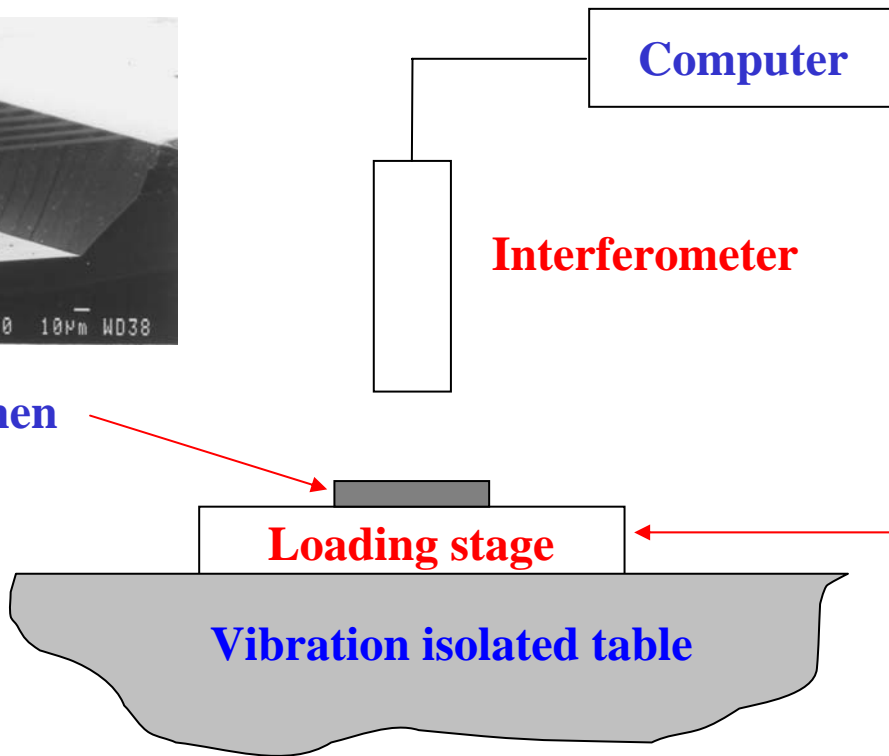




# Static Testing Platform



**Specimen**



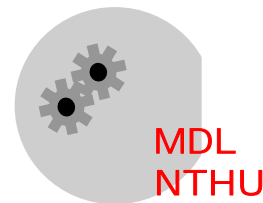
**Residual stresses**

**Heating stage**

**Electromagnetic stage**

**Pressure source**

**Indenter**

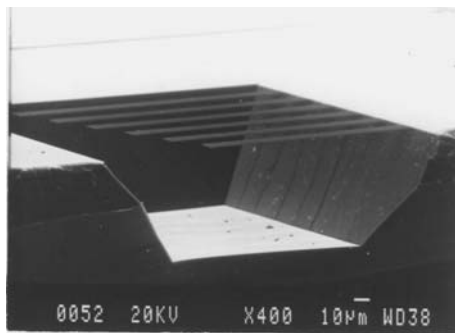




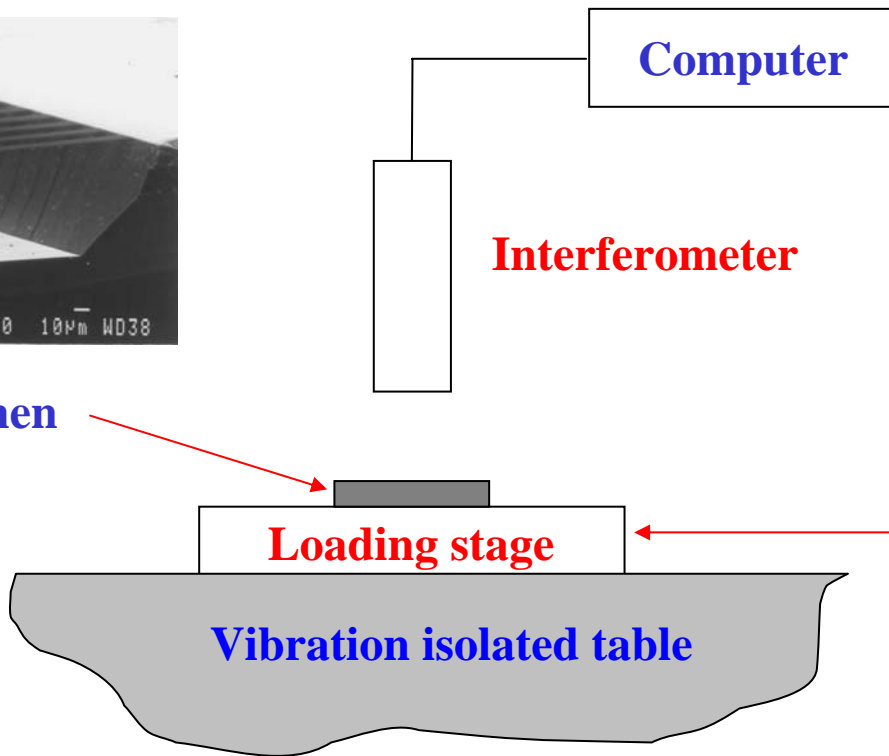
- **Static test**
  - + **Devices**
  - + **Material properties**
  
- **Dynamic test**
  - + **Devices**
  - + **Material properties**



# Static Testing Platform



Specimen



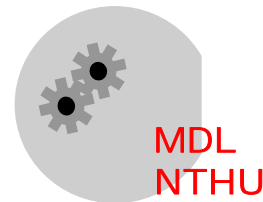
**Residual stresses**

**Heating stage**

**Electromagnetic stage**

**Pressure source**

**Indenter**

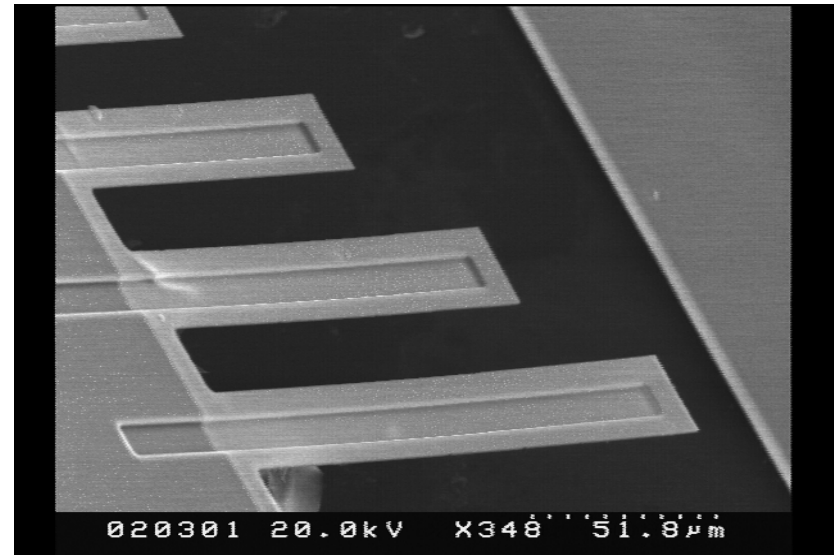
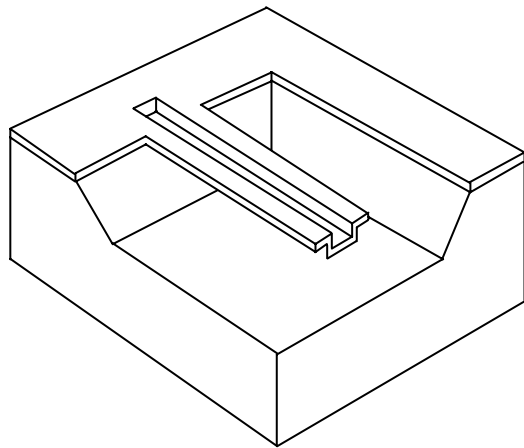






# Self loaded by residual stress

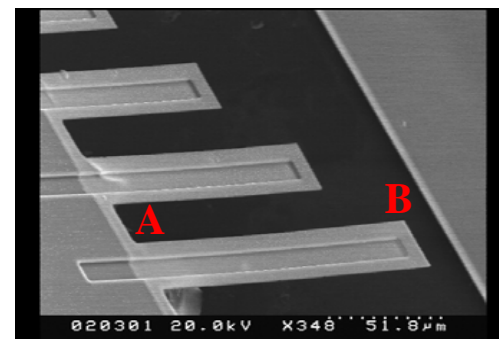
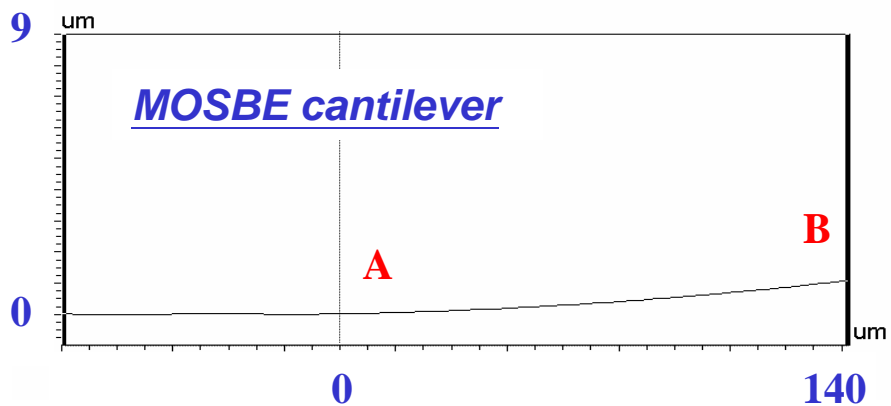
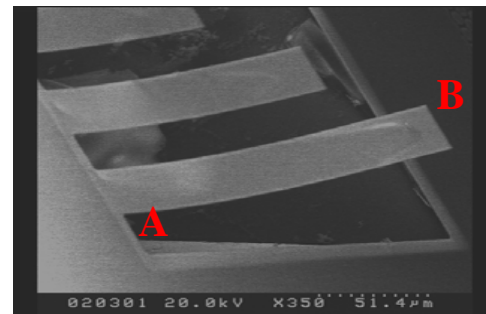
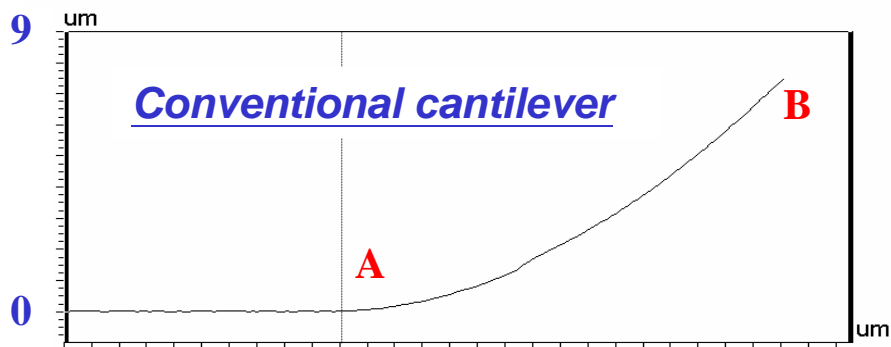
- Stiffness test of the cantilever



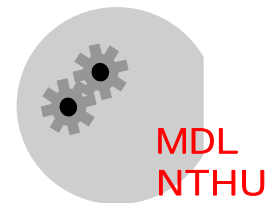
H.-Y. Lin and W. Fang, *J. of Micromechanics and Microeng.*, 2000



Deflection ( $\mu\text{m}$ )

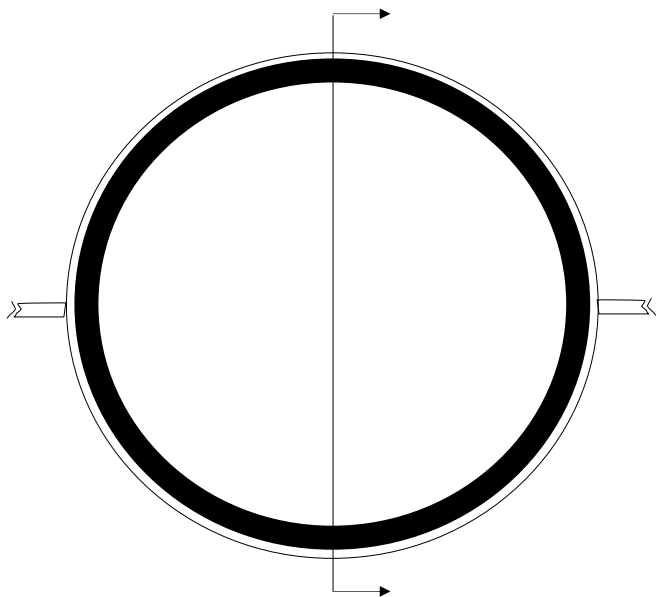


Position along the beam length ( $\mu\text{m}$ )

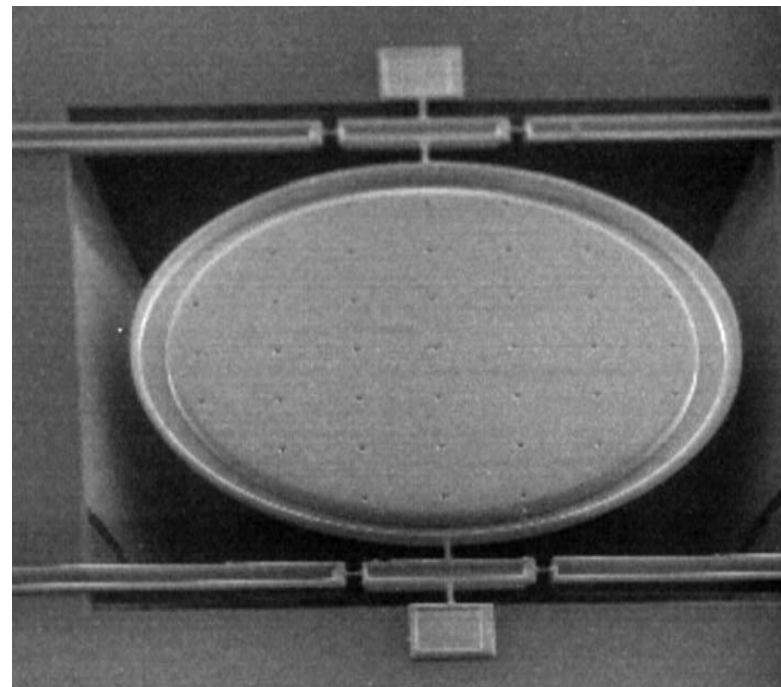




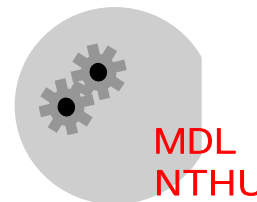
- **Stiffness test of the mirror**



**Reinforced folded frame**

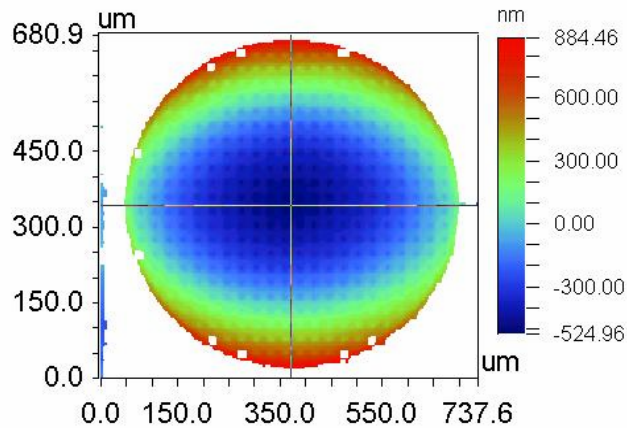


H.-Y. Lin and W. Fang, the *ASME IMECE*, Orlando, FL, 2000

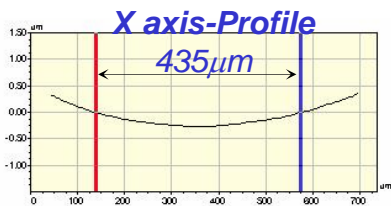
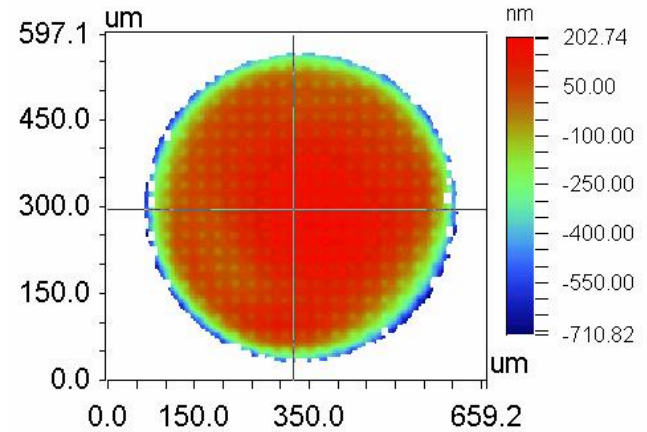




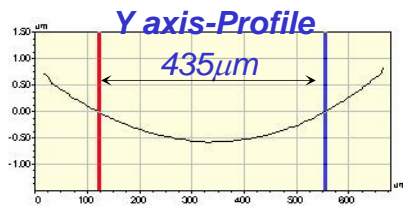
## MUMPs mirror



## MOSBE mirror



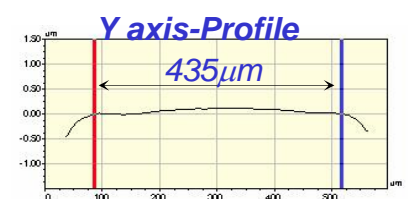
$\rho : 93\text{mm}$



$\rho : 41\text{mm}$

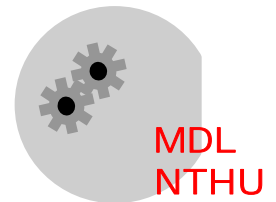


$\rho : 153\text{mm}$



$\rho : 179\text{mm}$

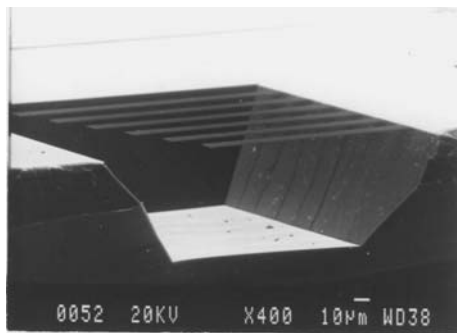
H.-Y. Lin and W. Fang, the ASME IMECE, Orlando, FL, 2000



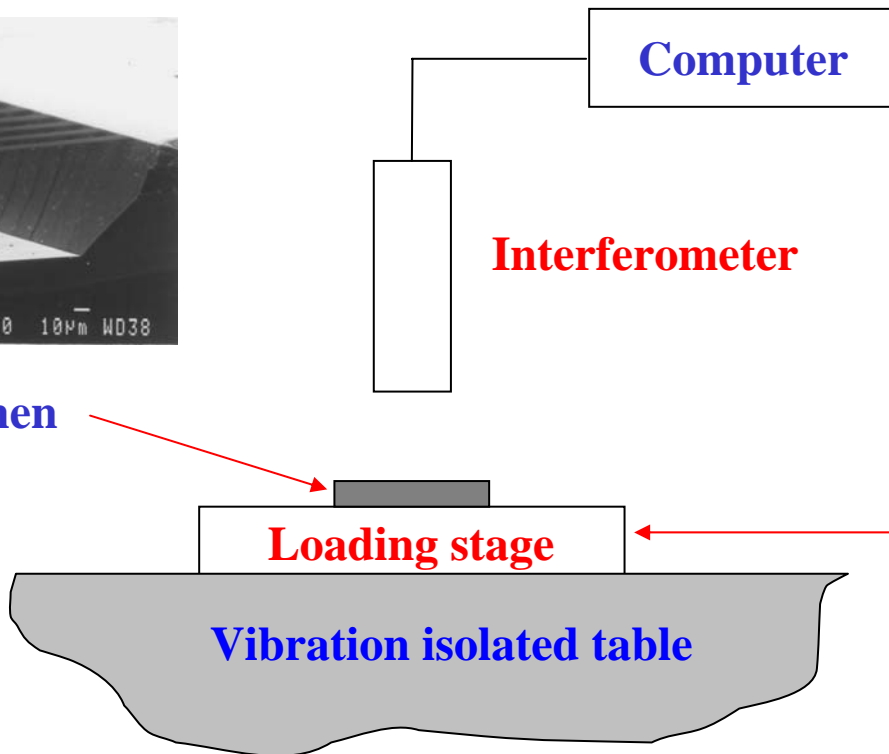




# Static Testing Platform



**Specimen**



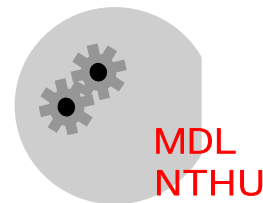
**Residual stresses**

**Heating stage**

**Electromagnetic stage**

**Pressure source**

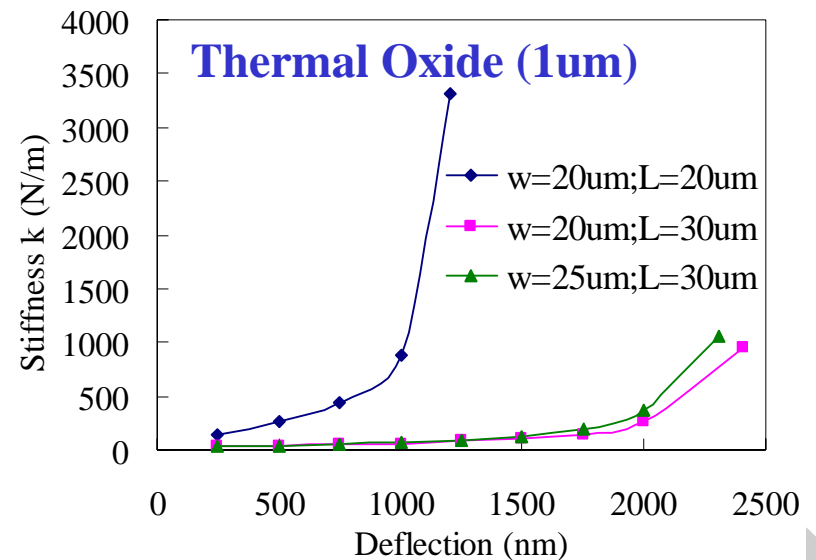
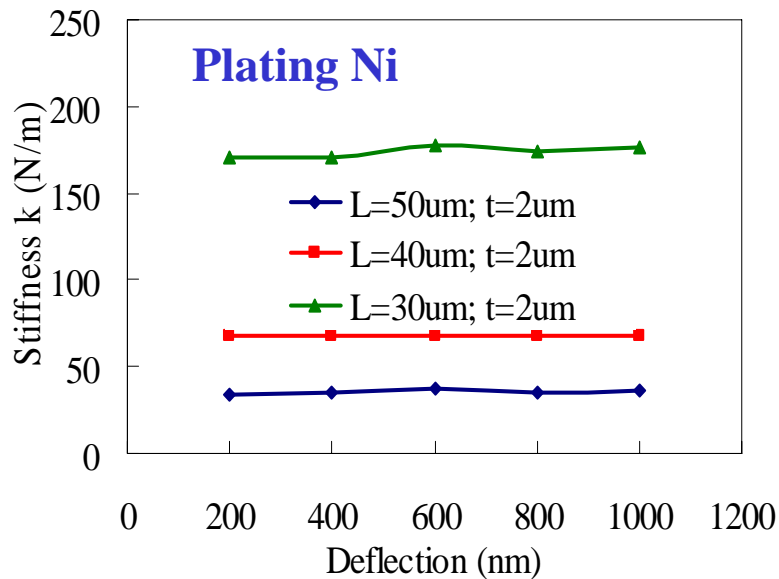
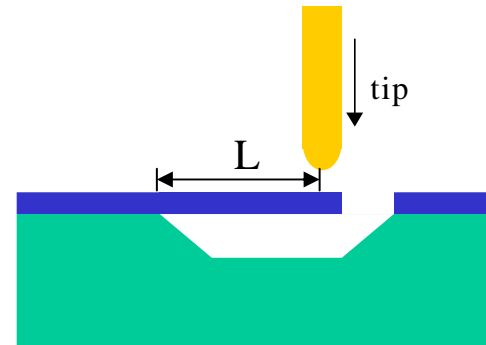
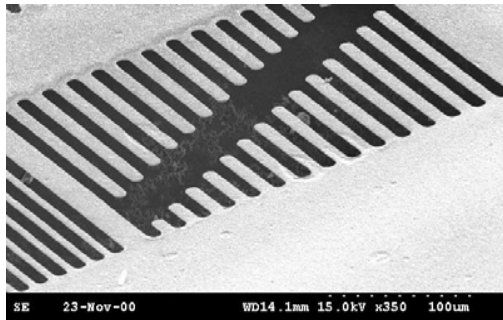
**Indenter**





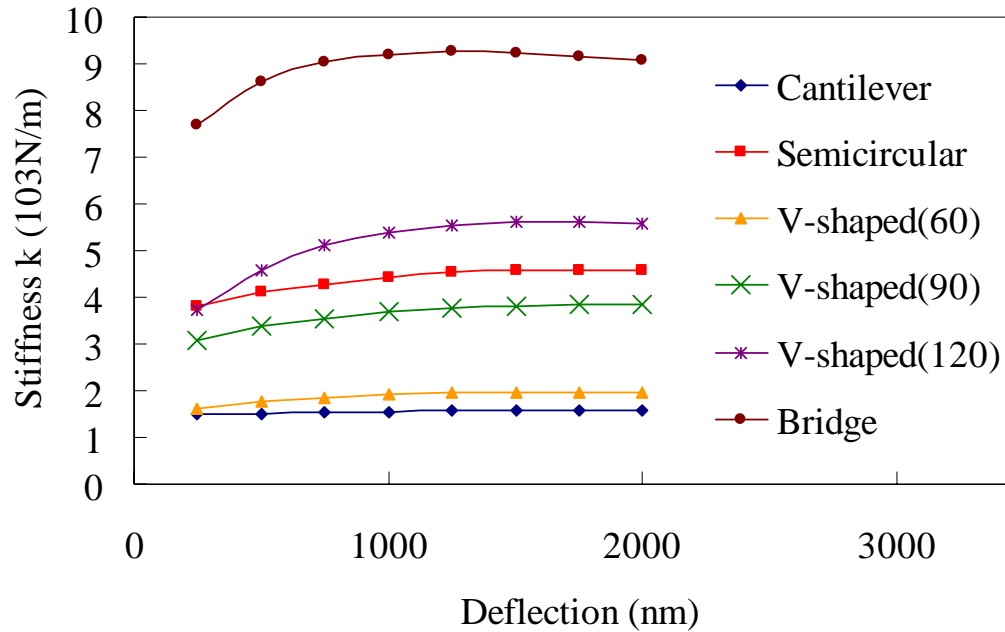
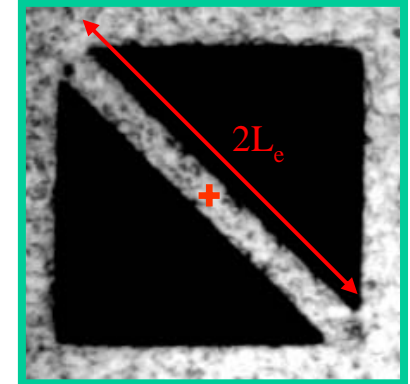
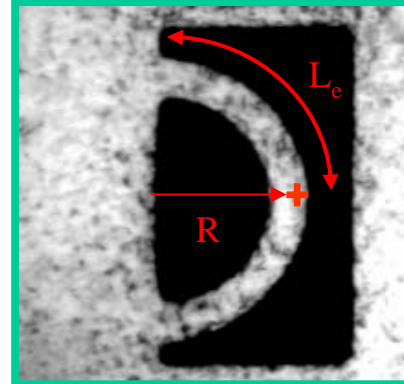
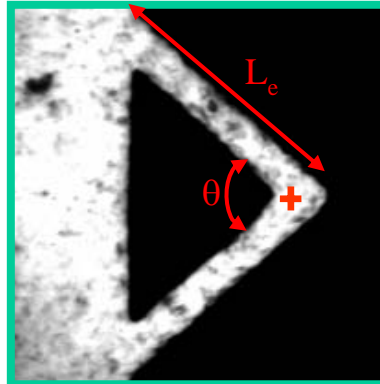
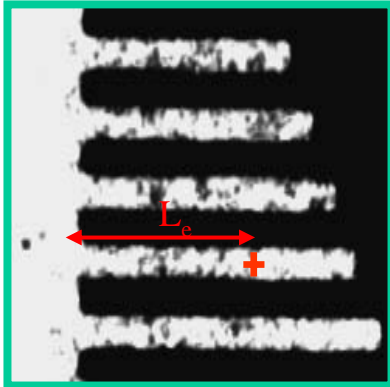
# External loaded by nano-indenter

- Stiffness test of the cantilever





## • Stiffness test of various structures





- **Static test**

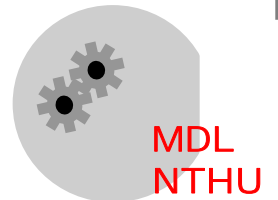
- + **Devices**

- + **Material properties – Residual stresses**

- **Dynamic test**

- + **Devices**

- + **Material properties**

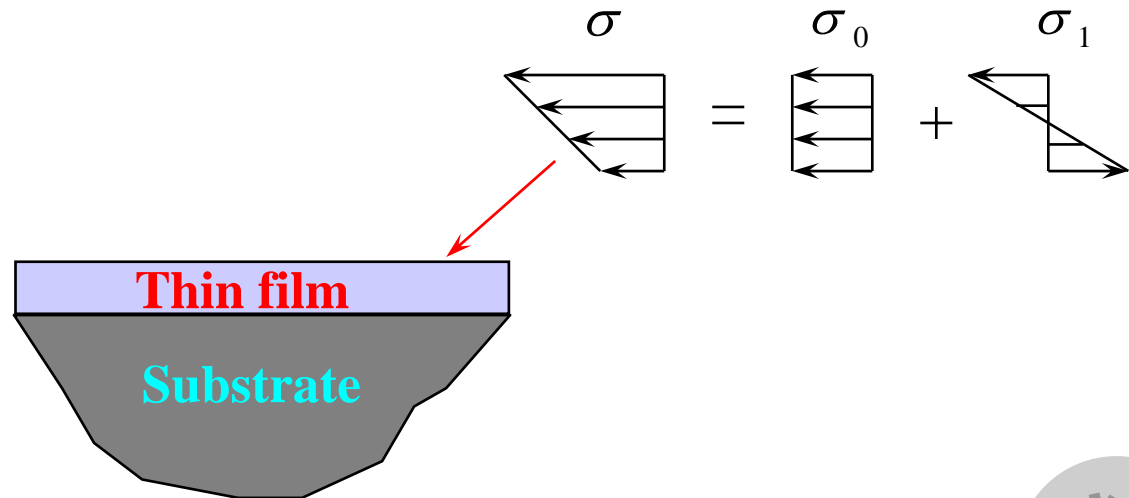






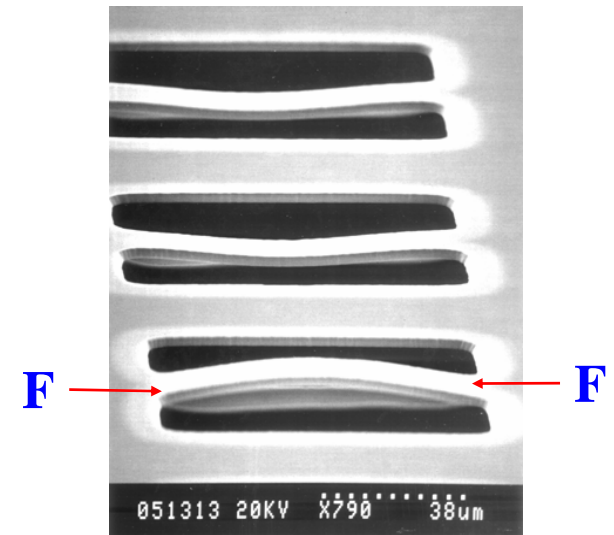
# Residual stress

- **Compression  $-\sigma_0$**
- **Tension  $+\sigma_0$**
- **Gradient  $\sigma_1$**





## Buckle Beam Method



- Idealization: critical beam length

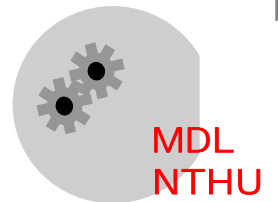
$L < L_{cr}$  unbuckled

$L > L_{cr}$  buckled

where 
$$L_{cr} = 2\pi \sqrt{\frac{EI}{\sigma_0 A}}$$

Guckel, Randazzo, and Burns, *J. of Applied Physics*, 1985

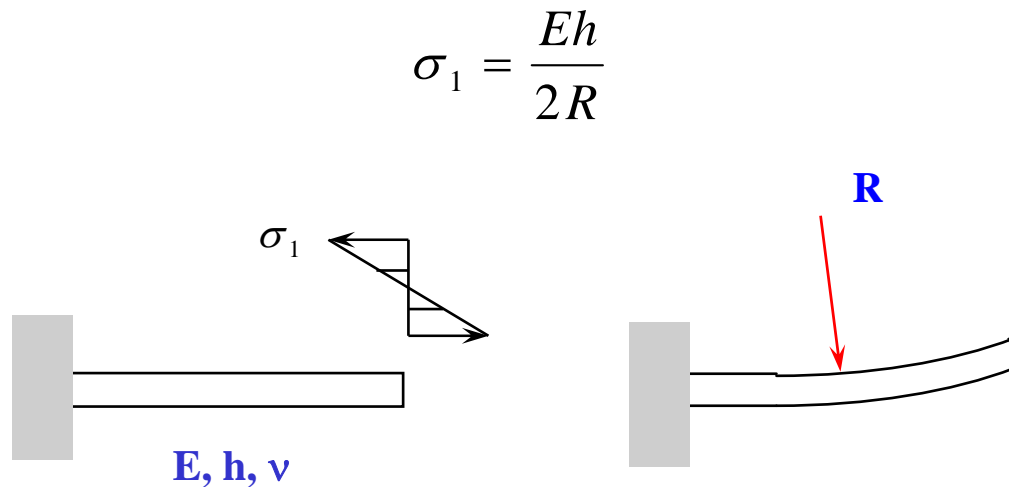
W. Fang, and J.A. Wickert, *J. of Micromechanics and Microeng.*, 1994

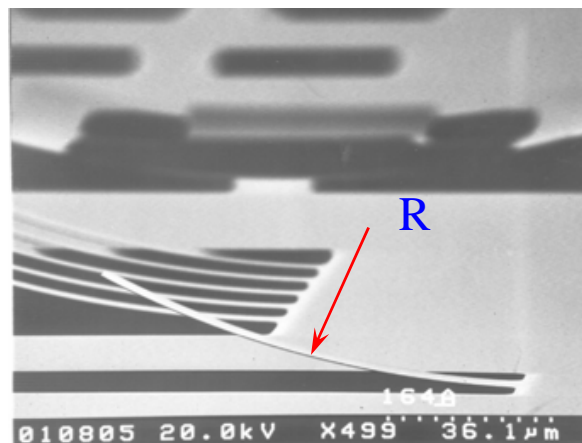
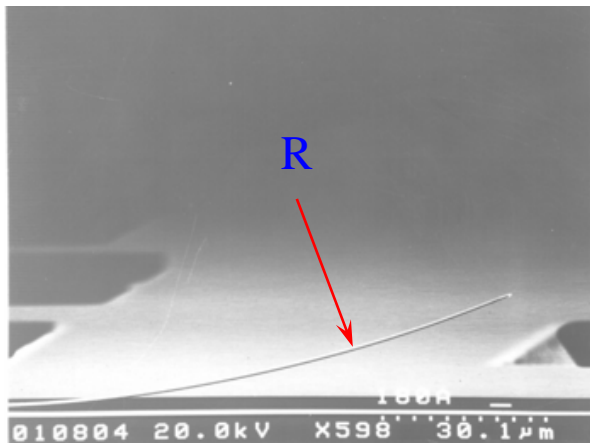




## Cantilever Beam Method

- **Gradient residual stress  $\sigma_1$**  will lead to a **bending moment** on the test cantilever
- **Gradient residual stress is determined by the radius of curvature  $R$**  of the bent cantilever





Y.-L. Chen, J.-S. Shie, and W. Fang, 1997



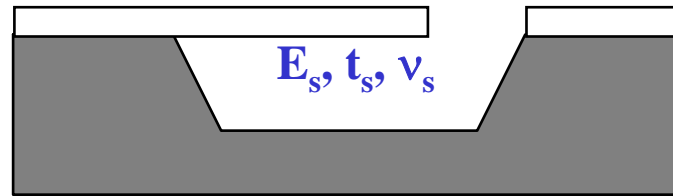


# Bilayer beam technique

$$\sigma_0 = \frac{E_s (t_s)^2}{6R t_f (1 - \nu_s)}$$

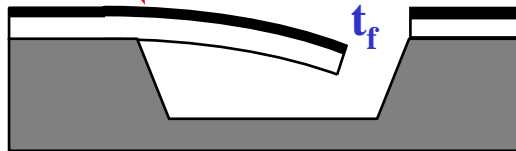
↑ measured

Test cantilever

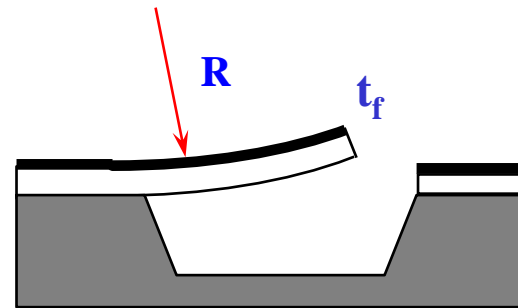


Substrate

deposited film

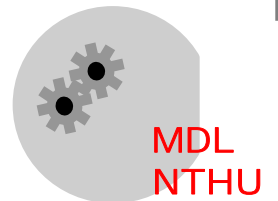


Compression



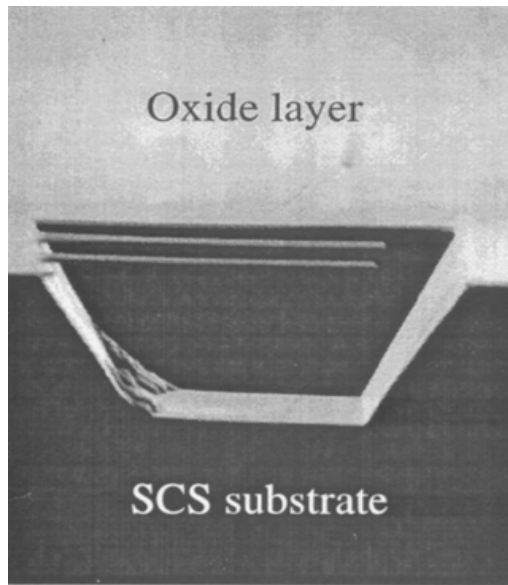
Tension

W. Fang and J.A. Wickert, J. of Micromech. and Microeng., 1995

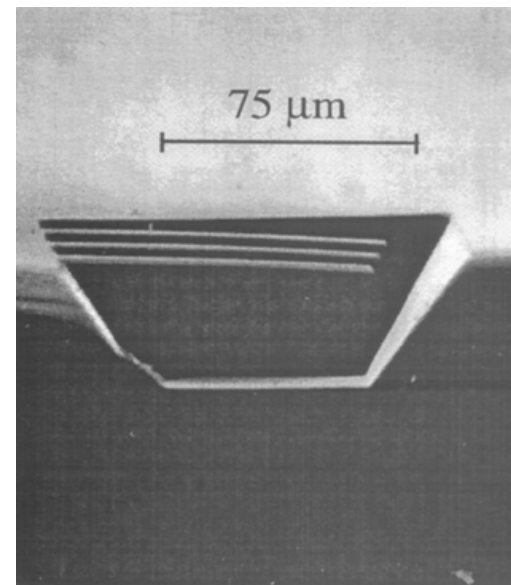




- **Bilayer beam technique can be applied to measure residual stress of thin films whose thickness are too small to fabricate micromachined structures**

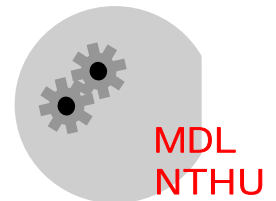


**SiO<sub>2</sub> test cantilever**



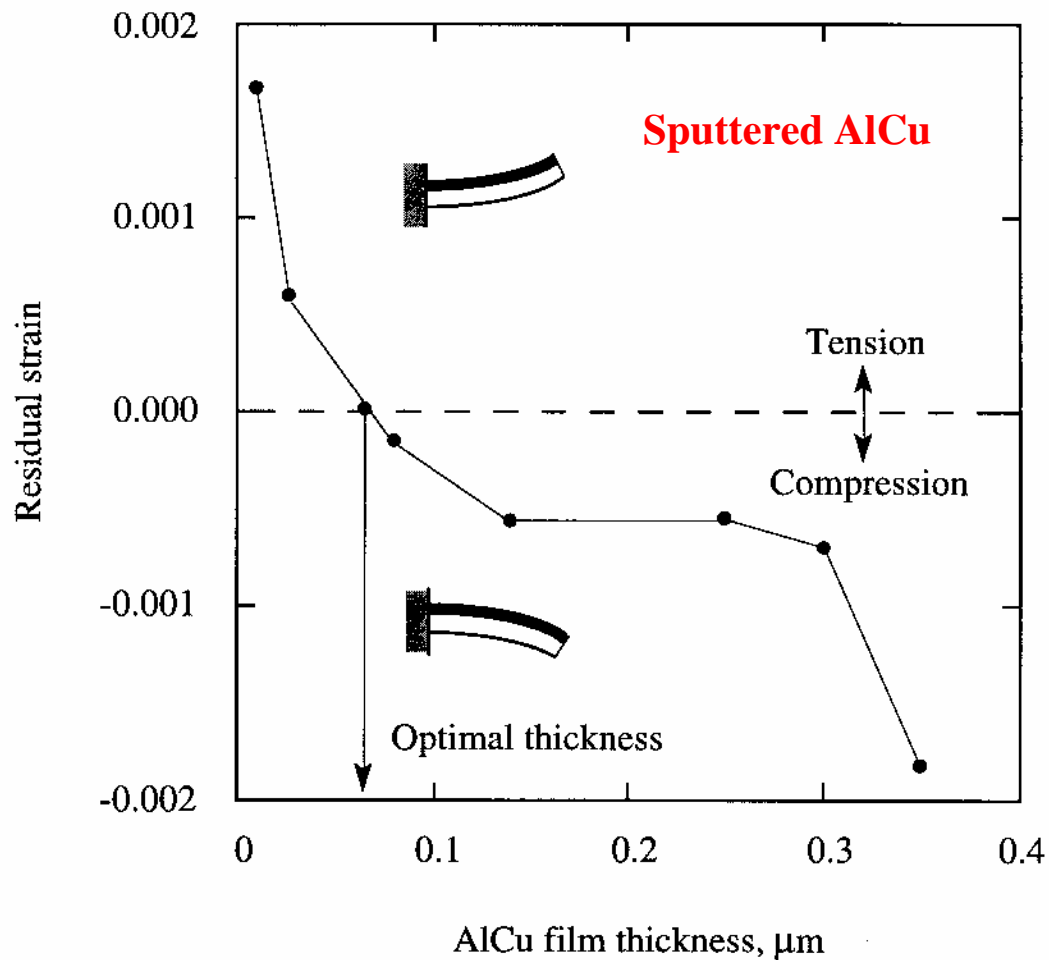
**Test cantilever deposited with a 15 nm thick *DLC* film**

**W. Fang and J.A. Wickert, *J. of Micromechanics and Microengineering*, 1995**



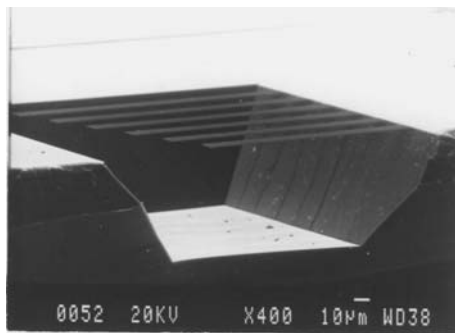


- Variation of the residual strain with the thickness of *AlCu* film

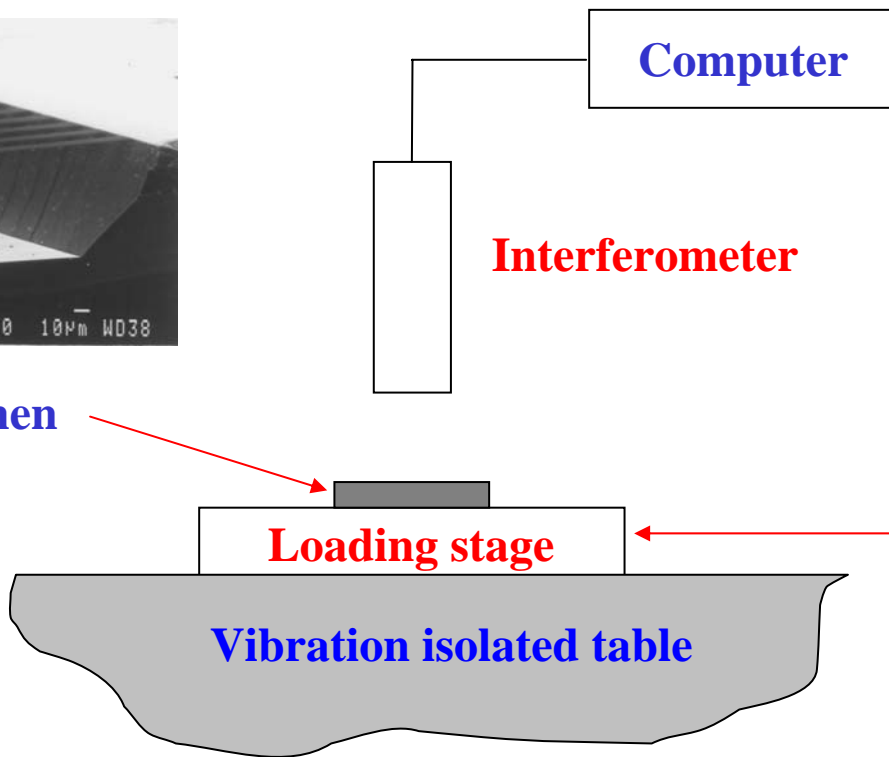




# Static Testing Platform



Specimen



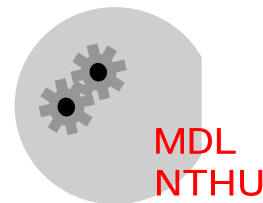
Residual stresses

Heating stage

Electromagnetic stage

Pressure source

Indenter





# Pressure load

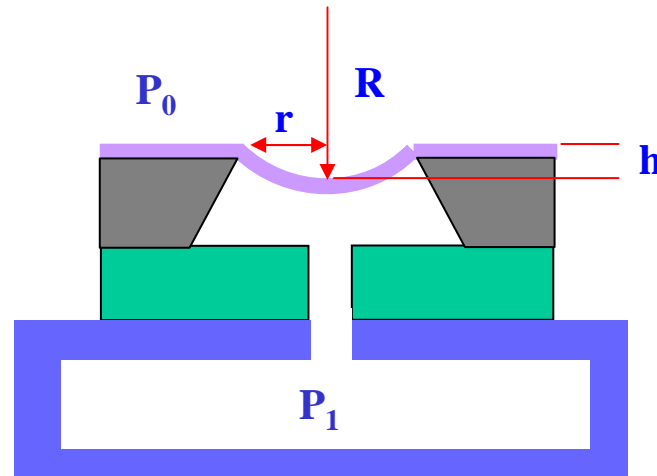
- Load-deflection test

Residual stress

Young's modulus

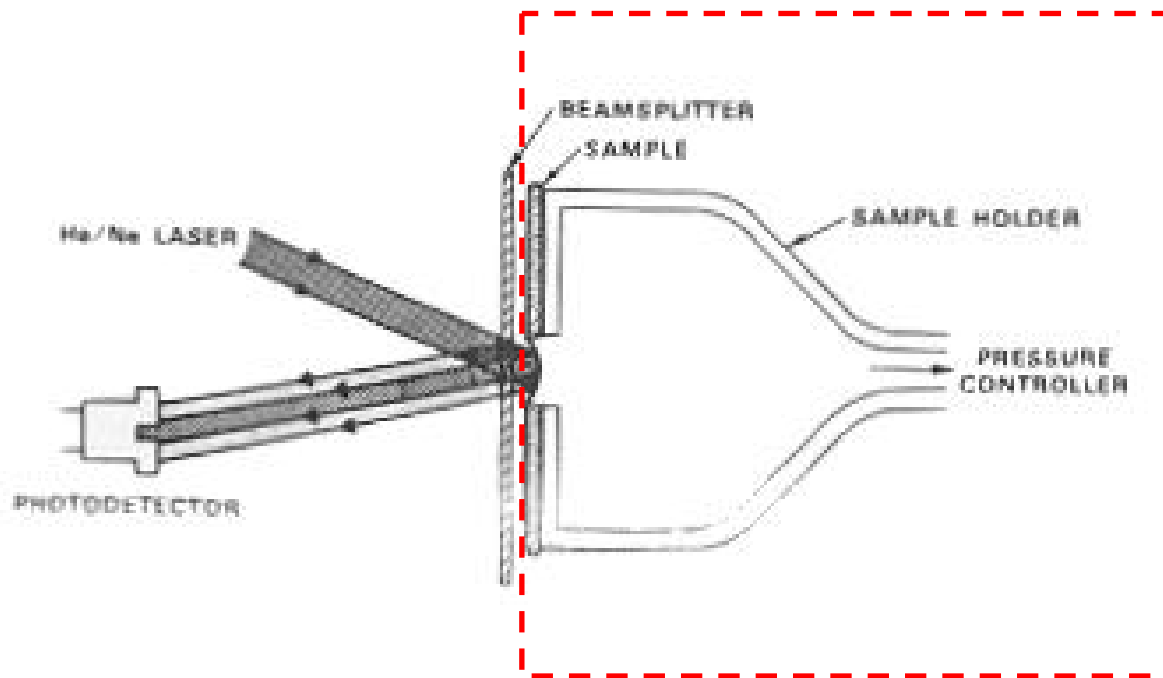
$$p = \frac{4t\sigma_0}{r^2} h + \frac{8t}{3r^4} \frac{E}{1-\nu} h^3$$

Deflection amplitude of the membrane





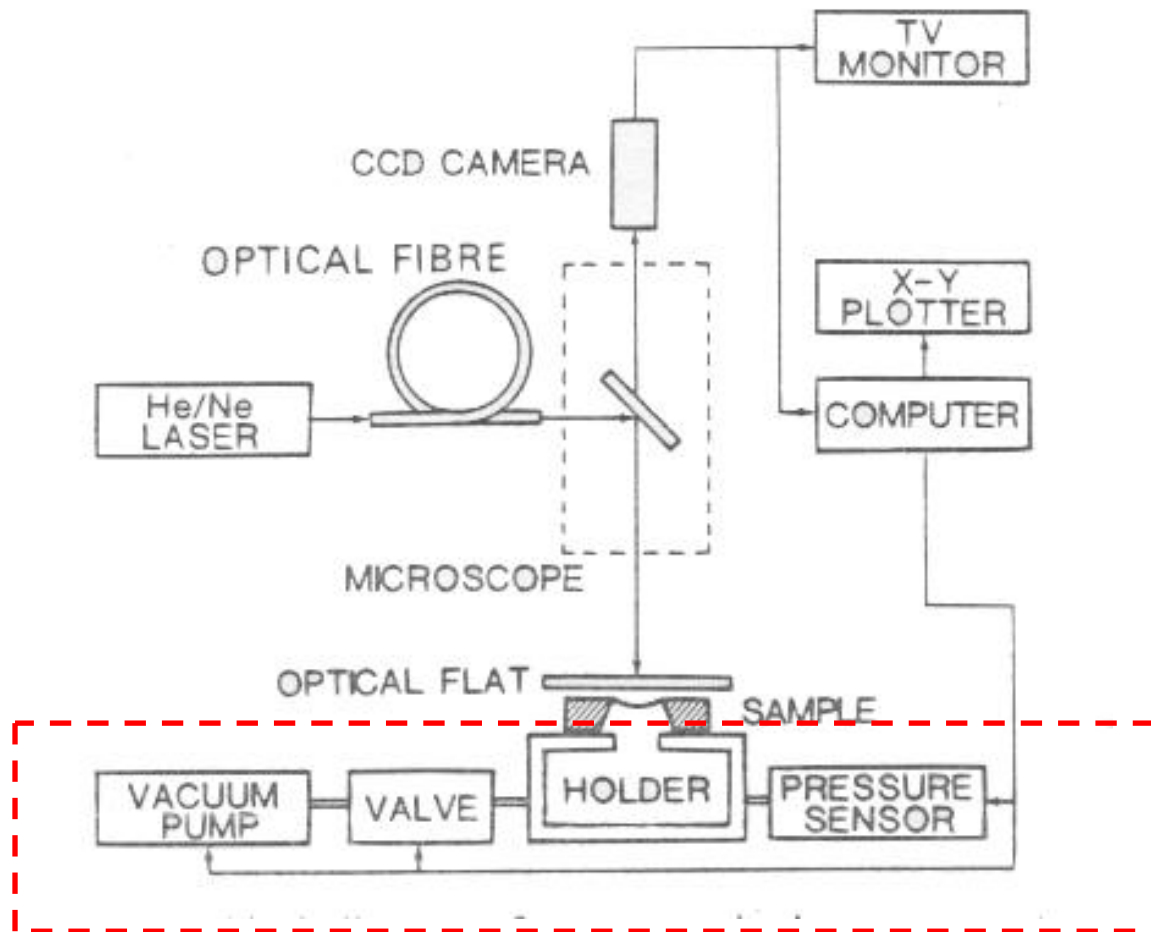
- Measurement system



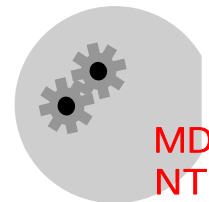
Setup for external load



- **Measurement system**

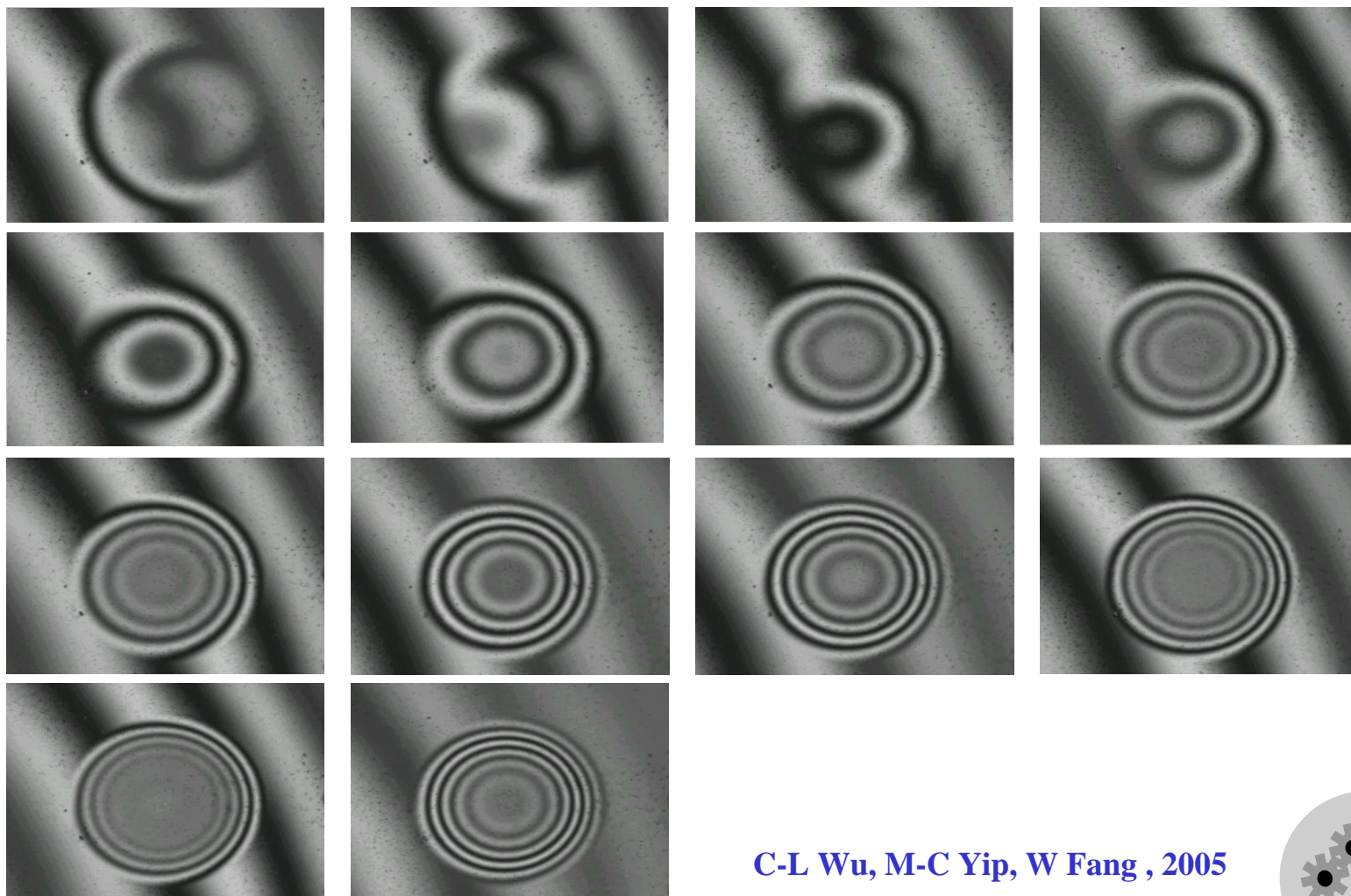


**Setup for external load**

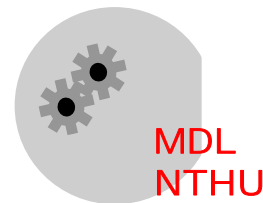




## •Bulge test



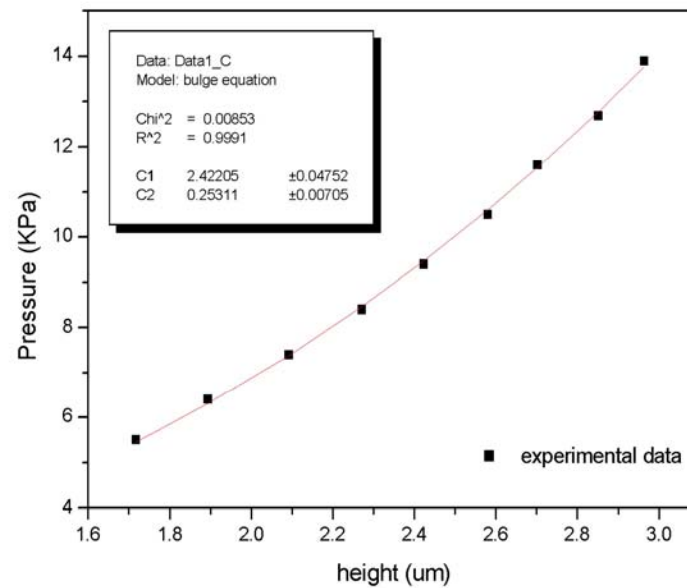
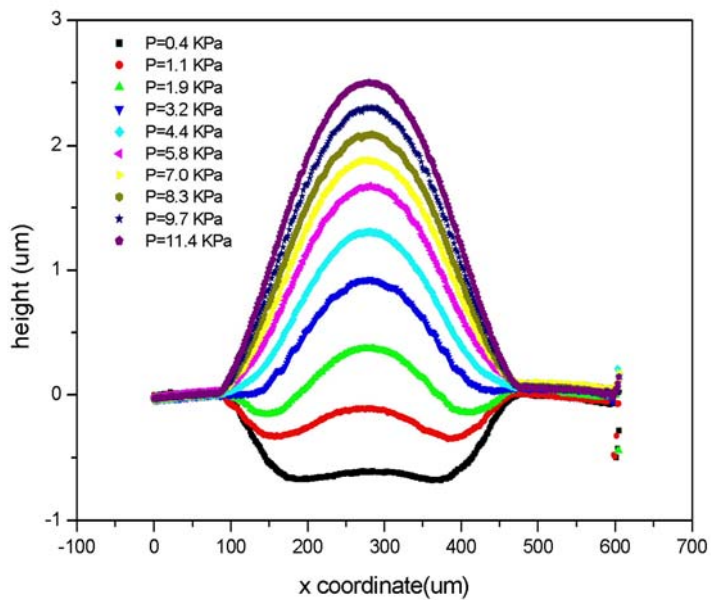
C-L Wu, M-C Yip, W Fang , 2005



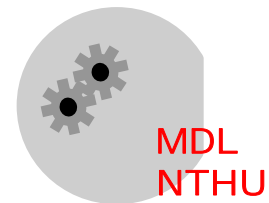




# Bulge test



C-L Wu, M-C Yip, W Fang, 2005





- **Static test**

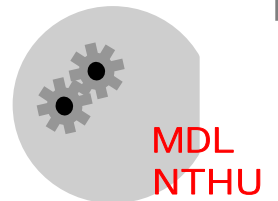
- + **Devices**

- + **Material properties – CTE**

- **Dynamic test**

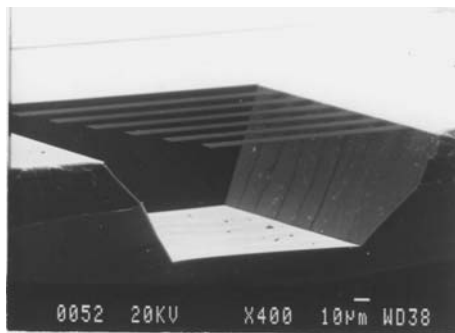
- + **Devices**

- + **Material properties**

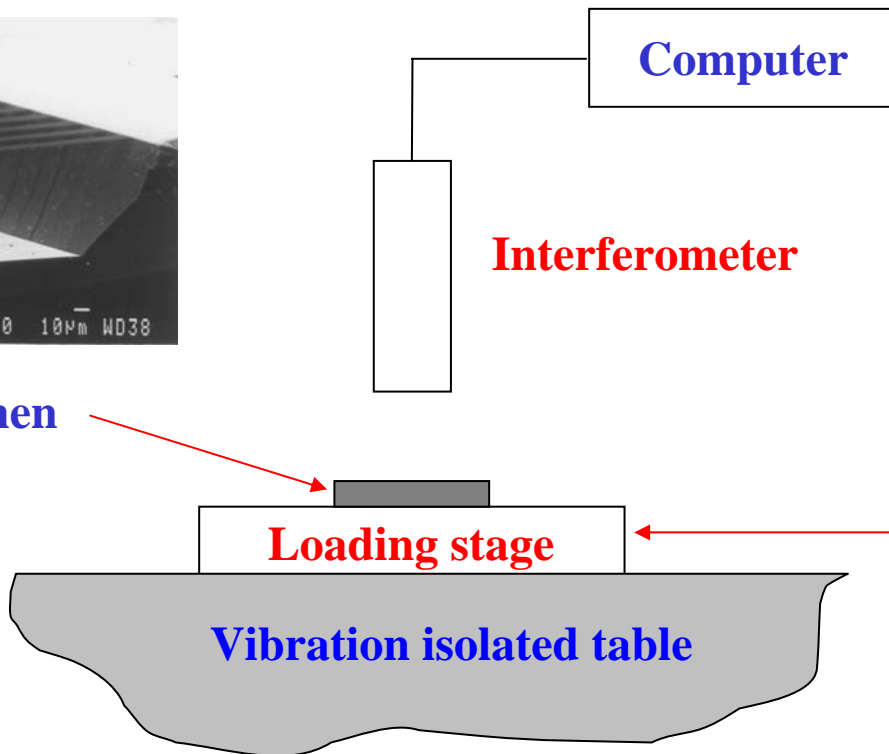




# Static Testing Platform



**Specimen**



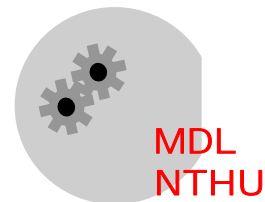
**Residual stresses**

**Heating stage**

**Electromagnetic stage**

**Pressure source**

**Indenter**

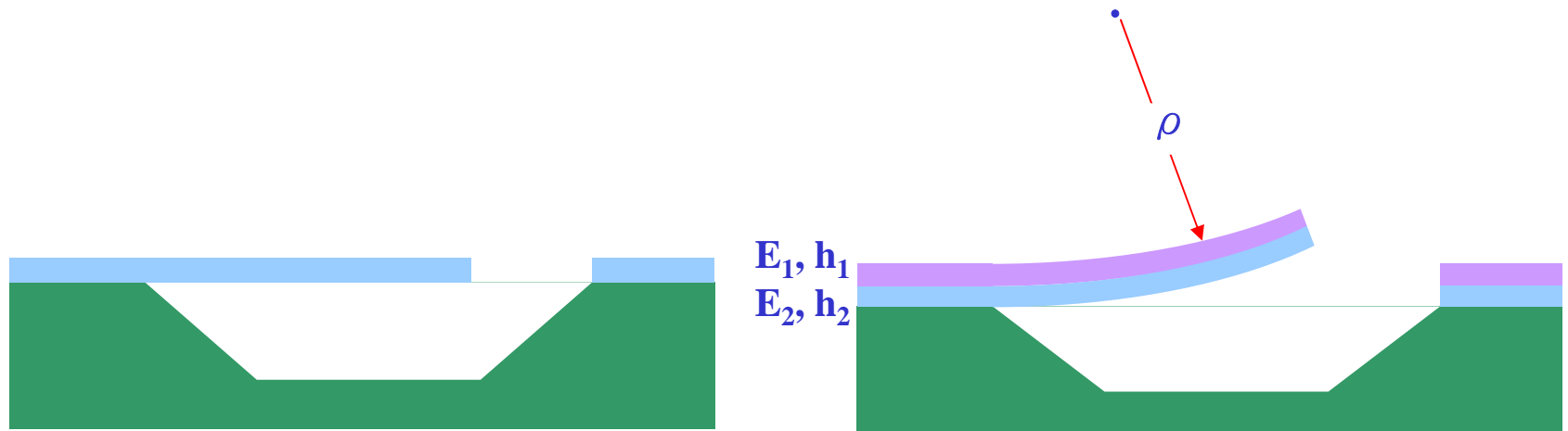




## Bi-layer approach

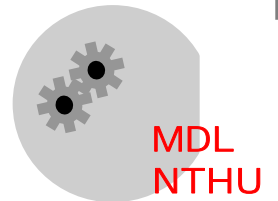
- Bi-layer - analysis**

$$\frac{1}{\rho} = \frac{6 \cdot \Delta T \cdot \Delta \alpha \cdot (1+m)^2}{h \cdot \left[ 3 \cdot (1+m)^2 + (1+m \cdot n) \cdot \left( m^2 + \frac{1}{m \cdot n} \right) \right]}$$



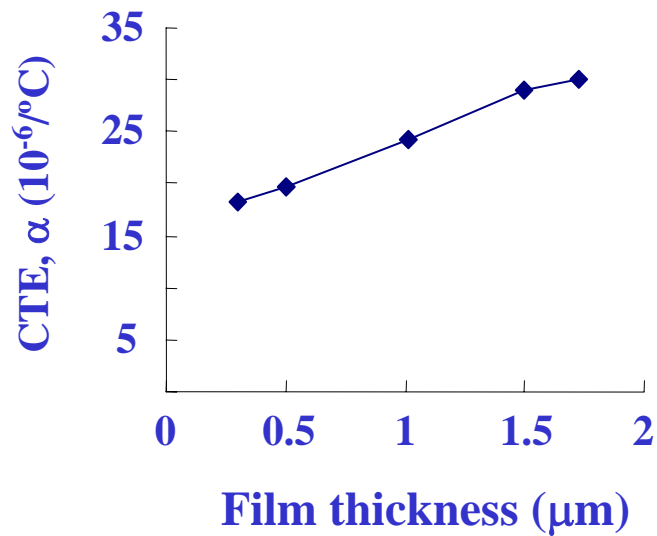
W. Fang, H.-C. Tsai, and C.-Y. Lo, *Sensors and Actuators A*, 1999

W. Fang and C.-Y. Lo, *Sensors and Actuators A*, 2000



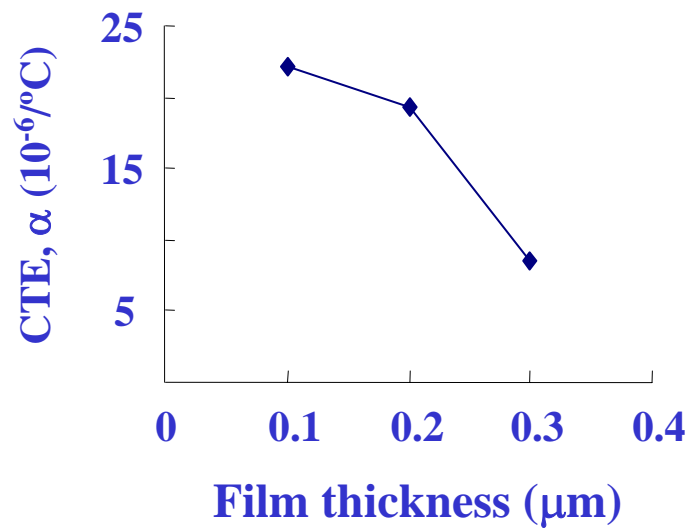


- Sputtered **Al**

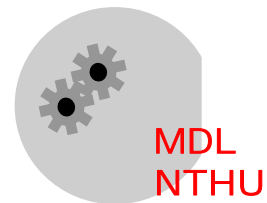


**Bulk Al :  $23.6 \times 10^{-6}/^{\circ}\text{C}$**

- E-gun **Ti**



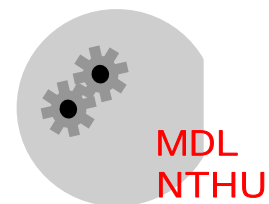
**Bulk Ti :  $8.4 \times 10^{-6}/^{\circ}\text{C}$**





- **Results**

	SiO <sub>2</sub>	W	Ti	Al
0.1 μm			22.21× 10 <sup>-6</sup>	
0.2 μm			19.4× 10 <sup>-6</sup>	
0.3 μm			9.04× 10 <sup>-6</sup>	18.23× 10 <sup>-6</sup>
0.5 μm		5.6× 10 <sup>-6</sup>		19.61× 10 <sup>-6</sup>
1 μm	0.25× 10 <sup>-6</sup>			24.14× 10 <sup>-6</sup>
1.5 μm				28.92× 10 <sup>-6</sup>
1.73 μm				29.97× 10 <sup>-6</sup>





- **Static test**

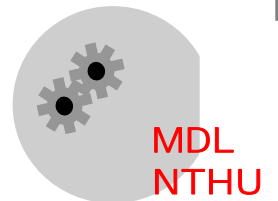
- + **Devices**

- + **Material properties – Elastic modulus**

- **Dynamic test**

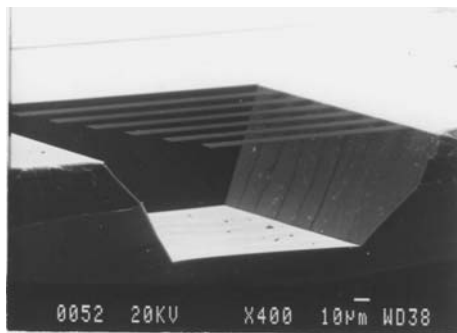
- + **Devices**

- + **Material properties**

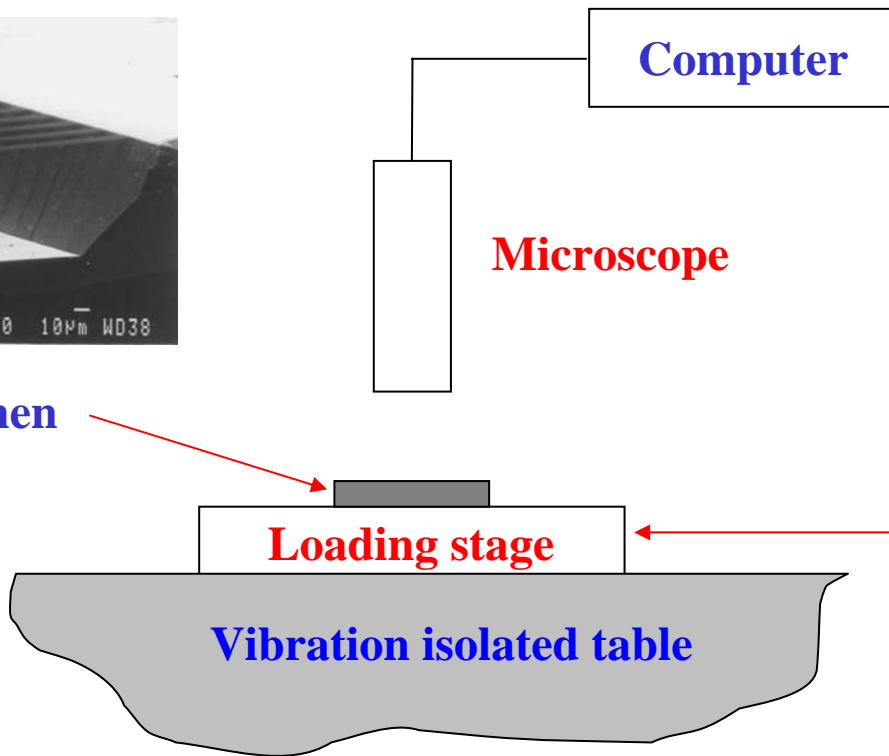




# Static Testing Platform



**Specimen**



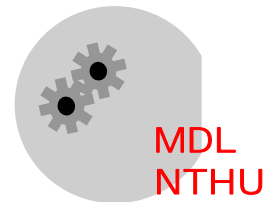
**Residual stresses**

**Heating stage**

**Electromagnetic stage**

**Pressure source**

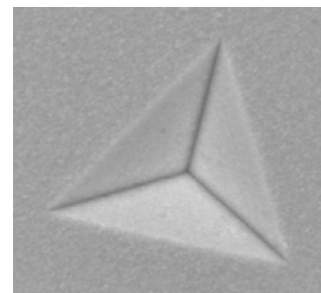
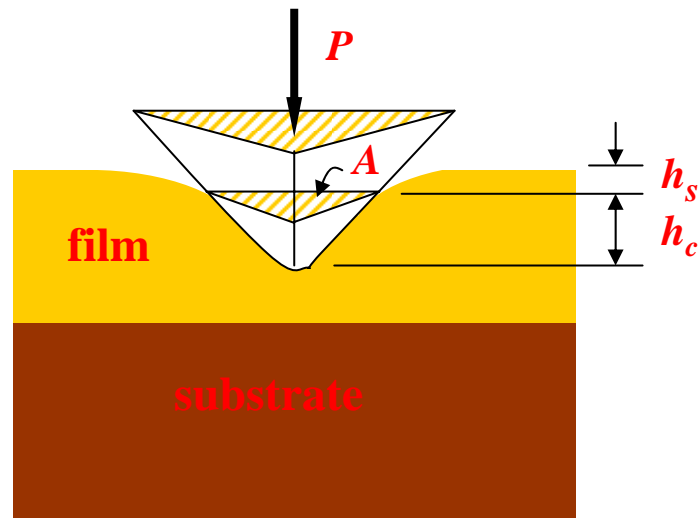
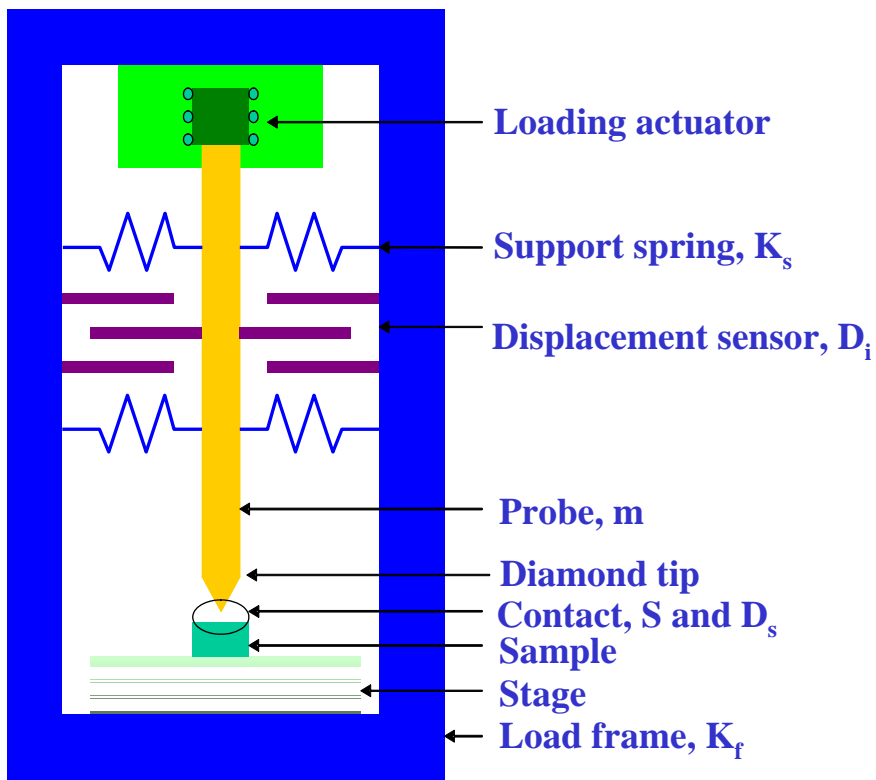
**Indenter**



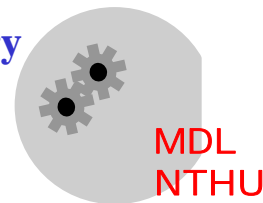




# Nanoindentation system



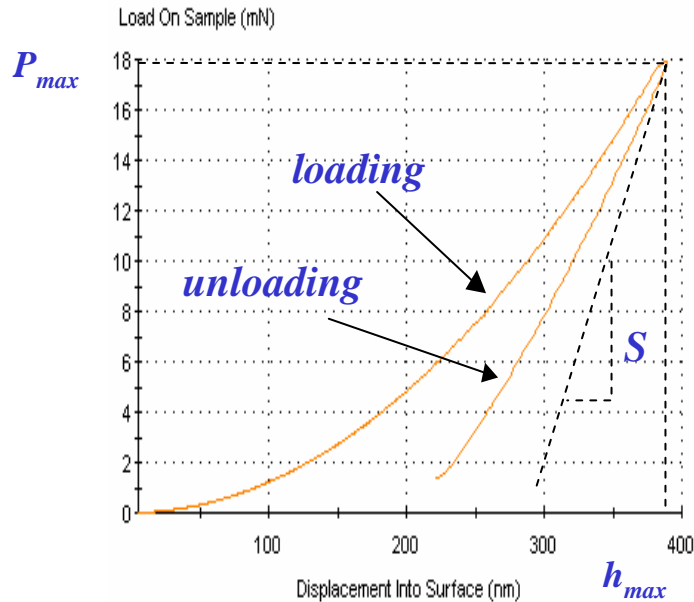
Berkovich tip geometry



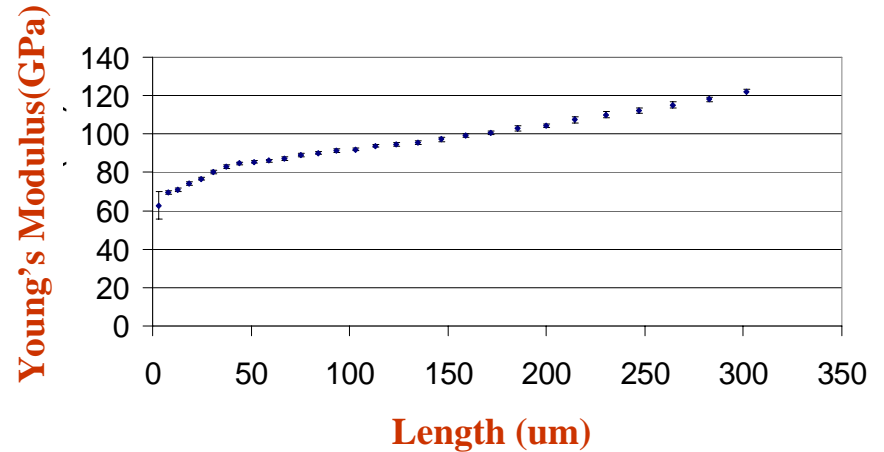


# Principle

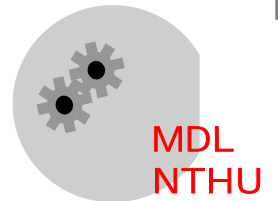
- + measured parameter: tip load and displacement
- + extracted properties: H & E



## Typical example: 0.84 $\mu\text{m}$ $\text{SiO}_2$ film

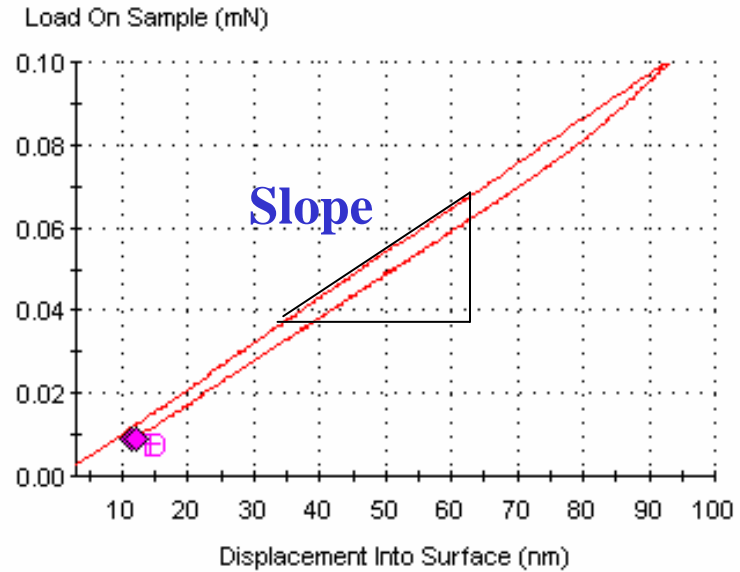
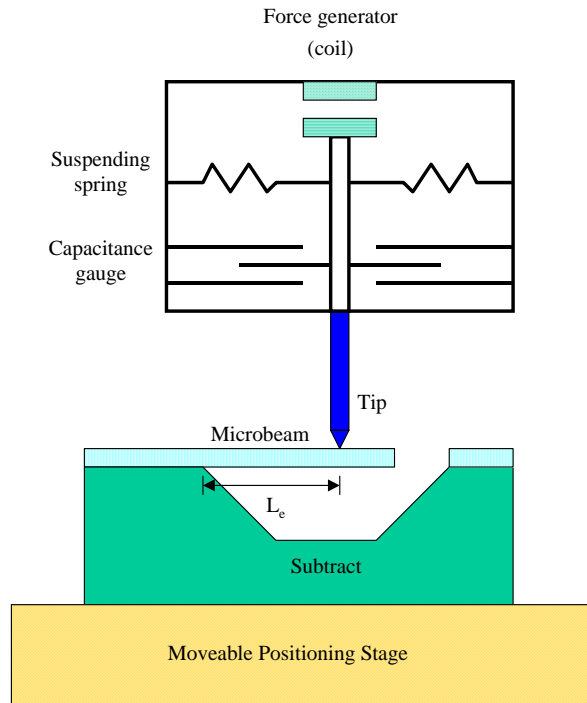


$E_{ave} = 88\text{GPa}$  (5%~10% of film thickness)



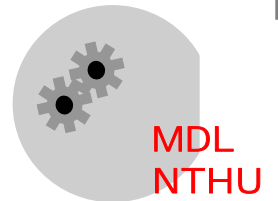


# Nanoindentation system for bending beam test



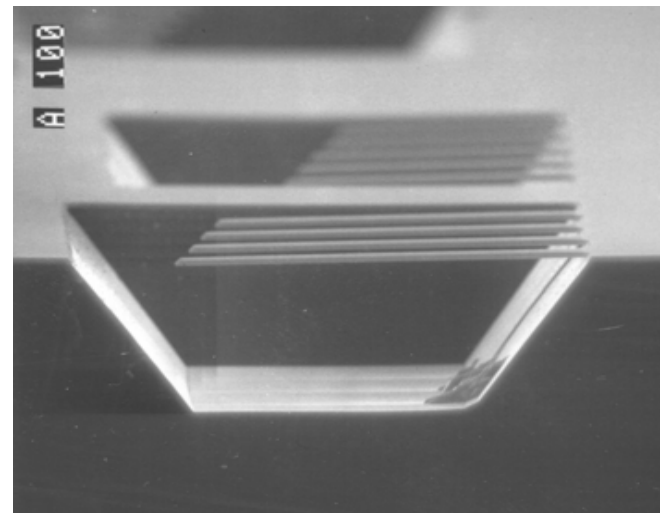
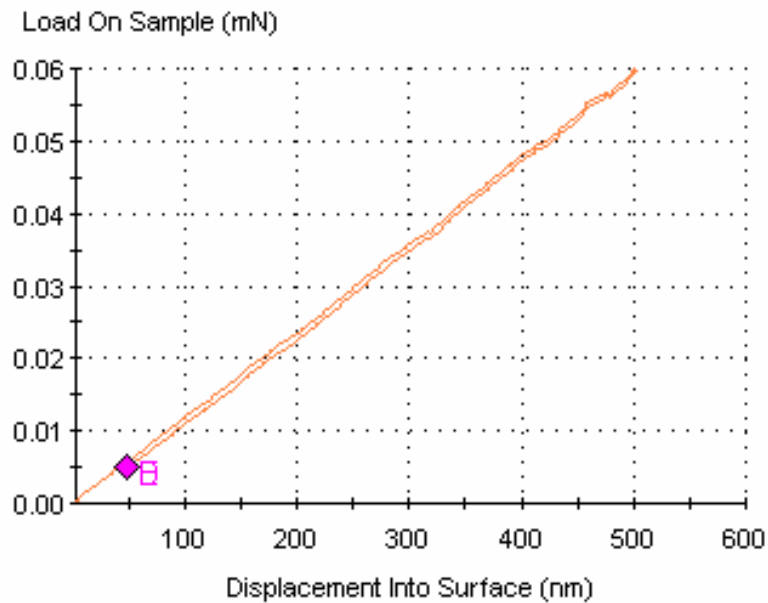
→ Slope is the stiffness of cantilever

$$E = \frac{4l^3}{wt^3} \frac{P}{\delta}$$





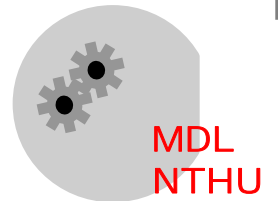
- Stiffness test of the SiO<sub>2</sub> cantilever



$$E = 71.3 \text{ GPa}$$

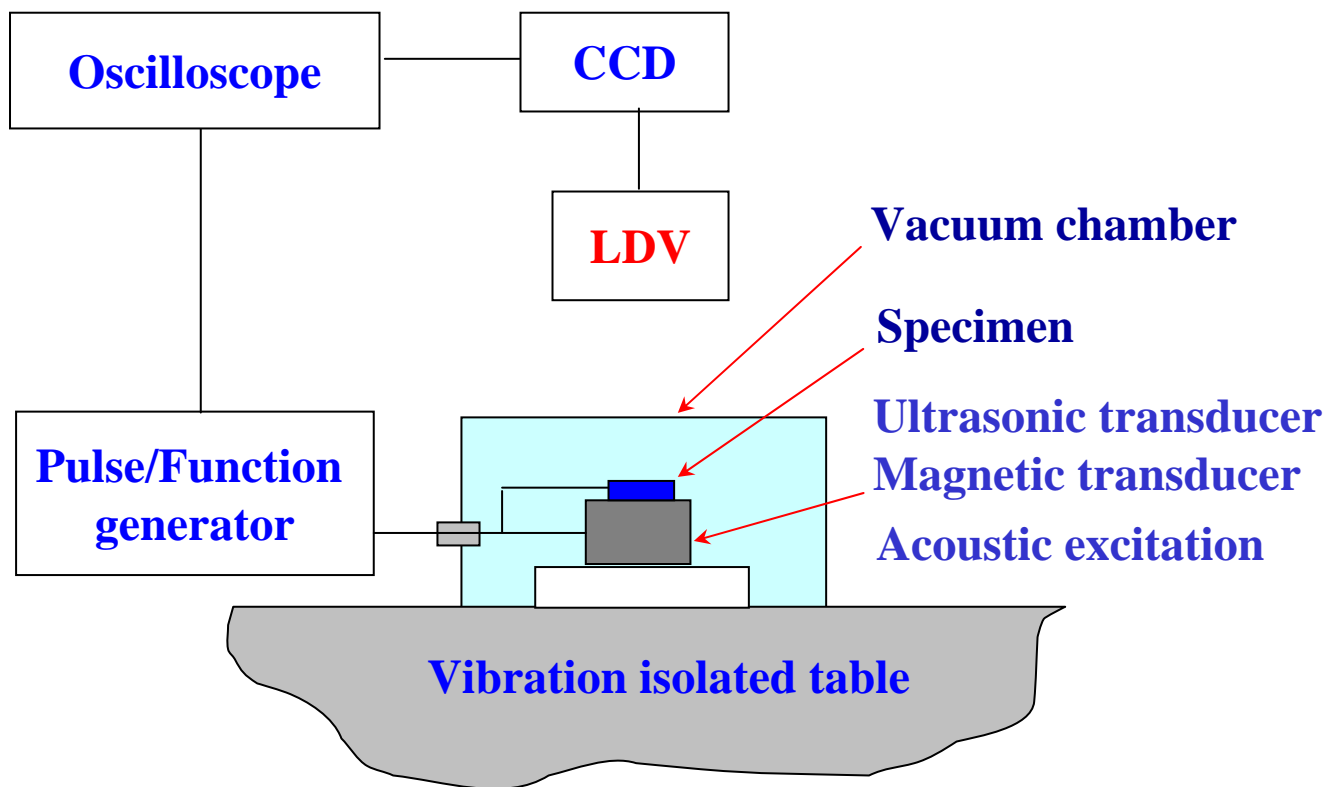


- **Static test**
  - + **Devices**
  - + **Material properties**
  
- **Dynamic test**
  - + **Devices**
  - + **Material properties**

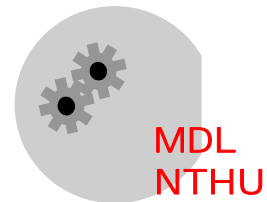




# Dynamic Testing Platform

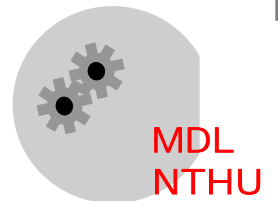


W. Lai and W. Fang, *Sensors and Actuators A*, 2001



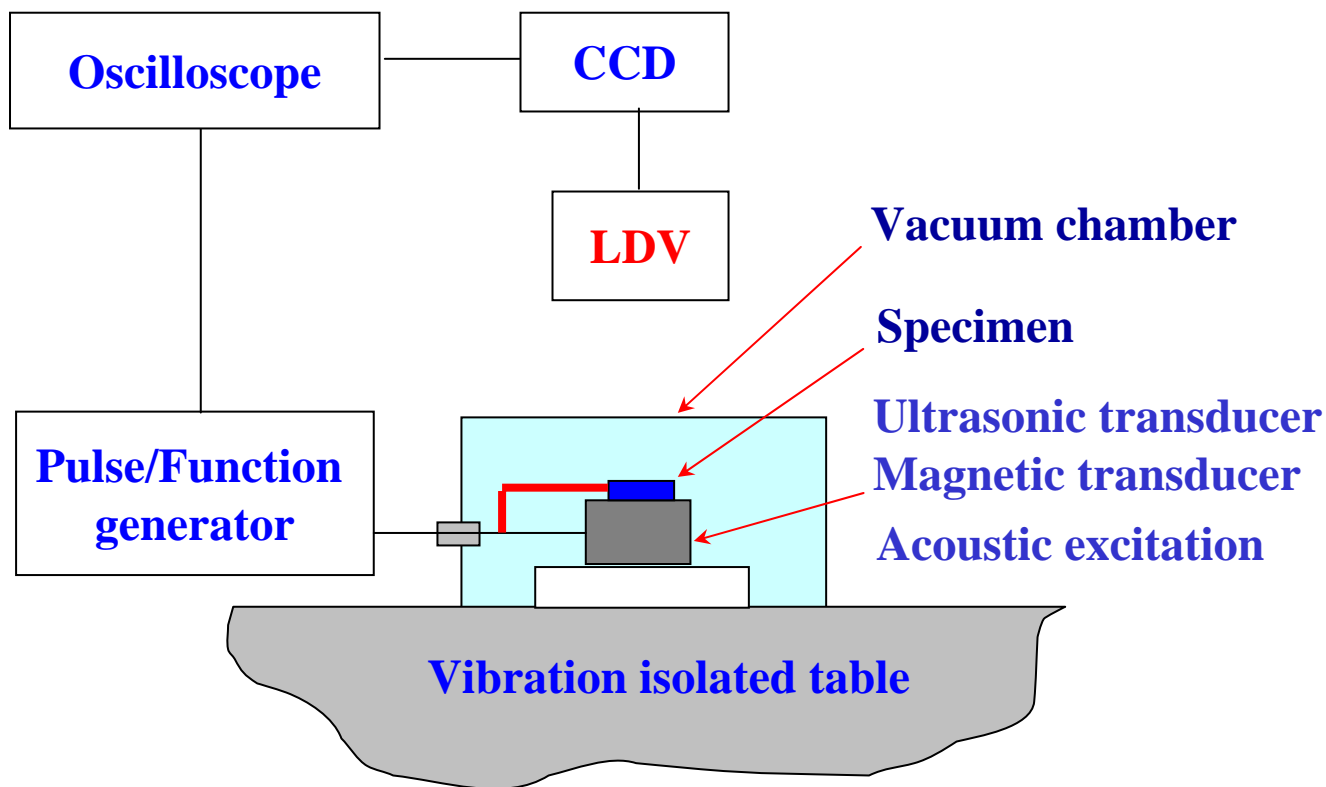


- **Static test**
  - + **Devices**
  - + **Material properties**
  
- **Dynamic test**
  - + **Devices**
  - + **Material properties**

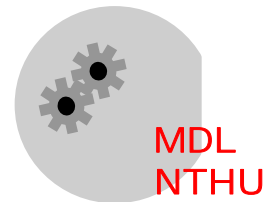




# Dynamic Testing Platform



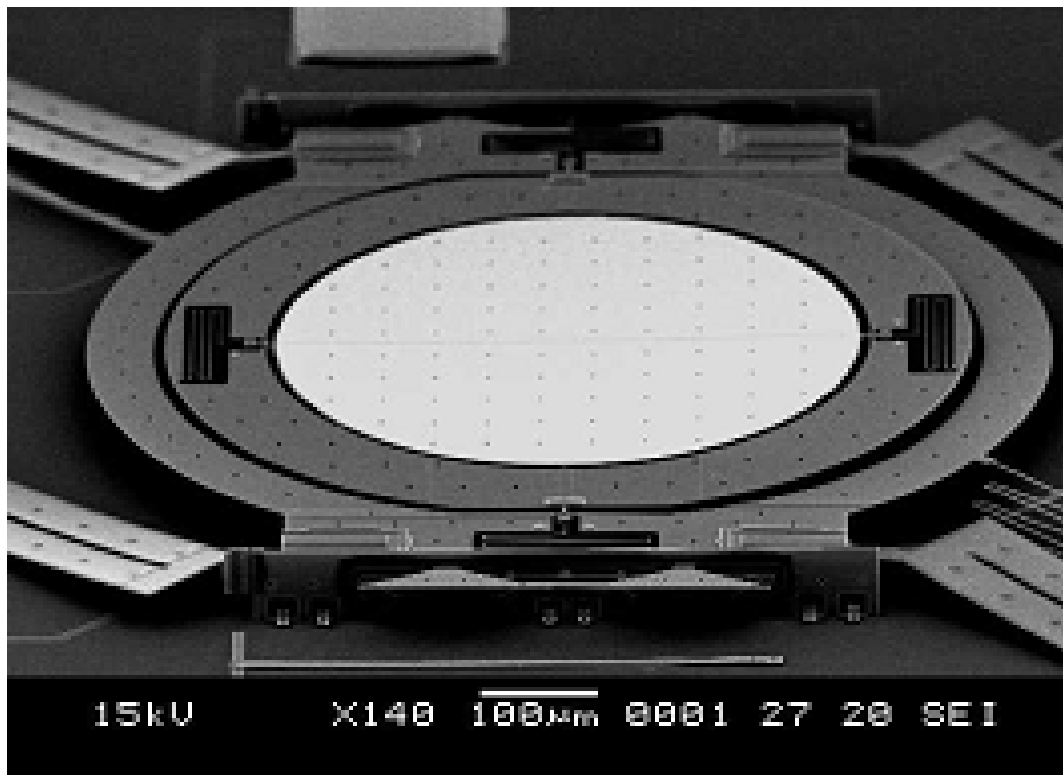
W. Lai and W. Fang, *Sensors and Actuators A*, 2001



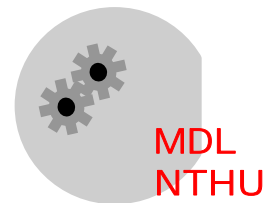


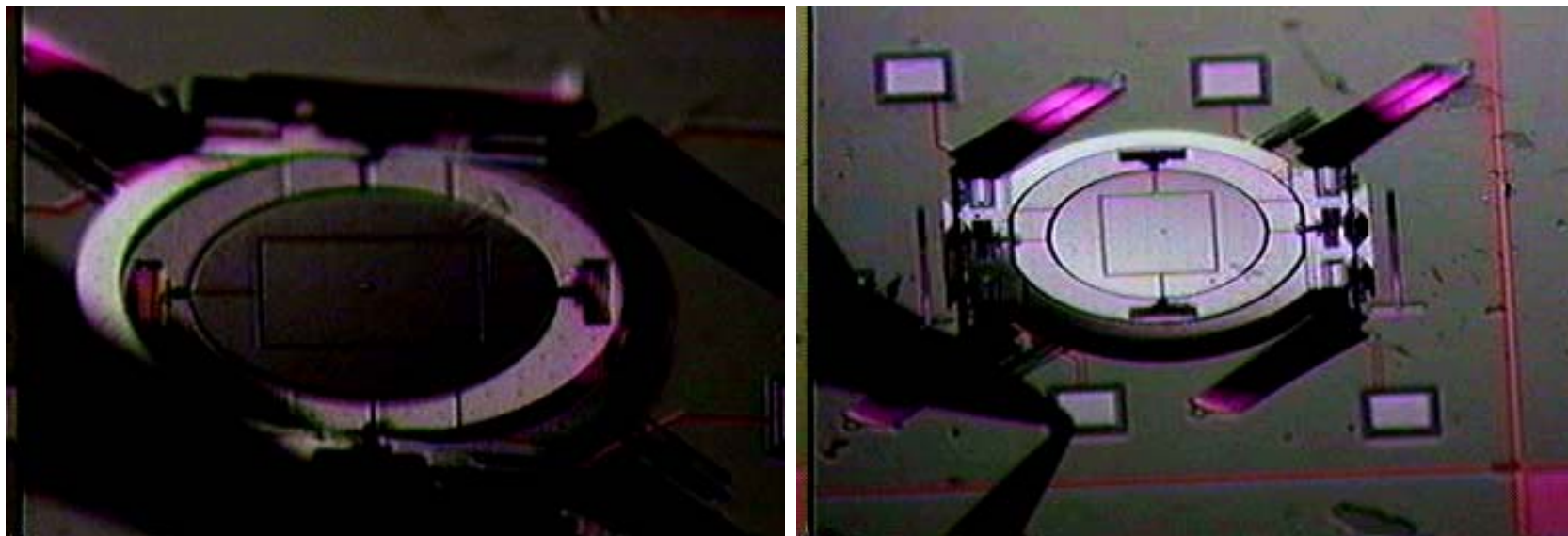


## Electrostatic actuator: optical scanner



Y.-P. Ho, M. Wu, H.-Y. Lin and W. Fang, *IEEE Optical MEMS '02*, 2002





Y.-P. Ho, M. Wu, H.-Y. Lin and W. Fang, *IEEE Optical MEMS '02*, 2002



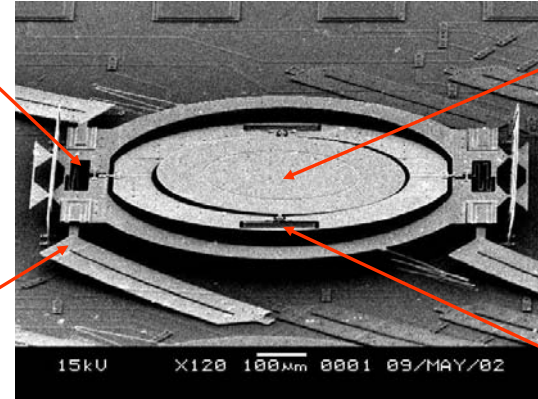
# • Frequency response

Torsional Bar

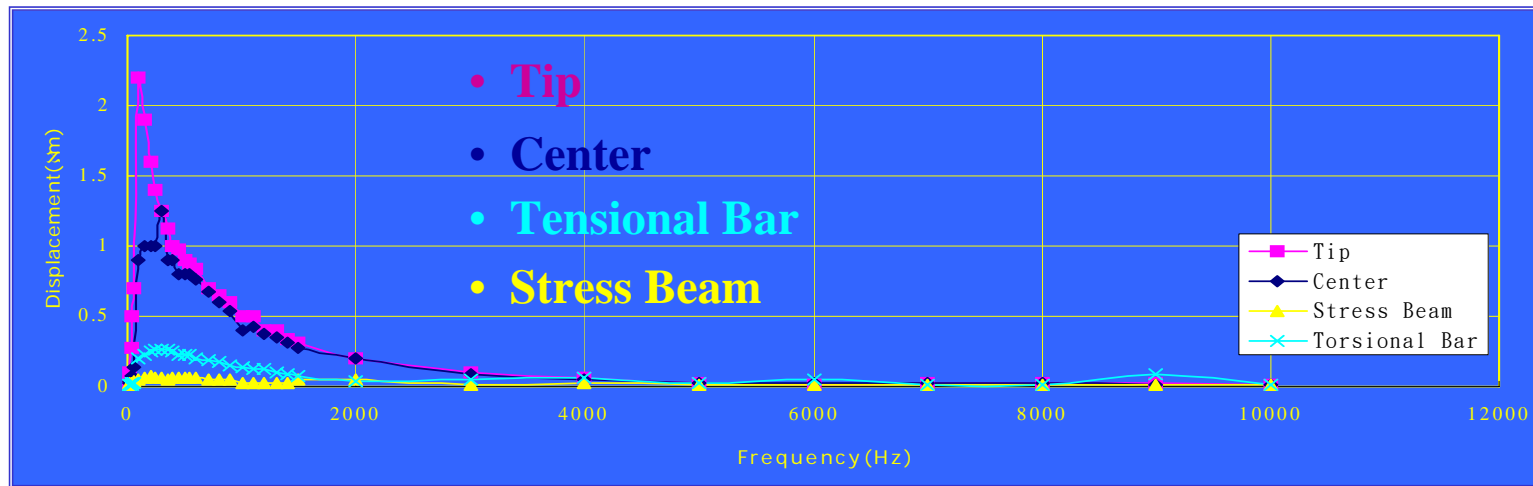
Center

Driving Outer Ring

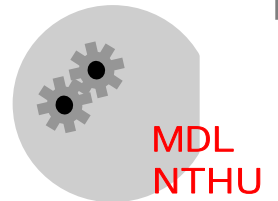
Stress Beam



Tip

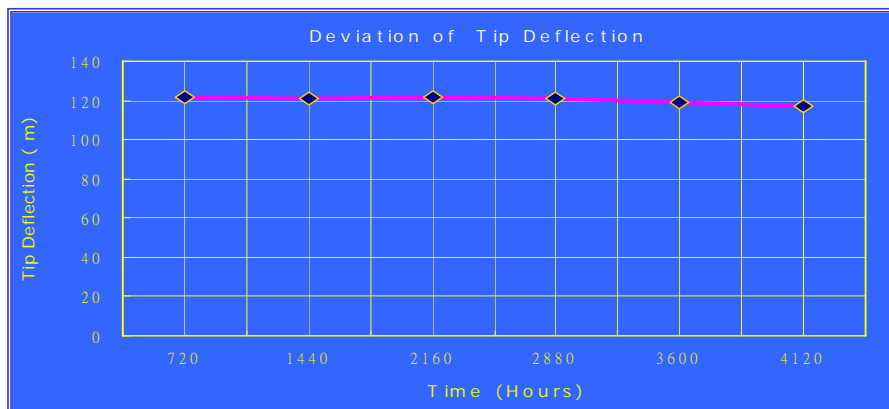
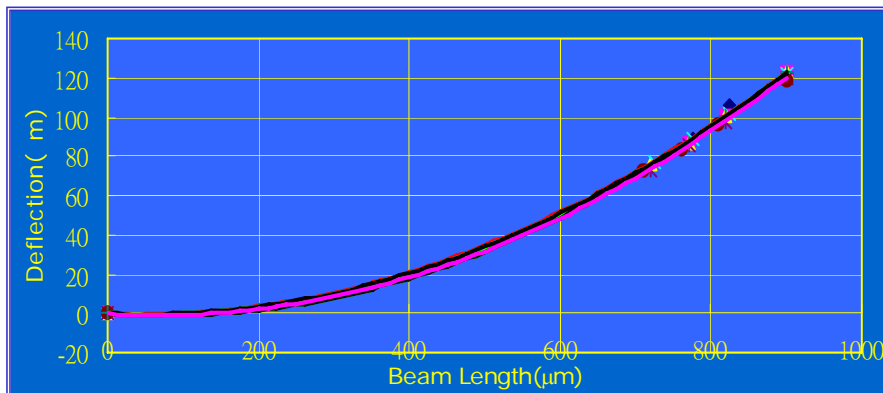
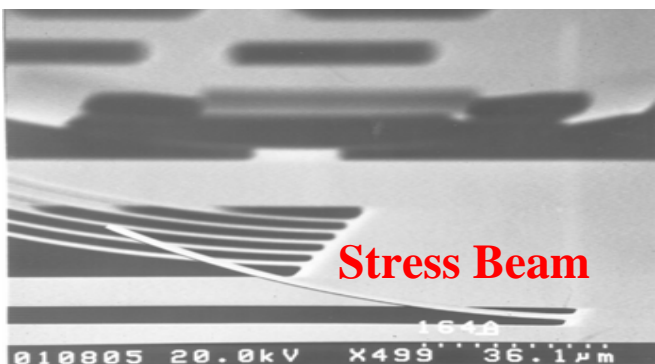
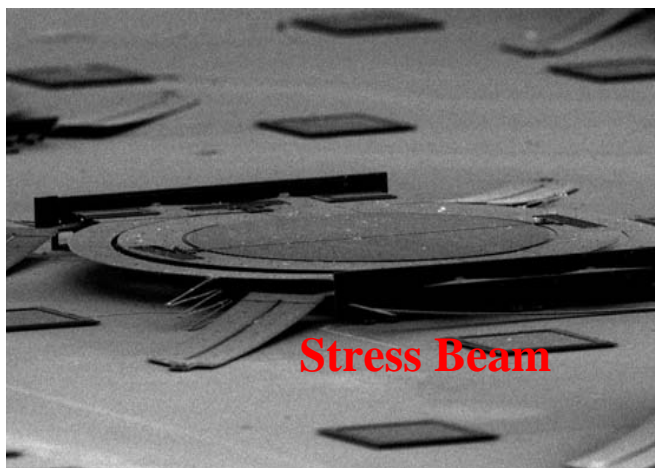


Coupling problem – the torsional & wobble motion





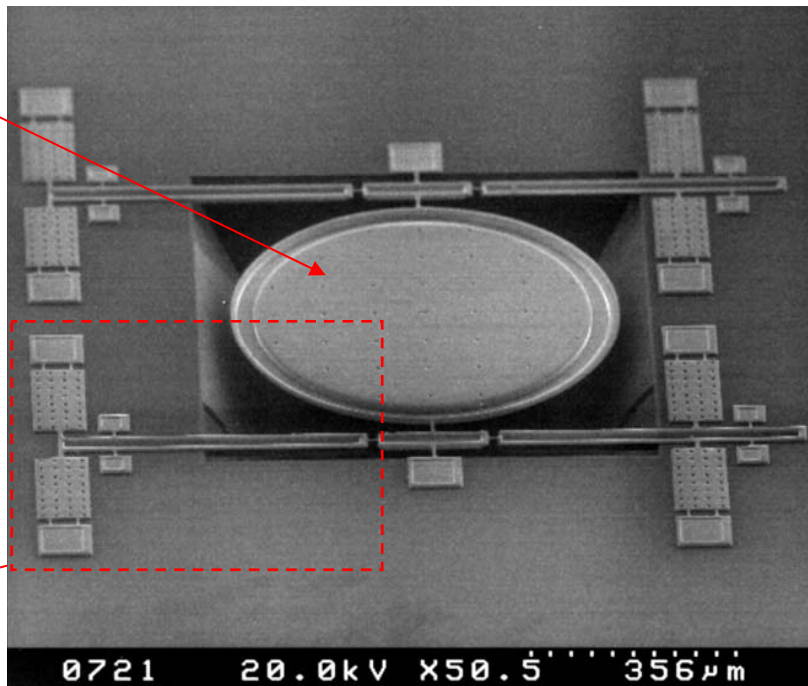
## • Reliability test





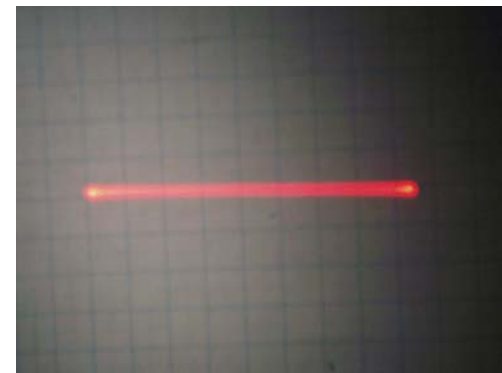
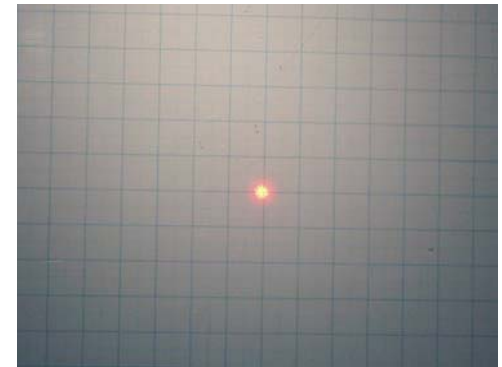
# Electrostatic actuator: optical scanner

Mirror  
(Follower)



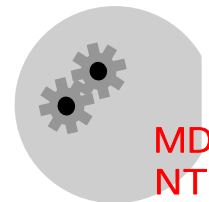
EDLA  
engine  
(Driver)

1 cm  
→ ←



H.-Y. Lin and W. Fang, *IEEE Optical MEMS*, Kauai, Hawaii, 2000

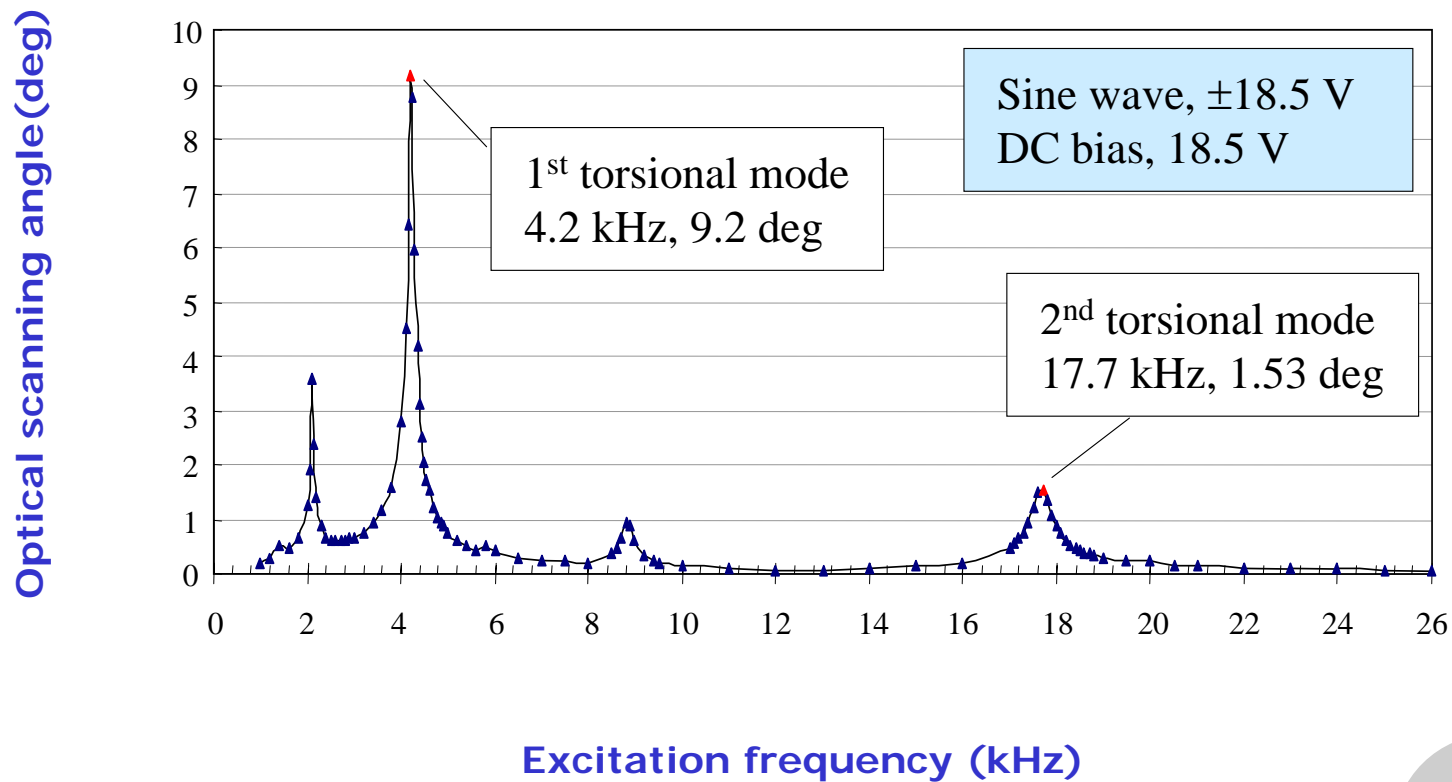
H.-Y. Lin and W. Fang, the *ASME IMECE*, Orlando, FL, 2000



MDL  
NTHU

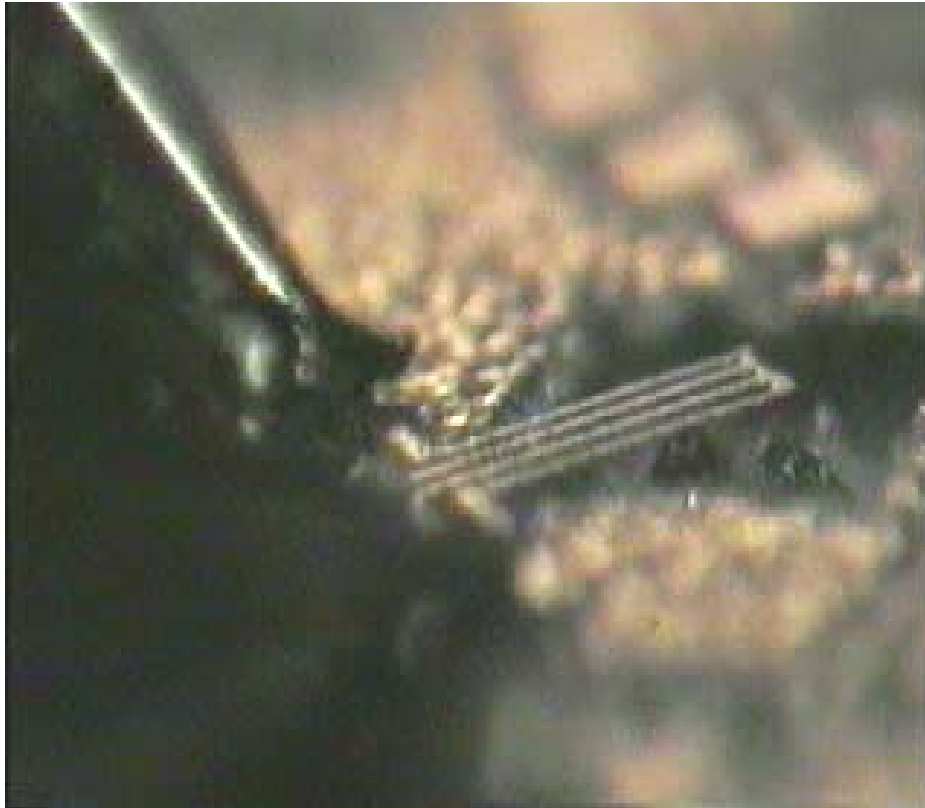


- Measured frequency response





## Electrothermal actuator

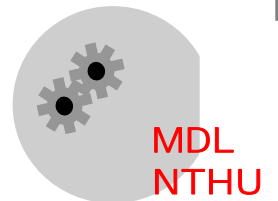


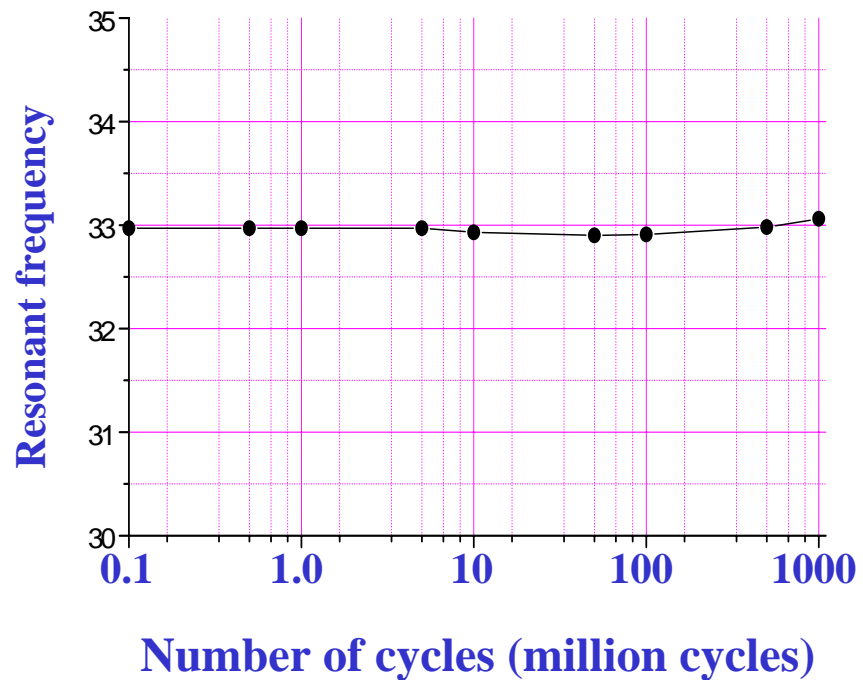
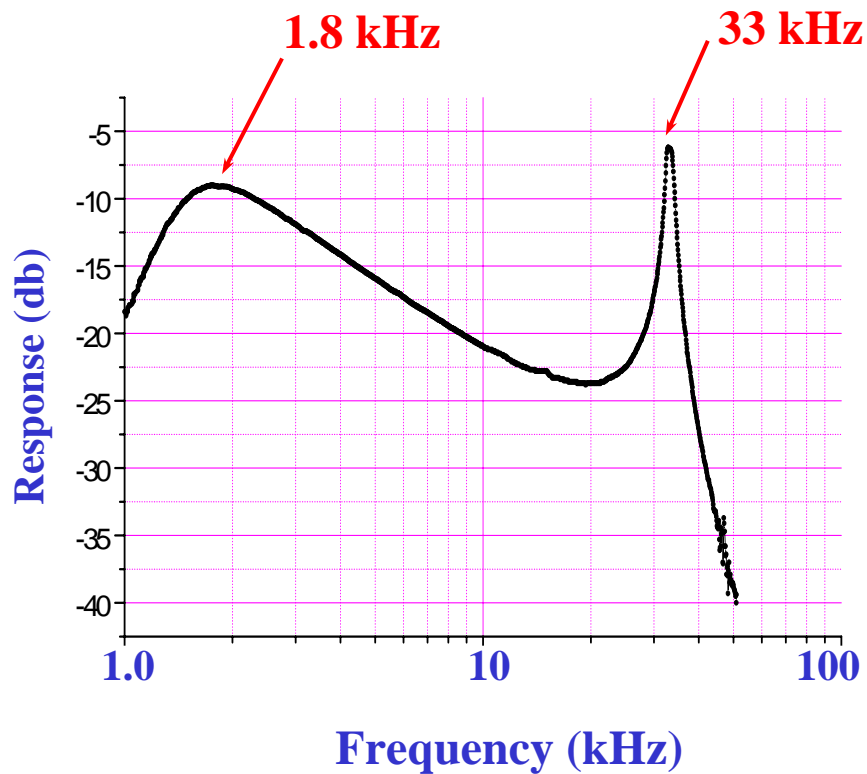
- Mono layer – long life time
- Bi-direction (DC mode)
- High frequency (AC mode)

**Driving voltage : 5 volts**

**Output displacement : 7  $\mu\text{m}$**

W.-C. Chen, J. Hsieh, and W. Fang, *IEEE MEMS'02*, Las Vegas, NV, 2002









- **Static test**

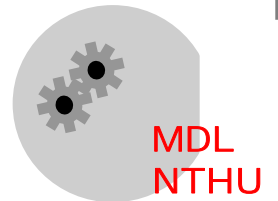
- + **Devices**

- + **Material properties**

- **Dynamic test**

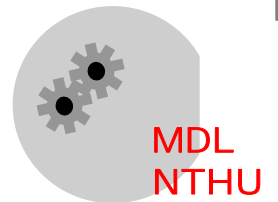
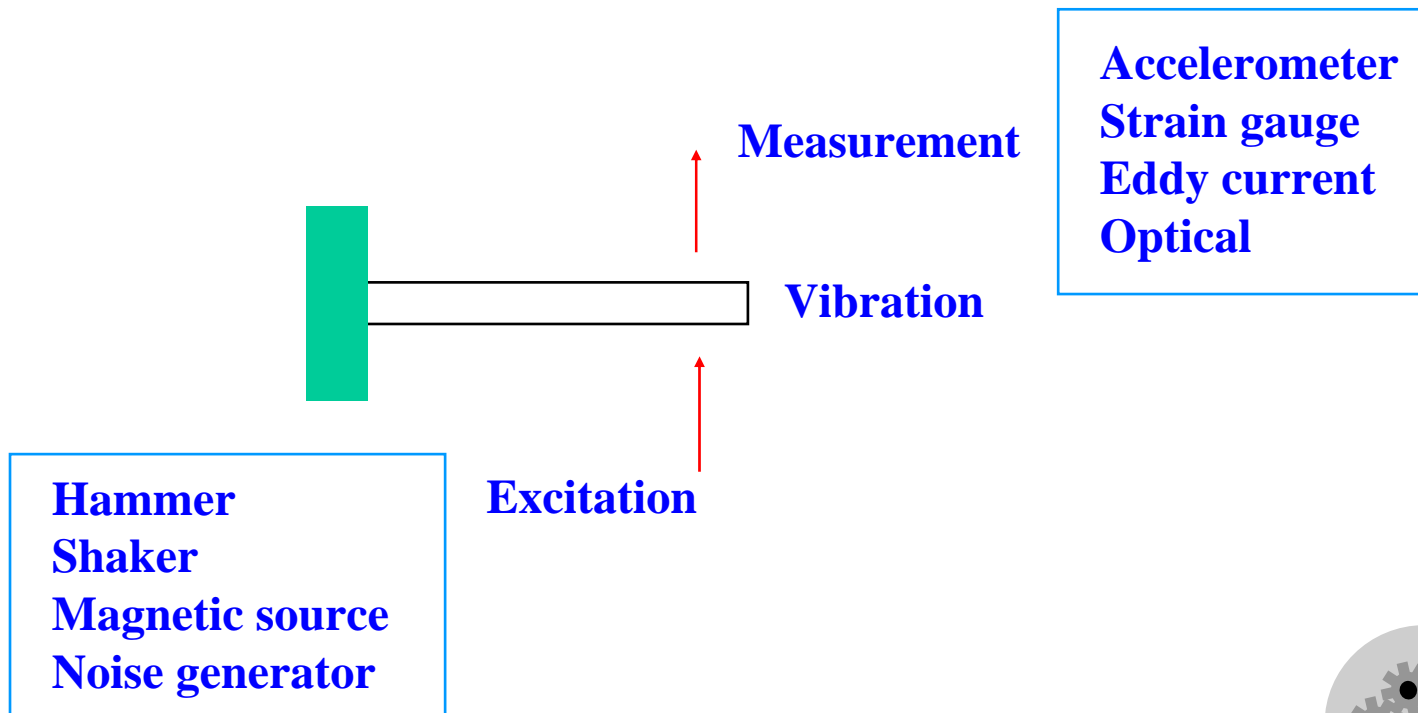
- + **Devices**

- + **Material properties – Resonant frequency, damping coefficient**





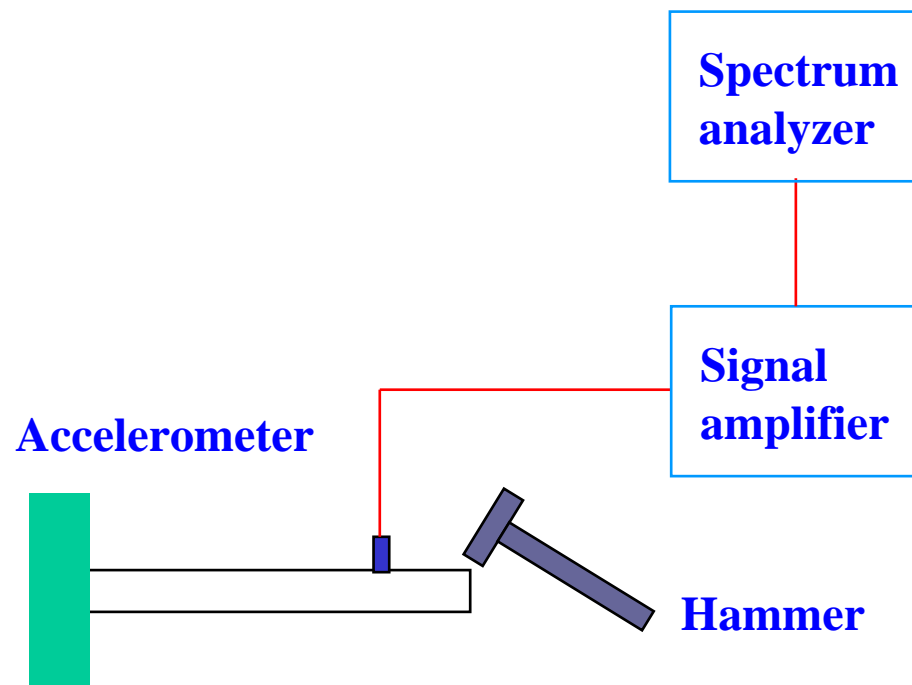
- When the **excitation frequency** of the structure coincides with its **natural frequencies**, its response will become extremely large
- In general, the vibration test requires a **excitation source** and a **measurement device**





- **Example 1**

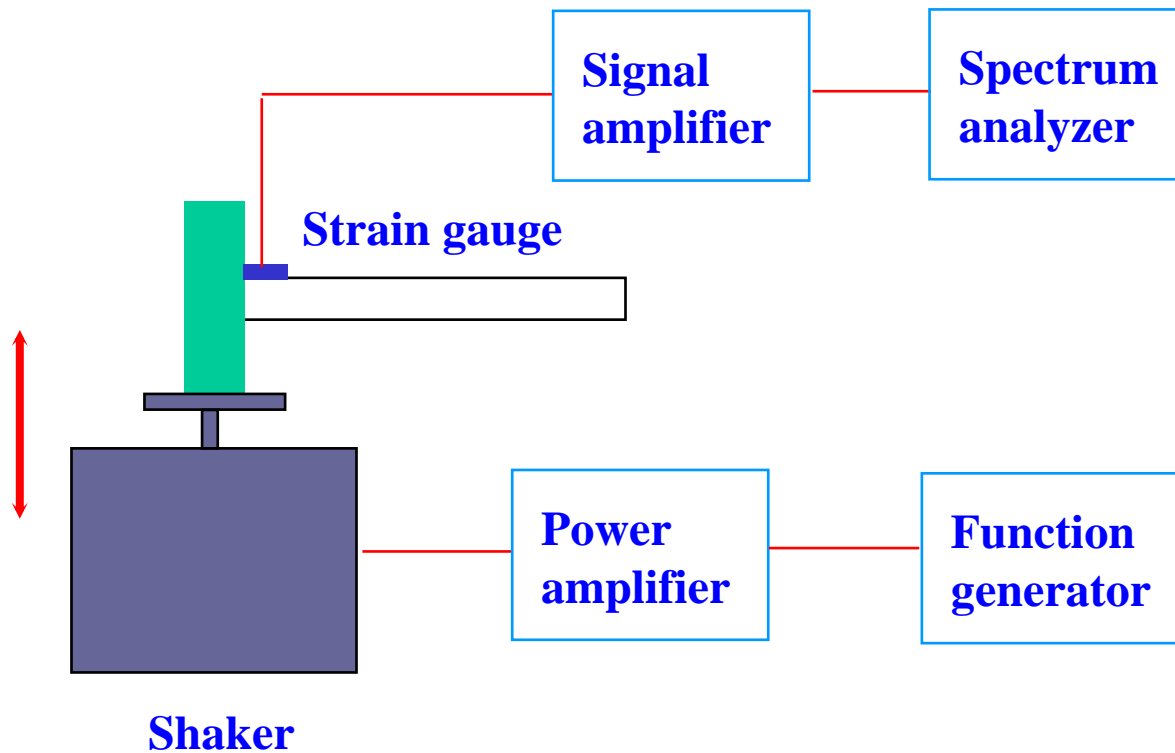
- + Structure excited by a **hammer** and detect by an **accelerometer**
- + In principle, **all of the vibration modes** will be excited after impact





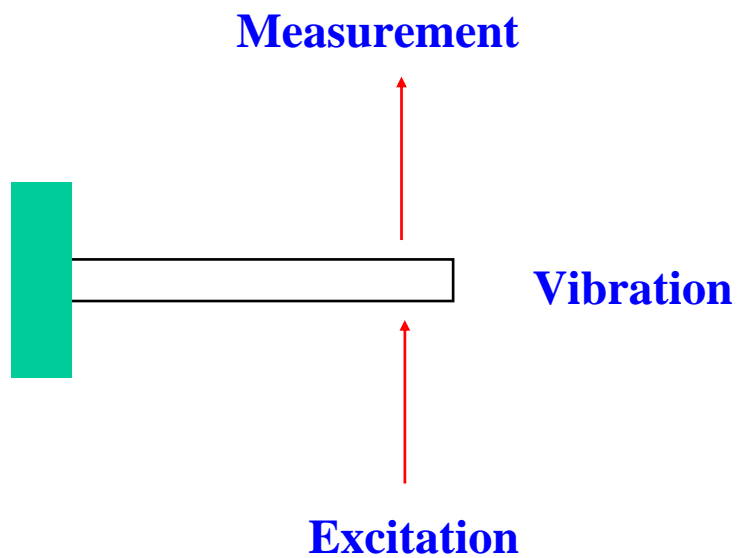
- **Example 2**

+ Structure excited by a **shaker** and detect by a **strain gauge**



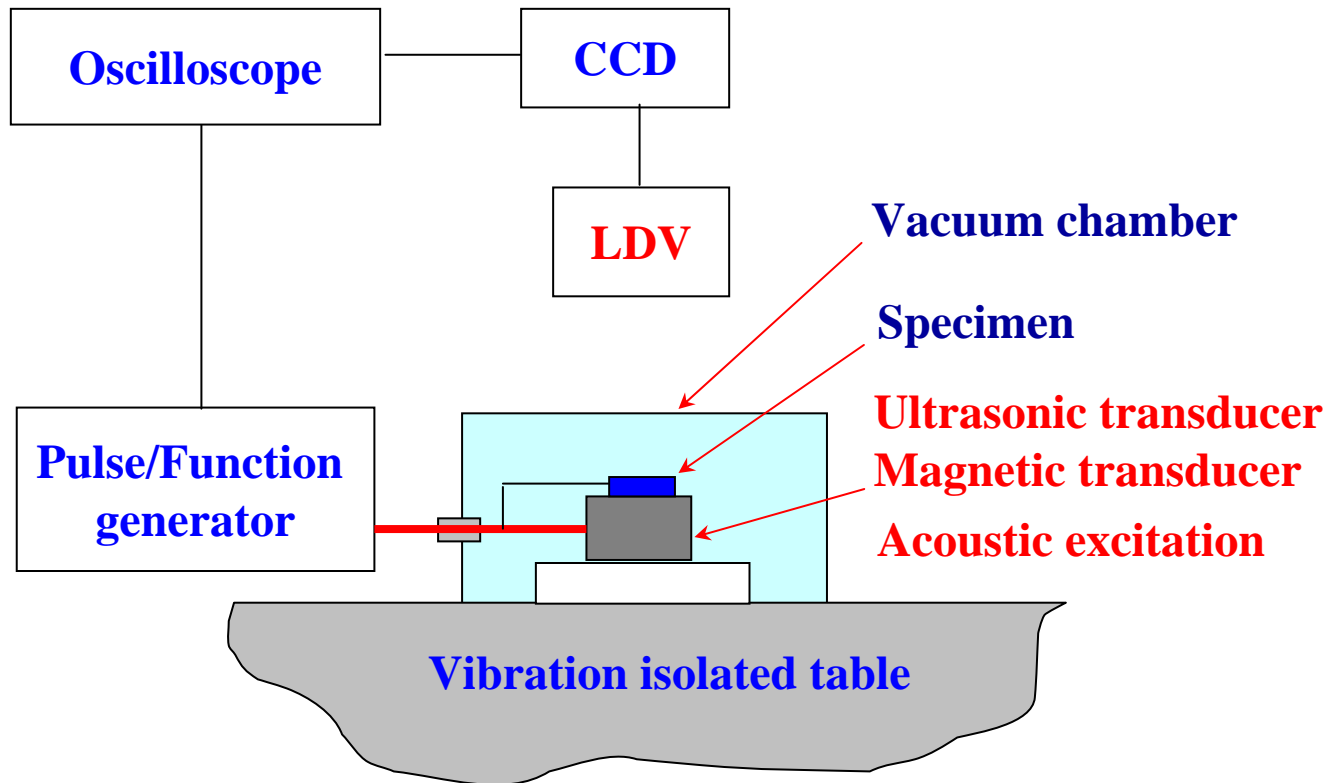


- **How to excite?**
- **How to sense?**





# Dynamic Testing Platform

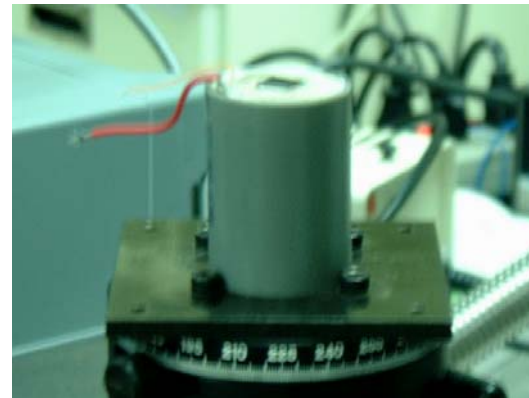




# Ultrasonic transducer

- **Ultrasonic Transducer: Pulse and Harmonic excitations**
- **The frequency range of the excitation can reach ~10 MHz**

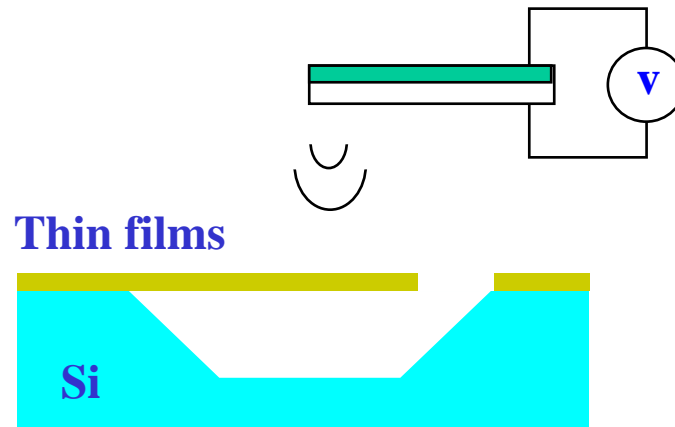
Thin films





## Acoustic excitation

- The frequency range of the wave generated by a **loudspeaker** is around 20 Hz ~ 20 KHz
- The frequency range of the wave generated by a **piezoelectric transducer** is around 0 ~ 1.2 MHz

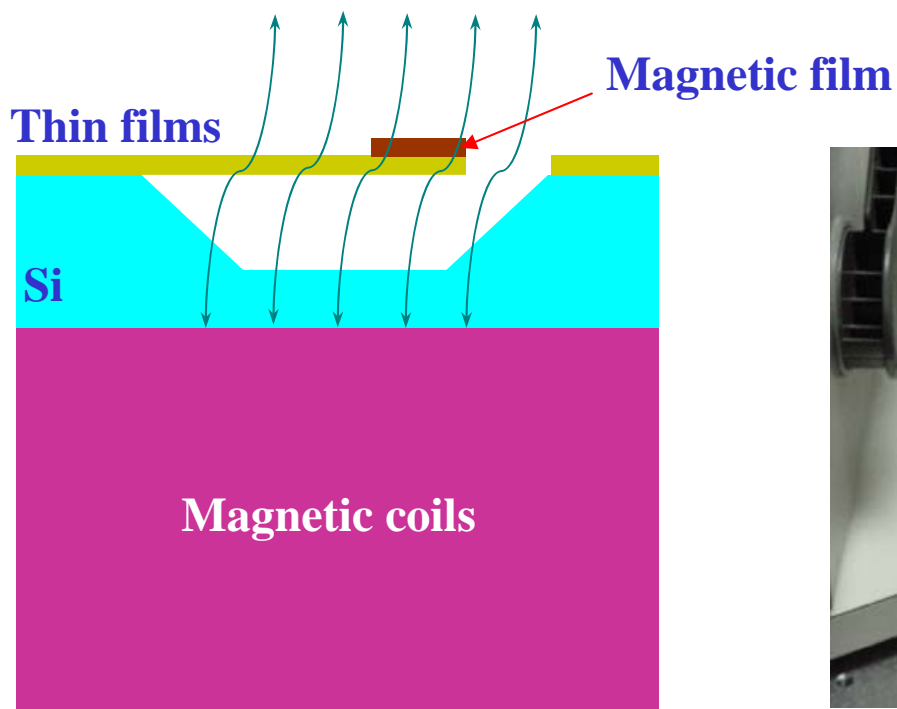




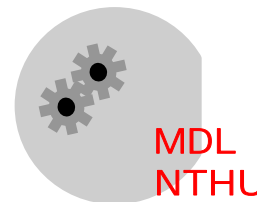


# Magnetic transducer

- An magnetic coil is used to generate magnetic force – harmonic excitation only

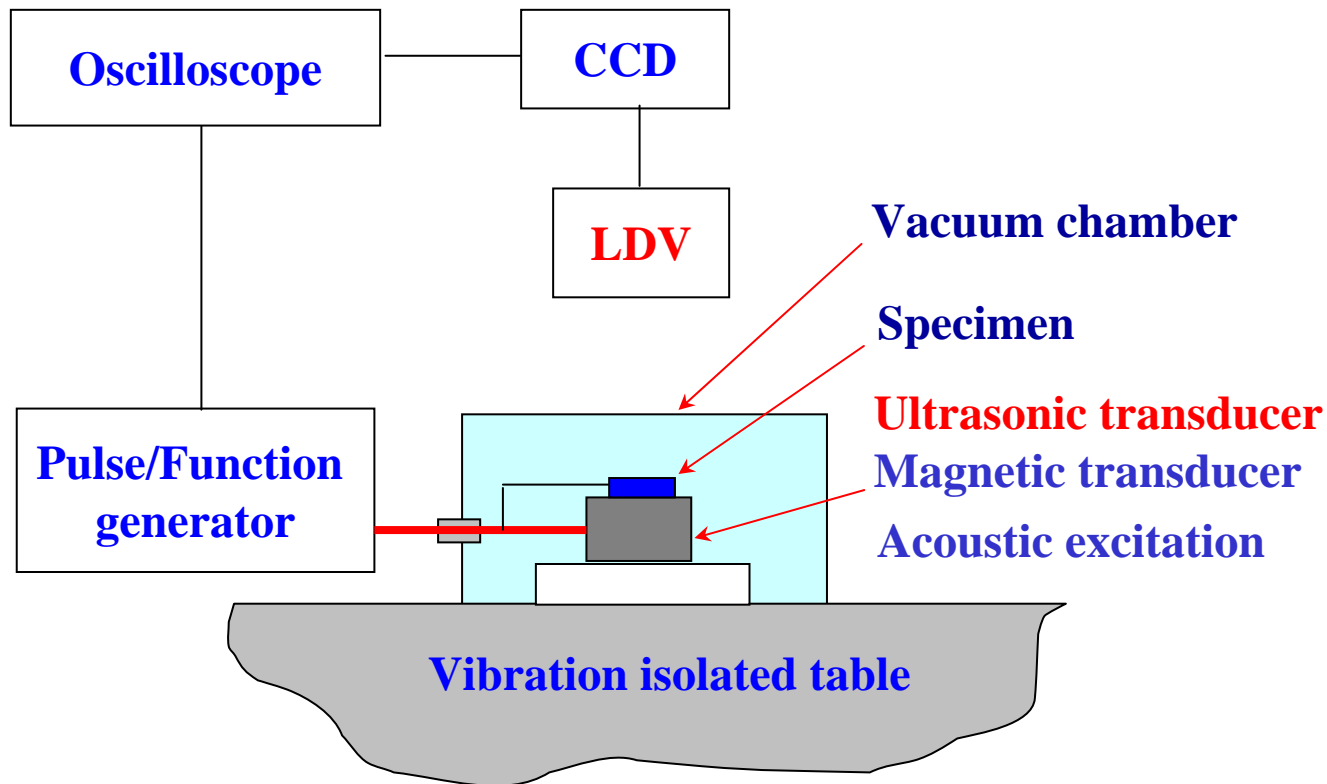


H.-C. Tsai and W. Fang, *AVS conference*, 2000

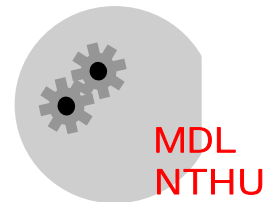




# Dynamic Testing Platform



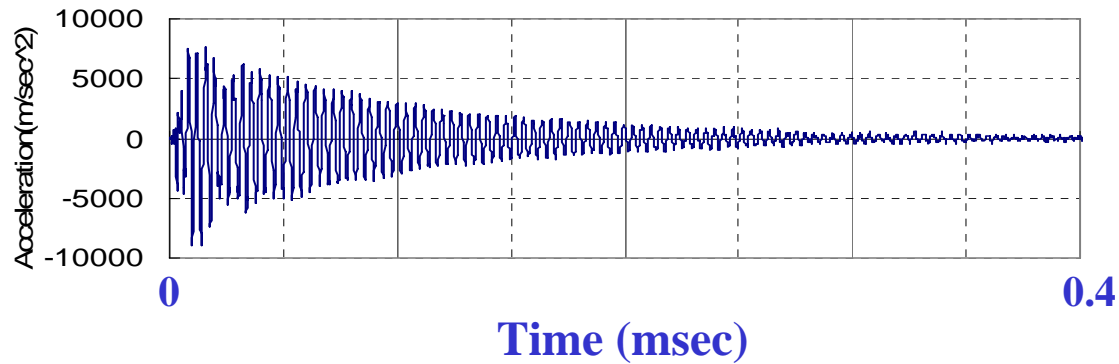
W. Lai and W. Fang, *Sensors and Actuators A*, 2001



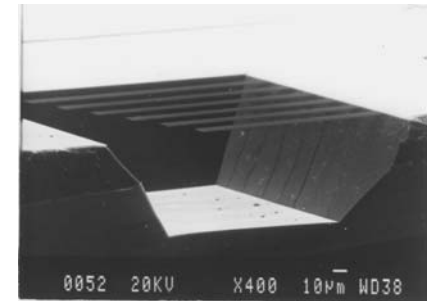
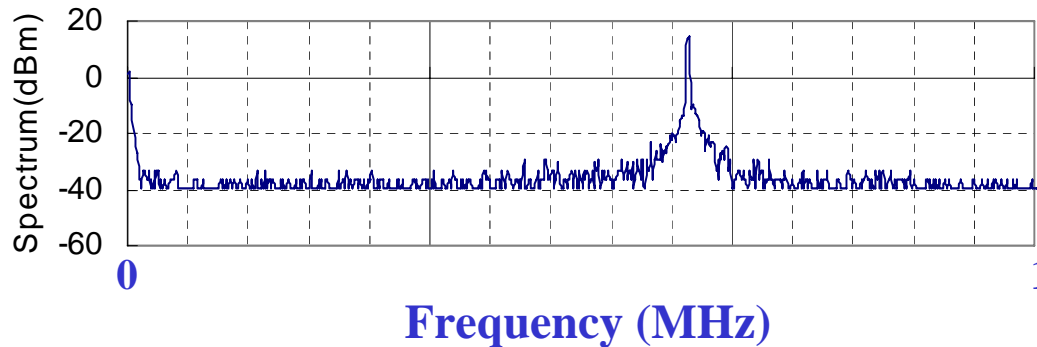


# Resonance frequency/ Damping coefficient

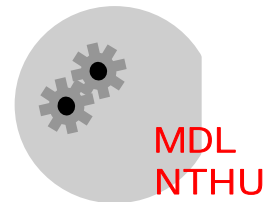
- Time domain



- Frequency domain

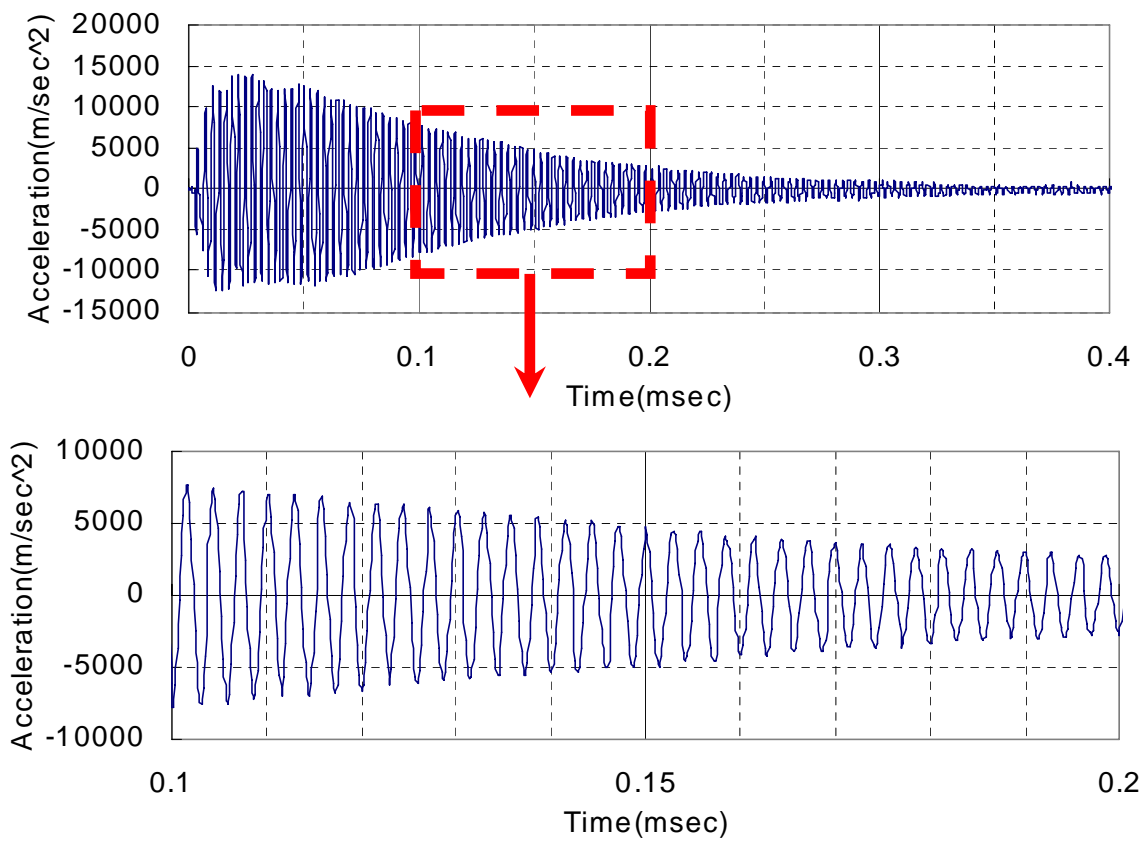


test cantilever





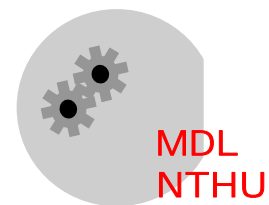
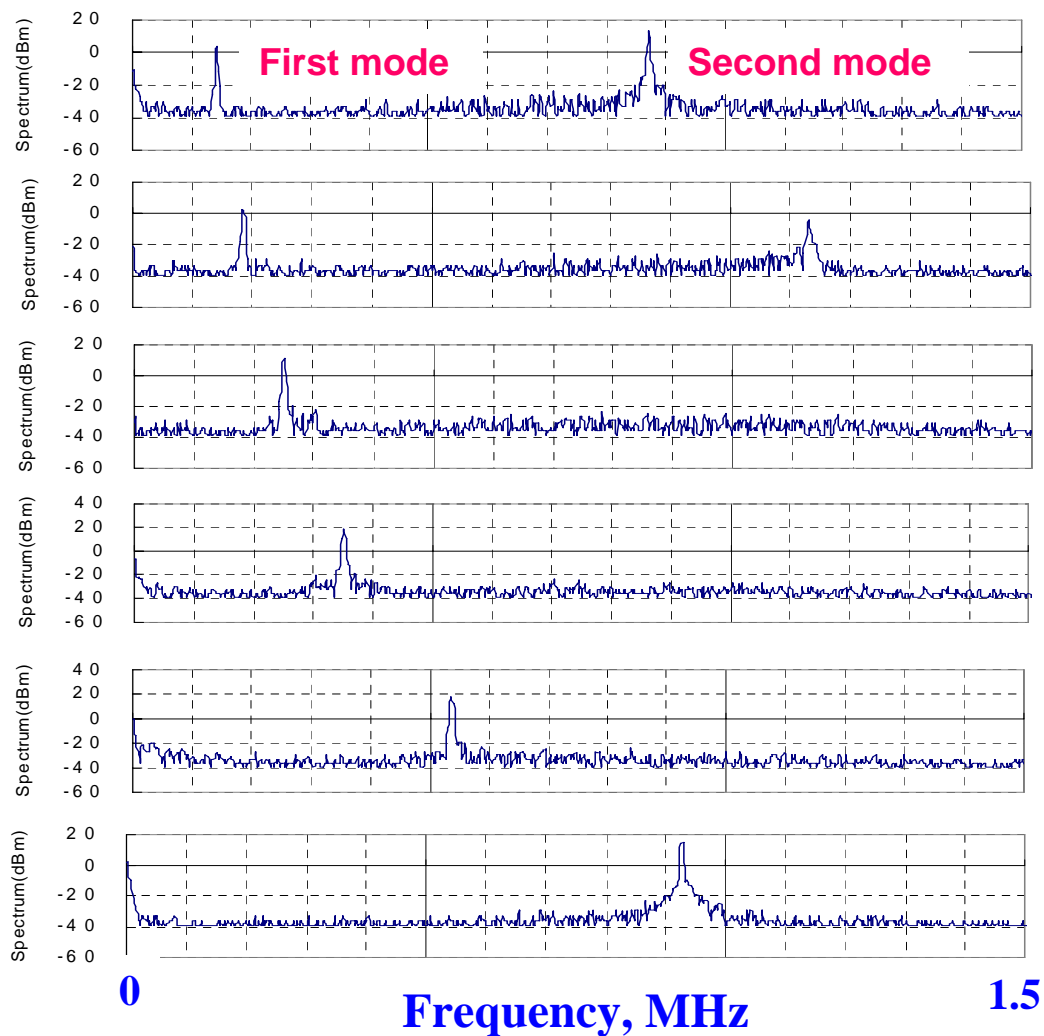
- Time domain response





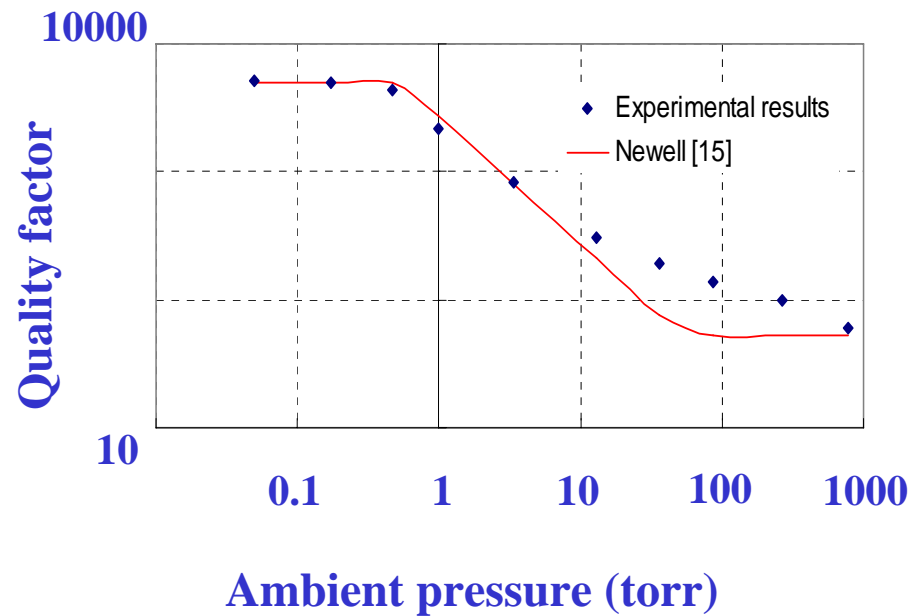
# Results

- Frequency domain response

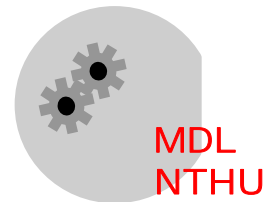




- Variation of the **quality factor** with the **ambient pressure**



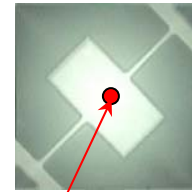
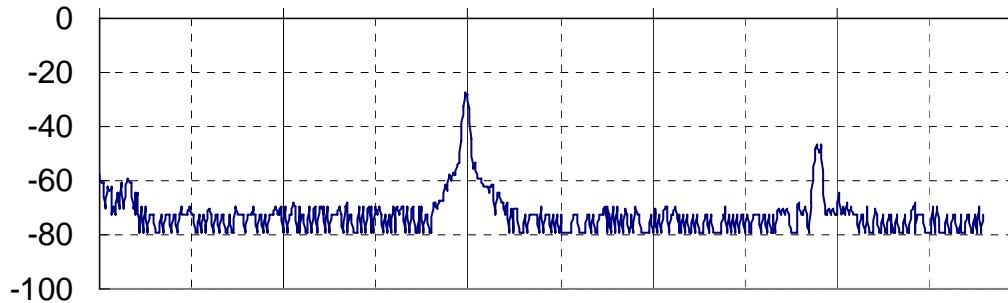
W. Lai, Y. Ho, and W. Fang, the *ASME IMECE*, New York NY, 2001



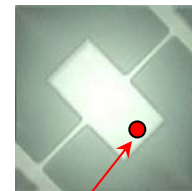
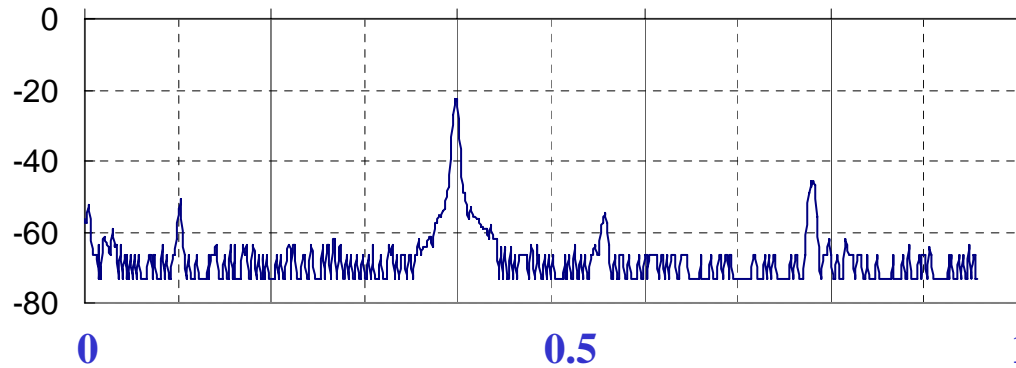


- **Dynamic behavior of complicated structure**

Power spectrum

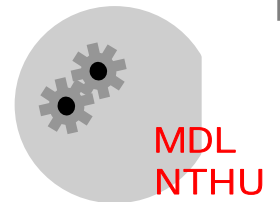


Laser spot



Laser spot

Frequency (MHz)





- **Static test**

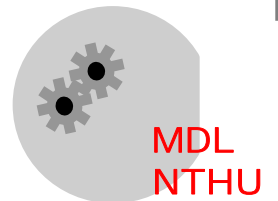
- + **Devices**

- + **Material properties**

- **Dynamic test**

- + **Devices**

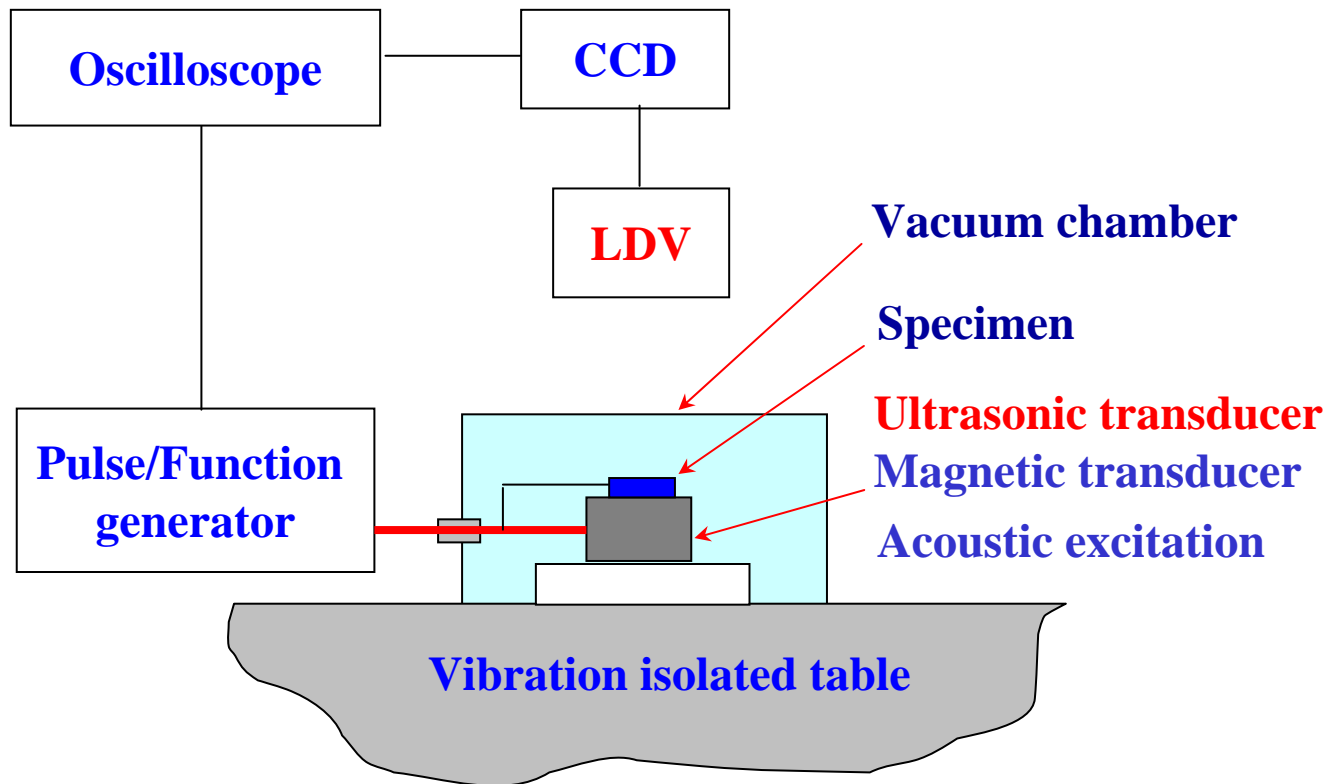
- + **Material properties – Young's modulus, Poisson's ratio**



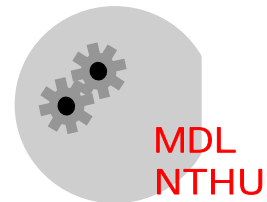




# Dynamic Testing Platform



W. Lai and W. Fang, *Sensors and Actuators A*, 2001





# Thin film material properties

- Young's modulus **E**, Shear modulus **G**, and Poisson's ratio  **$\nu$**

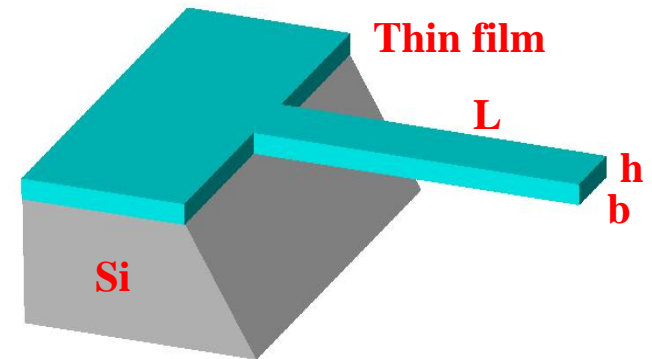
Bending mode

$$E = C_1(L, h, \rho) f_B^2$$

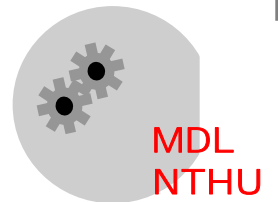
Geometry and material constants

$$G = C_2(L, h, b, \rho) f_T^2$$

Torsional mode

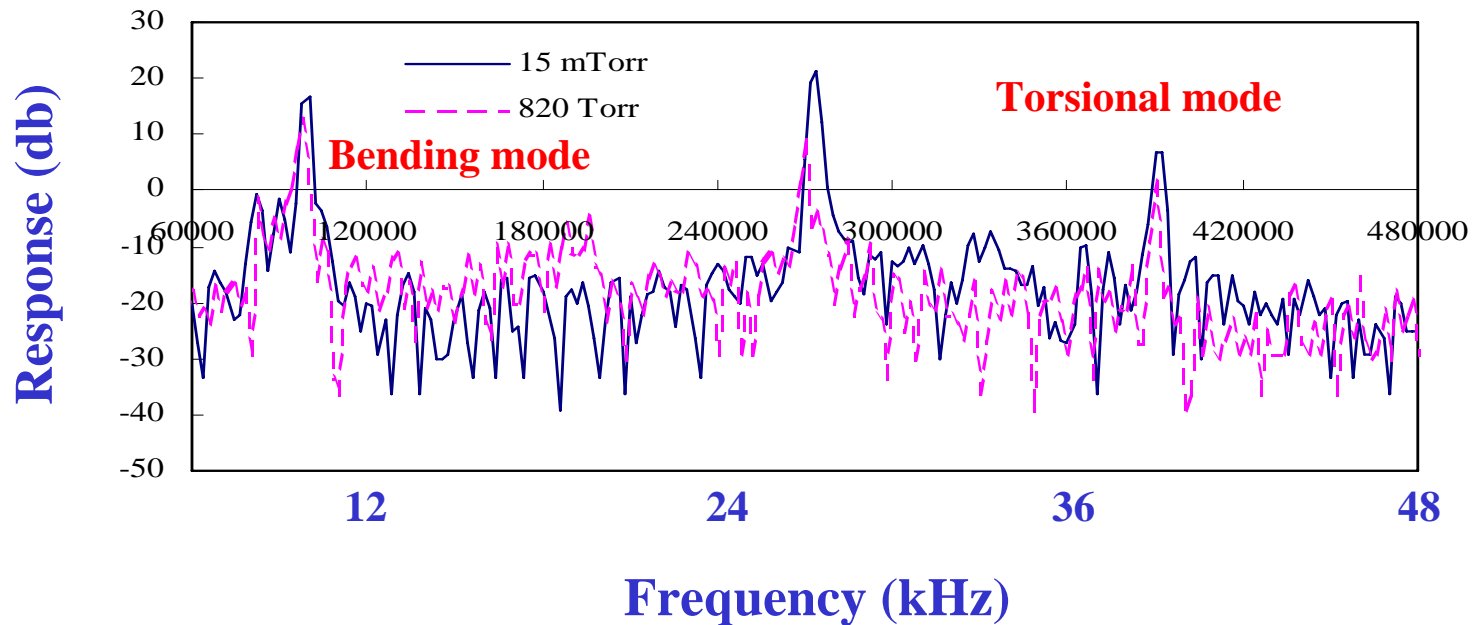


$$\nu = \frac{E}{2G} - 1$$

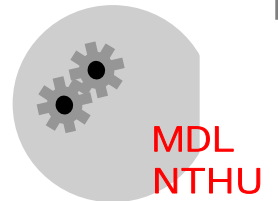




- Measured Young's modulus for SiO<sub>2</sub> film :  $E = 57 \text{ Gpa}$  (bulk : 70 Gpa)
- Measured Poisson's ratio for SiO<sub>2</sub> film :  $\nu = 0.202 \pm 0.021$  (bulk : 0.17)



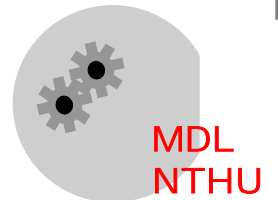
H.-C. Tsai, W. Lai, and W. Fang, the *ASME IMECE*, New York NY, 2001





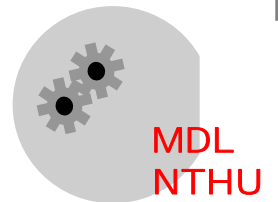
# Summary

- **Static test**
  - + **Devices**
  - + **Material properties**
  
- **Dynamic test**
  - + **Devices**
  - + **Material properties**





# Geometry and Boundary Considerations

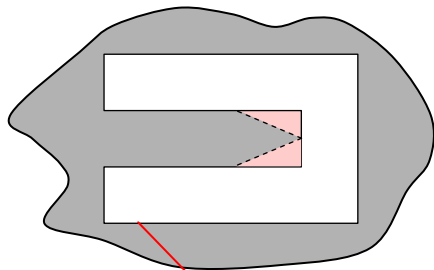




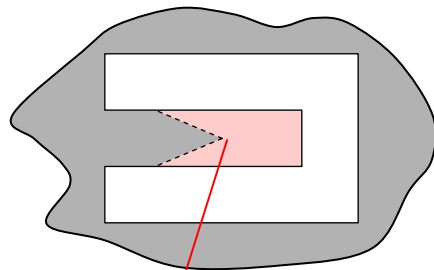
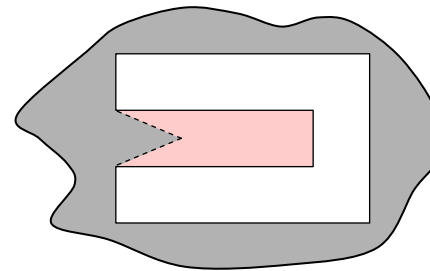
# Cross section of the test beams

H.-H. Hu and W. Fang, Sensors and Actuators A, 2001

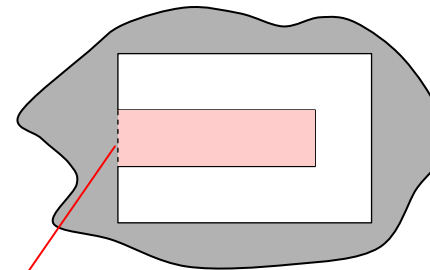
- For (100) Si substrate



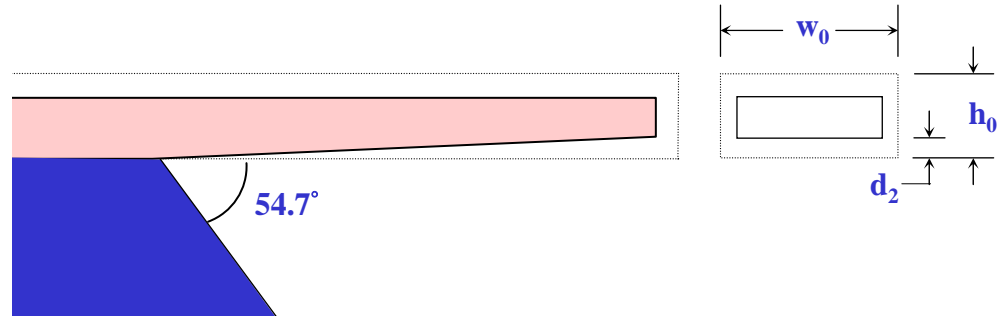
edge of the opening



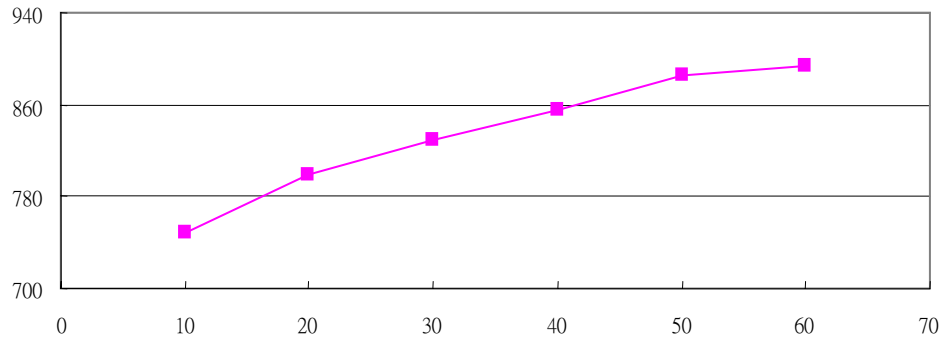
sharp corner



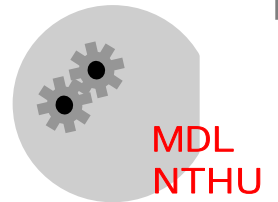
boundary of the cantilever



radius of curvature (  $\mu\text{m}$  )



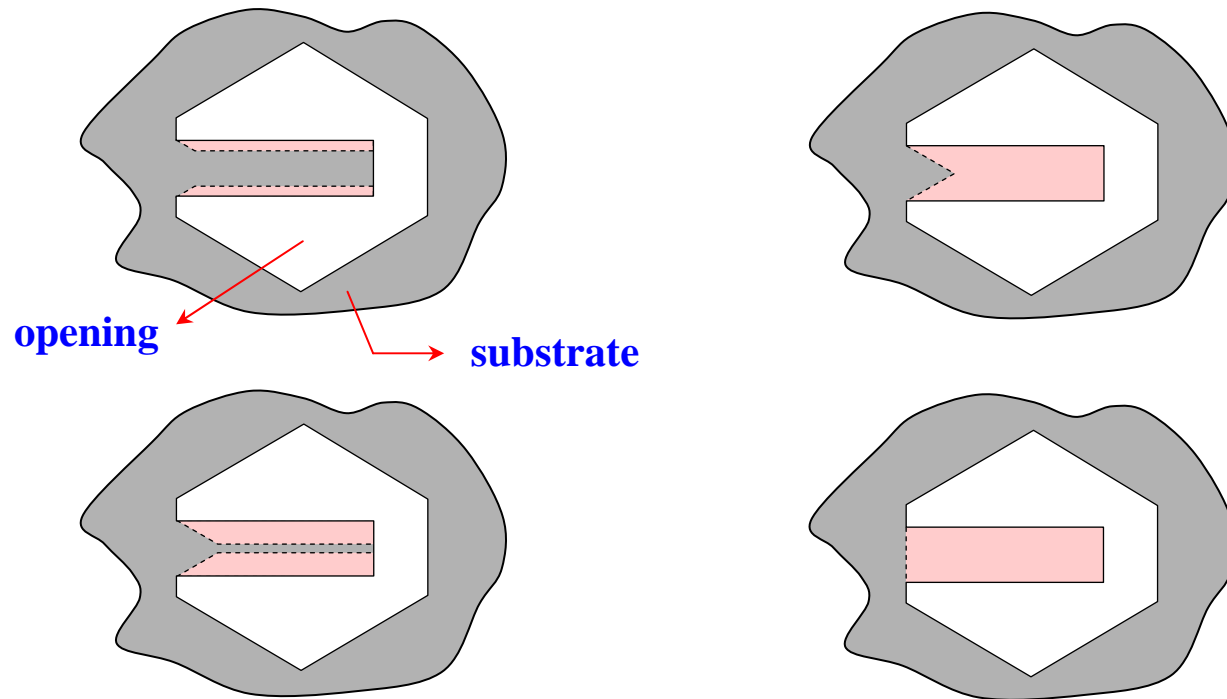
beam length ( $\mu\text{m}$ )



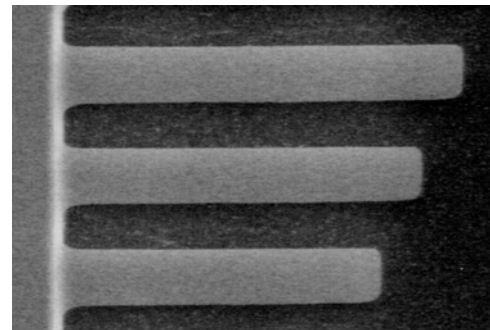
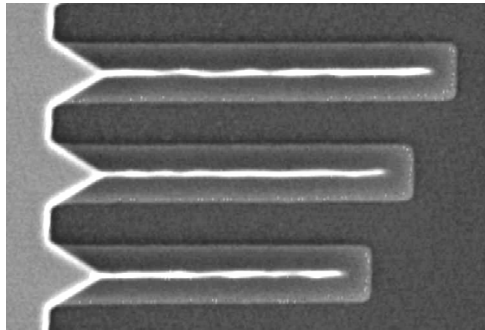
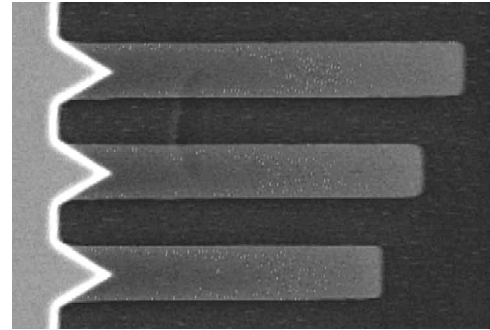
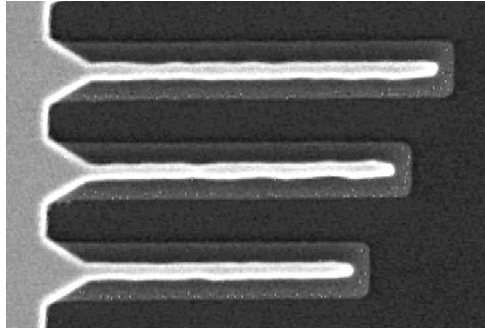
MDL  
NTHU

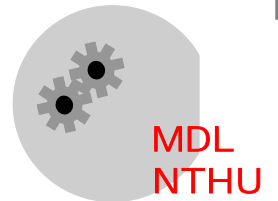
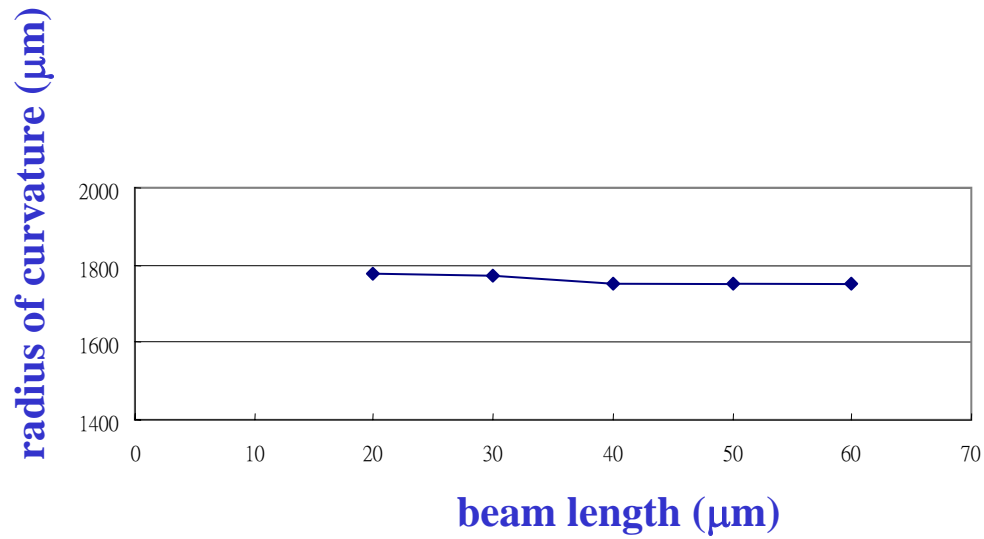
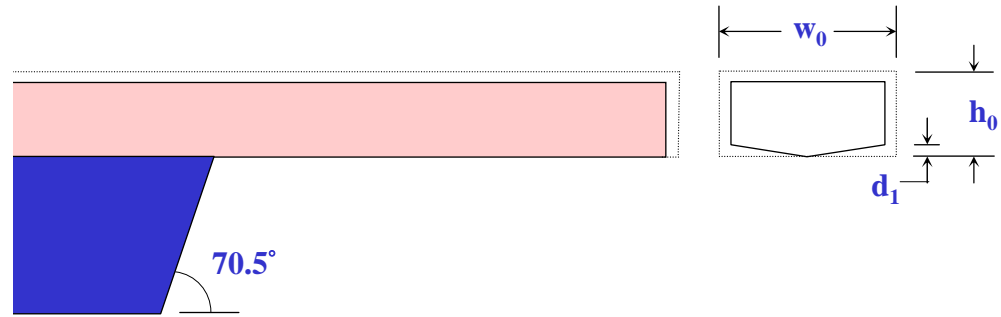


- For (111) Si substrate





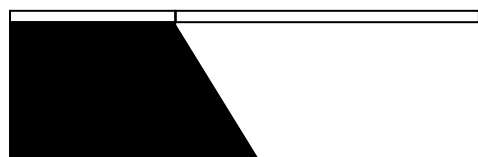




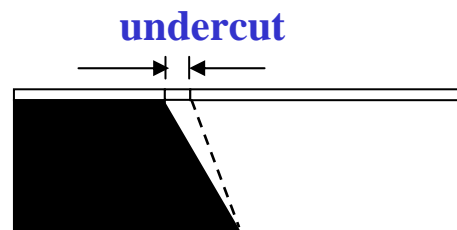


# Boundary Conditions - I

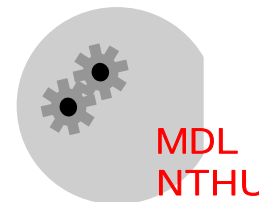
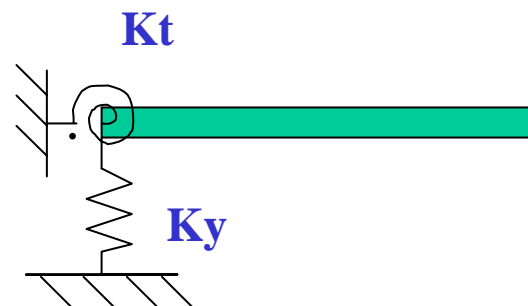
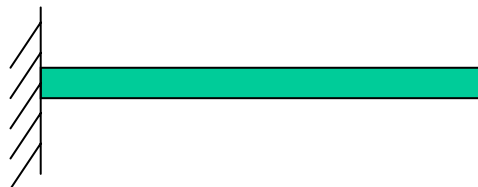
- Bulk process – half plane, undercut



Halfplane



Undercut

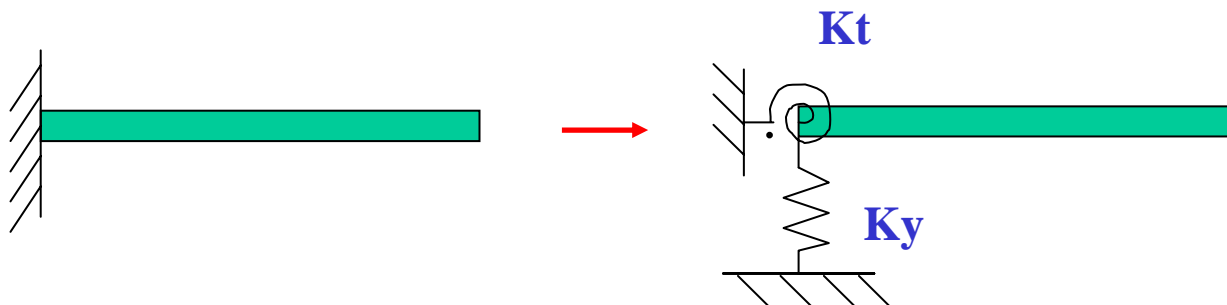




# Boundary Conditions - II

- Surface process – step

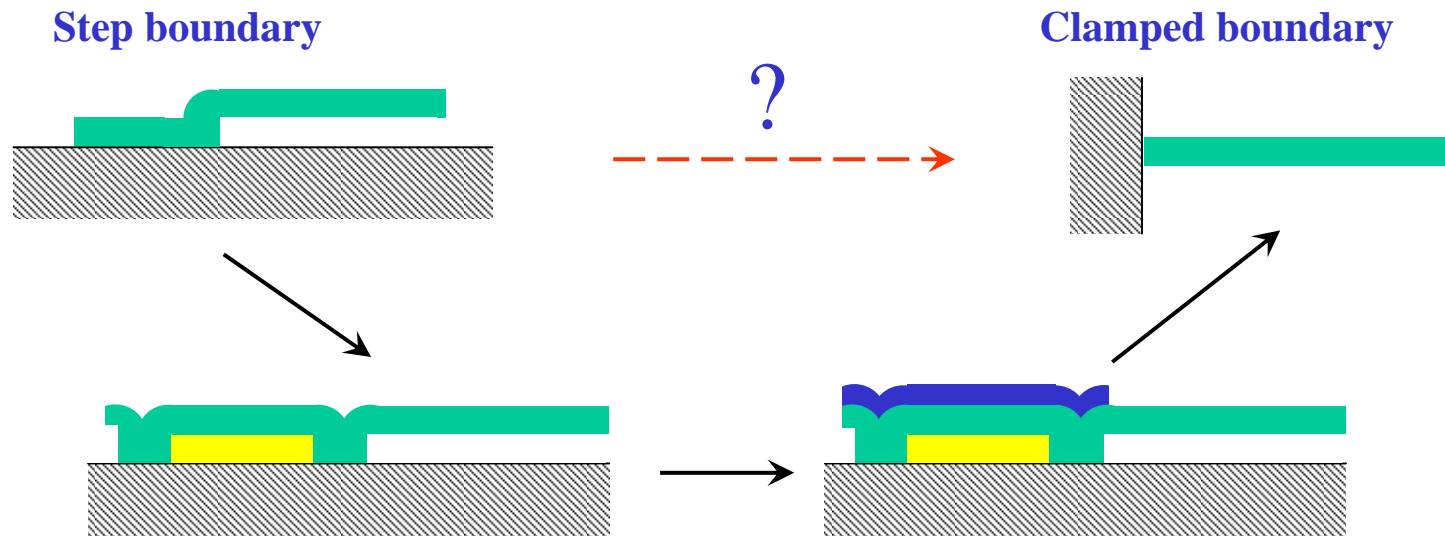
Step boundary





# Boundary Reinforcement

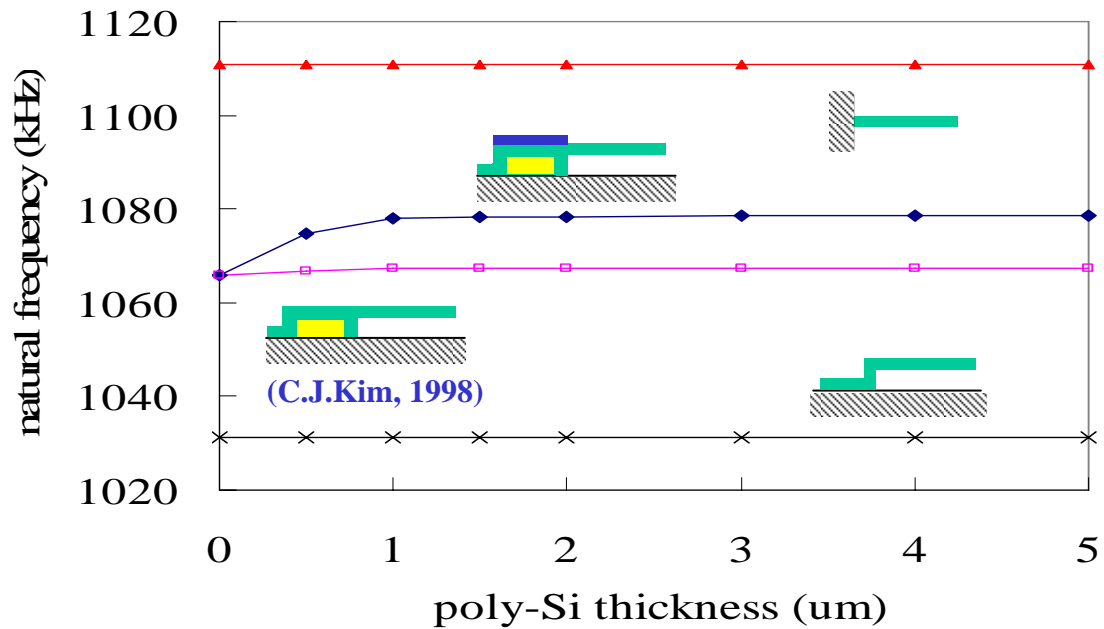
- For 2 poly surface processes



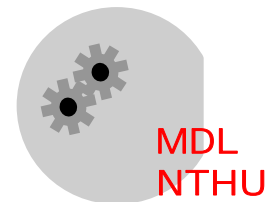
C.J.Kim, 1998



## • FEM simulation



	Ideal	Step	Plane	Stack
Natural frequency	1110690	103180	1065990	1078310
Error	0 %	7.25 %	4.02 %	2.91 %



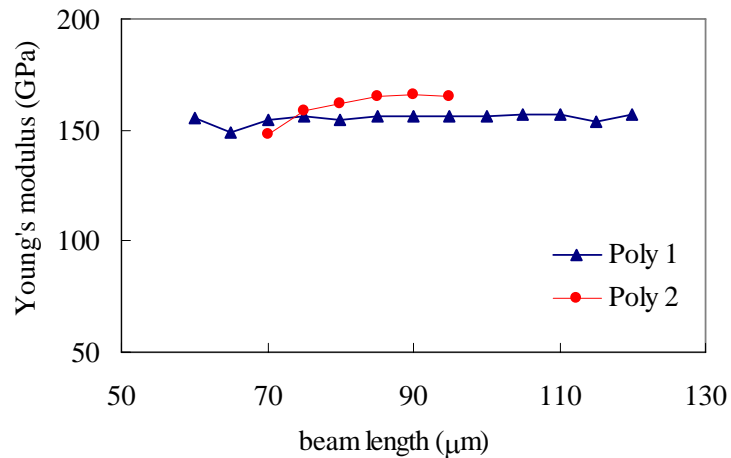


## • Measurement – elastic modulus of poly-Si

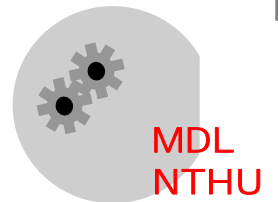
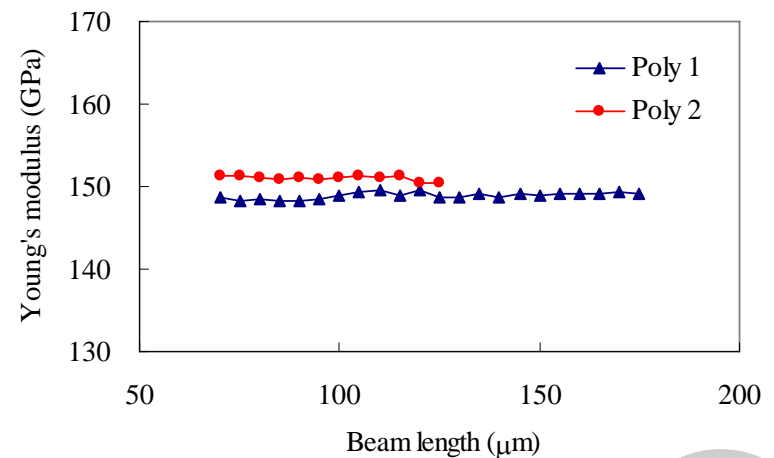
+  $E_{\text{Poly1}} = 148.9 \pm 0.7$  GPa, in MUMPs 55

+  $E_{\text{Poly2}} = 151.0 \pm 0.7$  GPa, in MUMPs 55

MUMPs 51

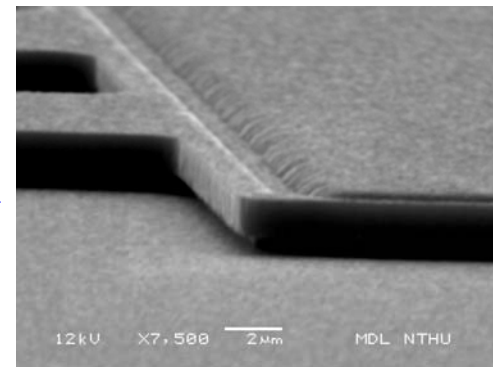
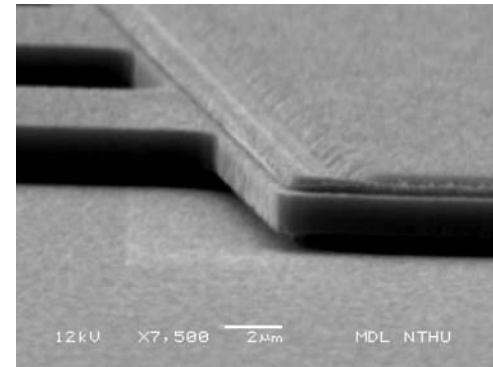
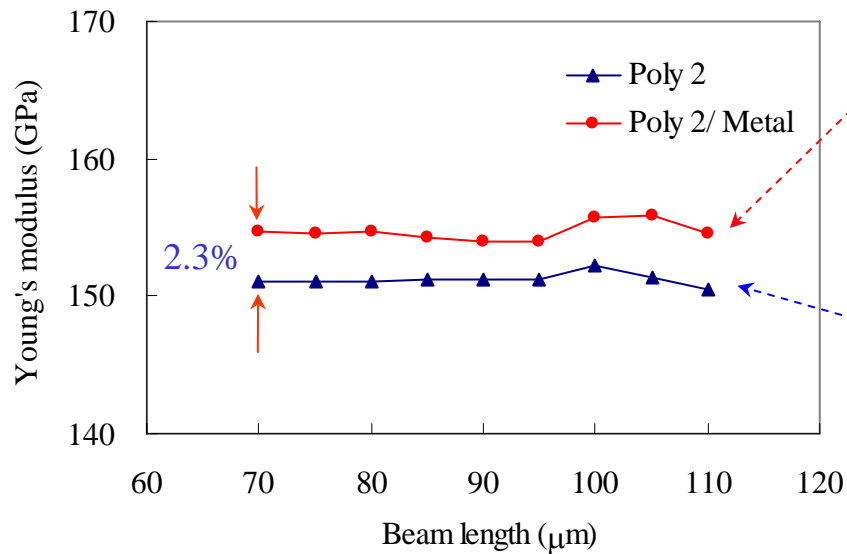


MUMPs 55





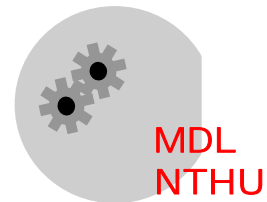
- **Comparison of the measured elastic modulus for different boundary condition**







# Elastic modulus of thin film



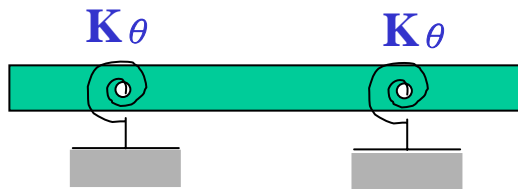


# Free-Free Beam

ideal

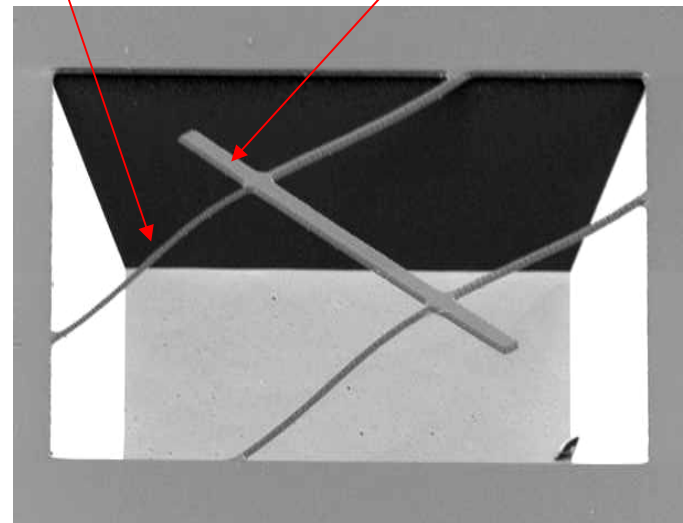


practical



suspension

Free-free beam

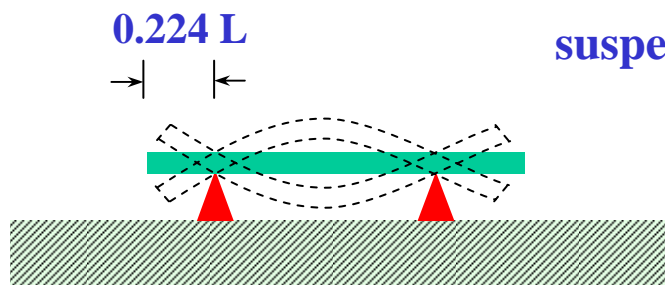




- **Micro “free-free” beam**

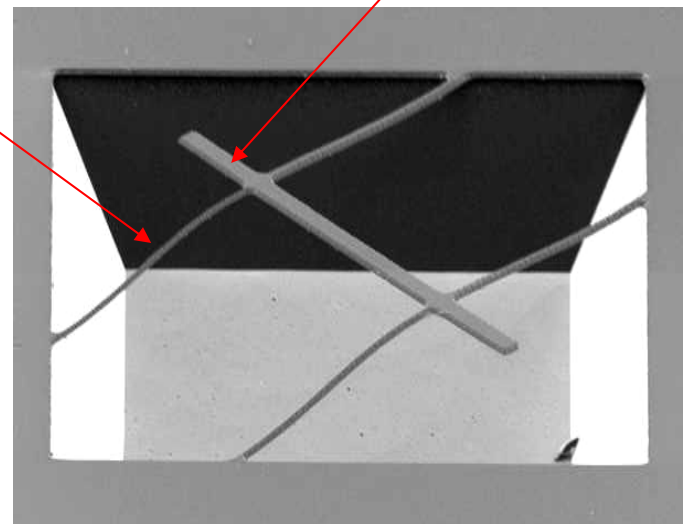
- + **The location of suspension**

- + **Torsional Stiffness vs resonant frequency & mode**

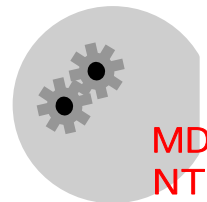


suspension

$$E = 0.9465 \frac{\rho A L^4 f_F^2}{b h^3} T_1$$

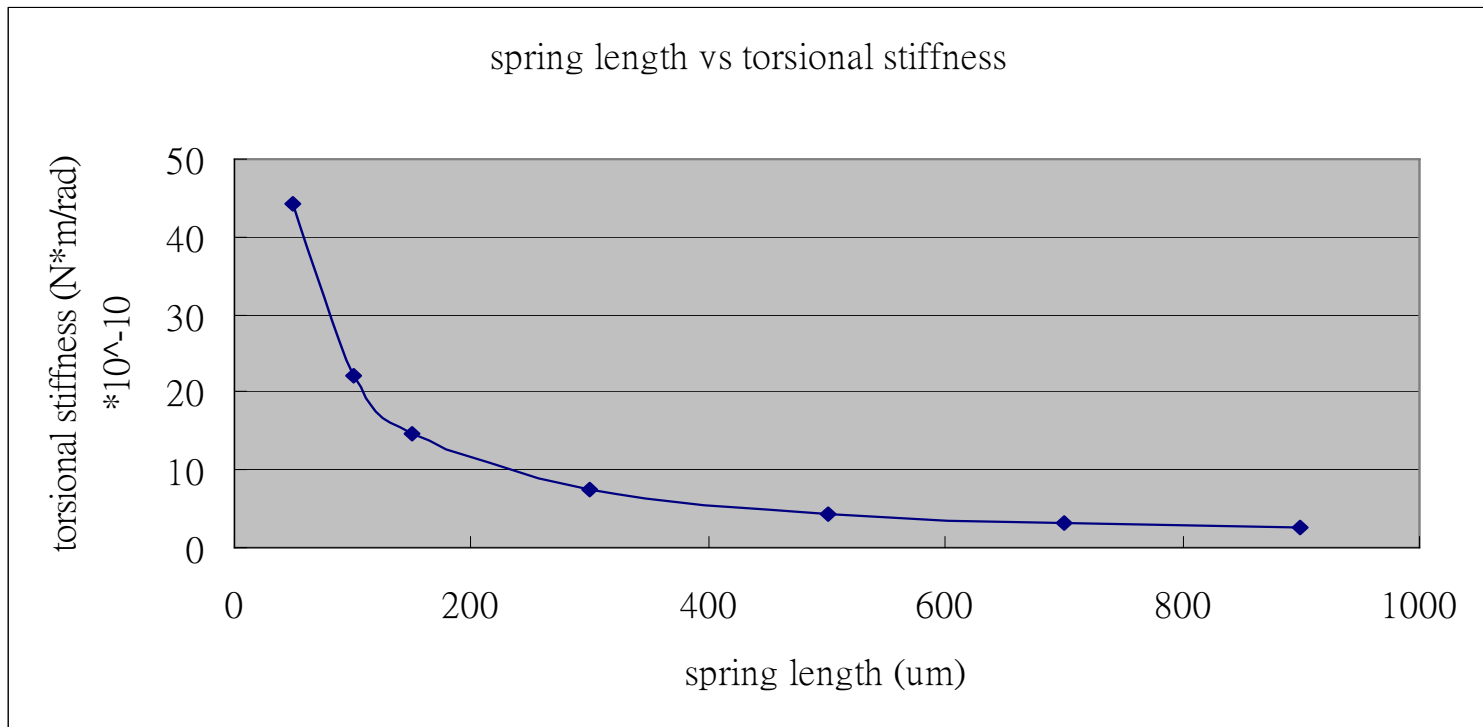


Free-free beam



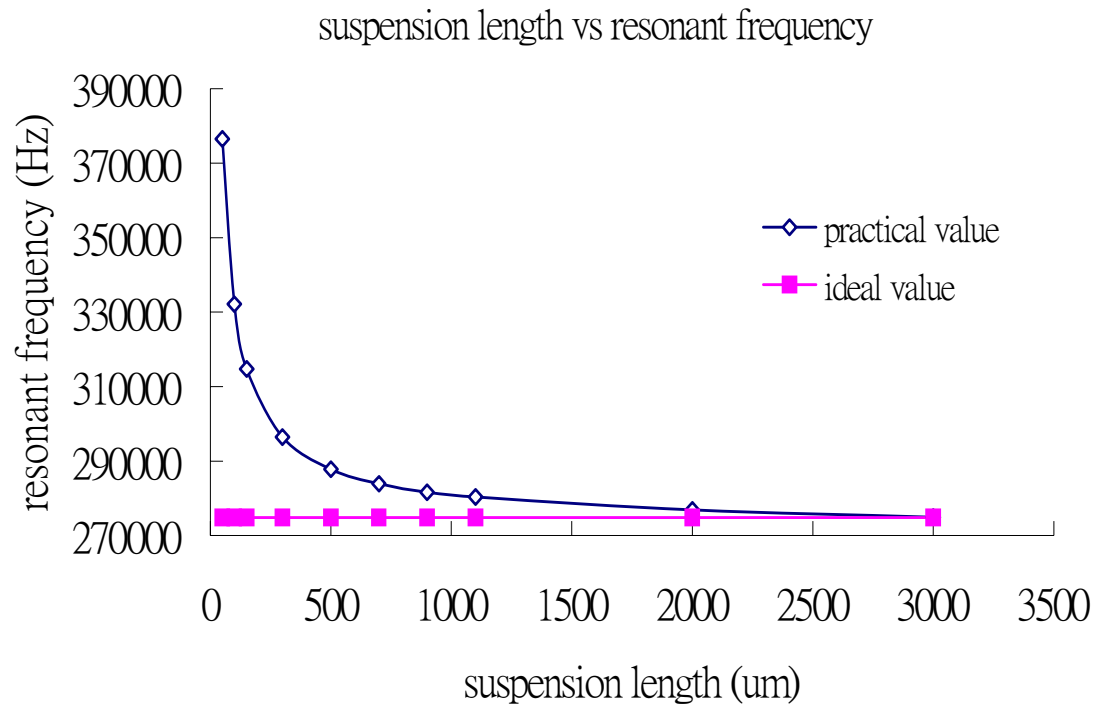


- **Torsional stiffness vs suspension length**

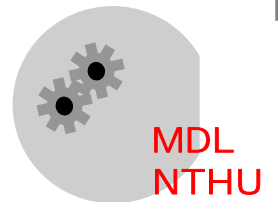




- **Simulation of the natural frequency vs suspension length**



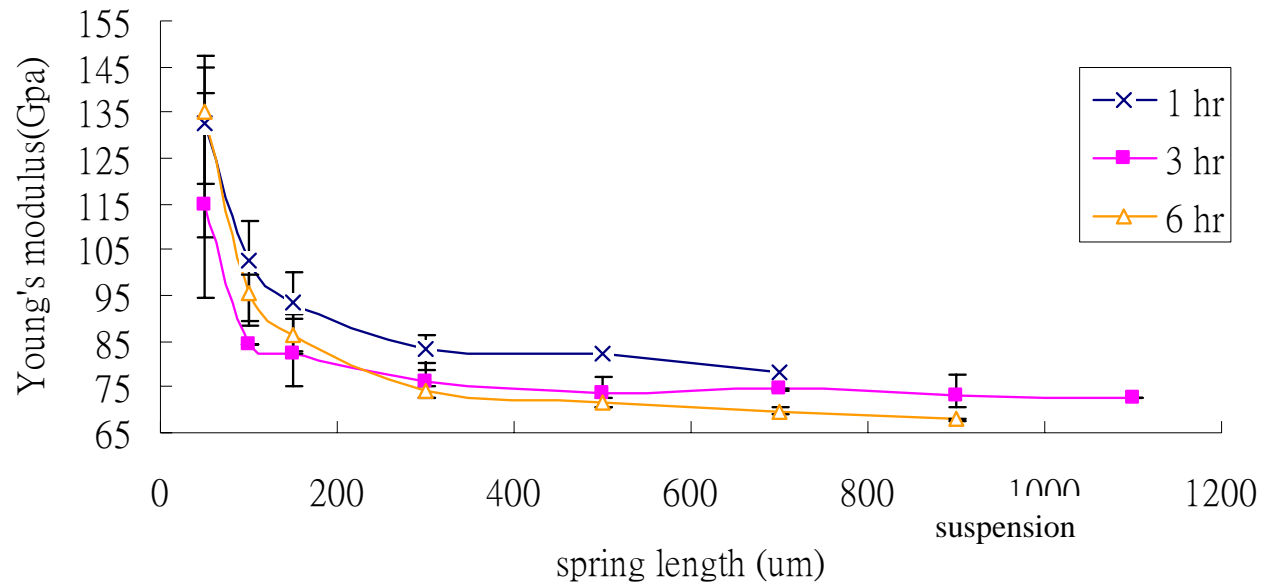
**4.7 % error when torsional spring length is 500  $\mu\text{m}$**



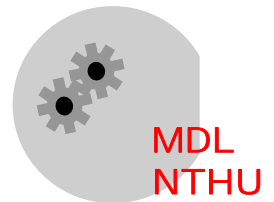


- Measurement of 0.84  $\mu\text{m}$  thermal oxide – Young's modulus

### Free-free beam

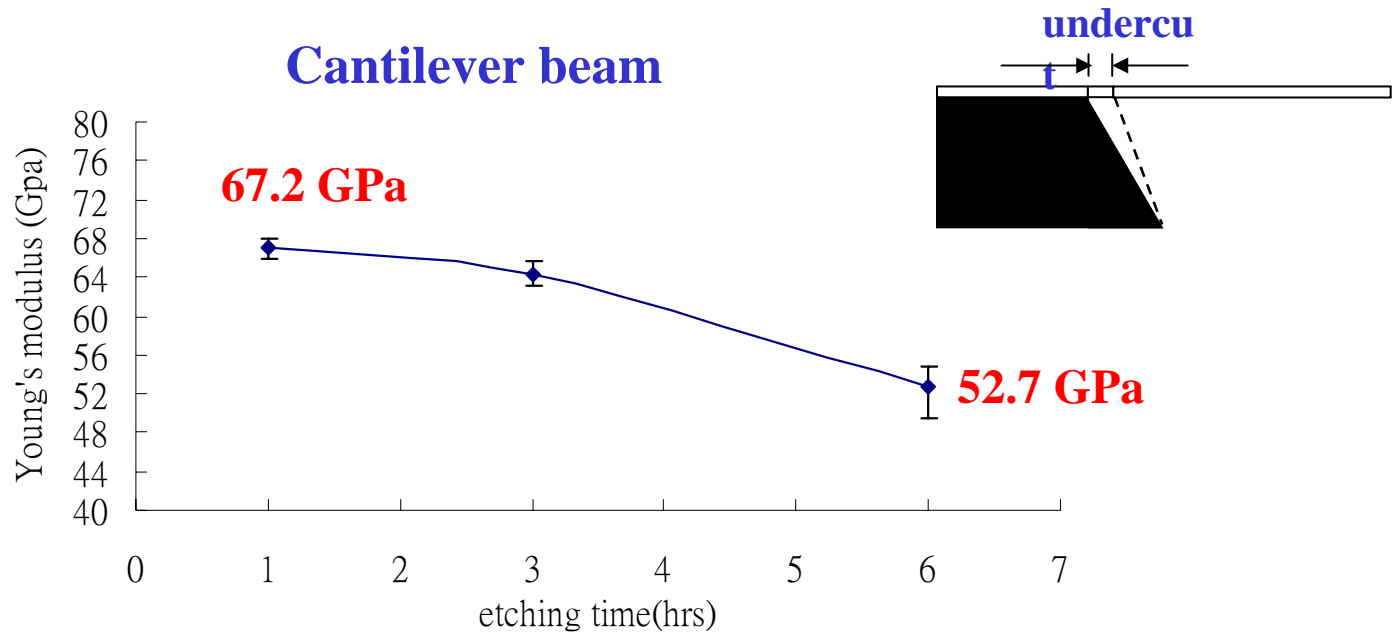


**E = 67.9 GPa** (for 900  $\mu\text{m}$  suspension with 6 hrs etching time)

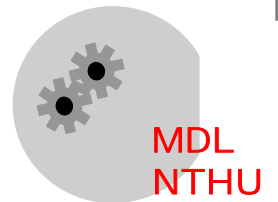




- Measurement of  $0.84\ \mu\text{m}$  thermal oxide – Young's modulus

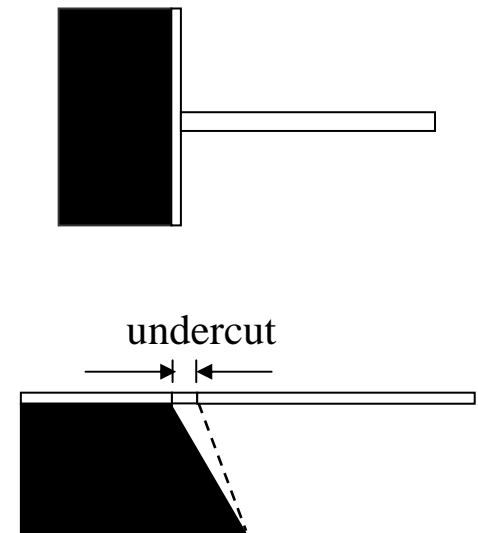
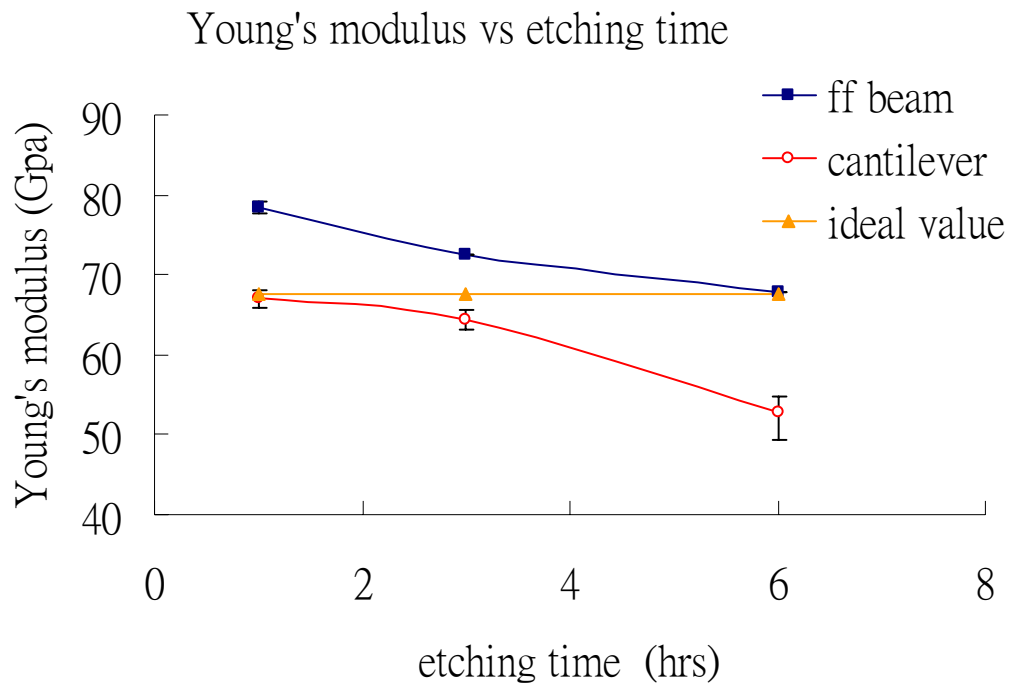


After 6 hours etching, cantilever has 21.5% deviation from ideal





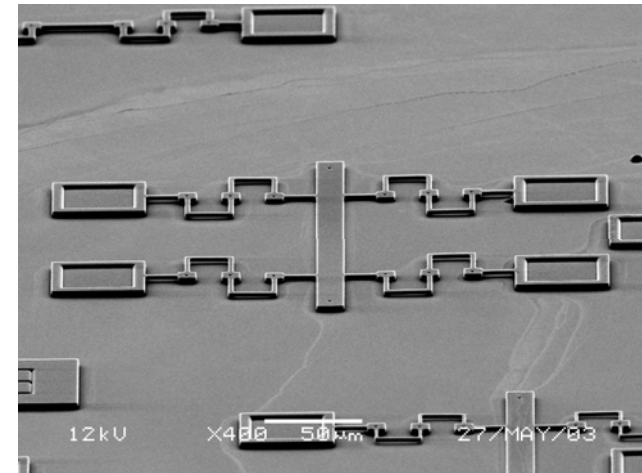
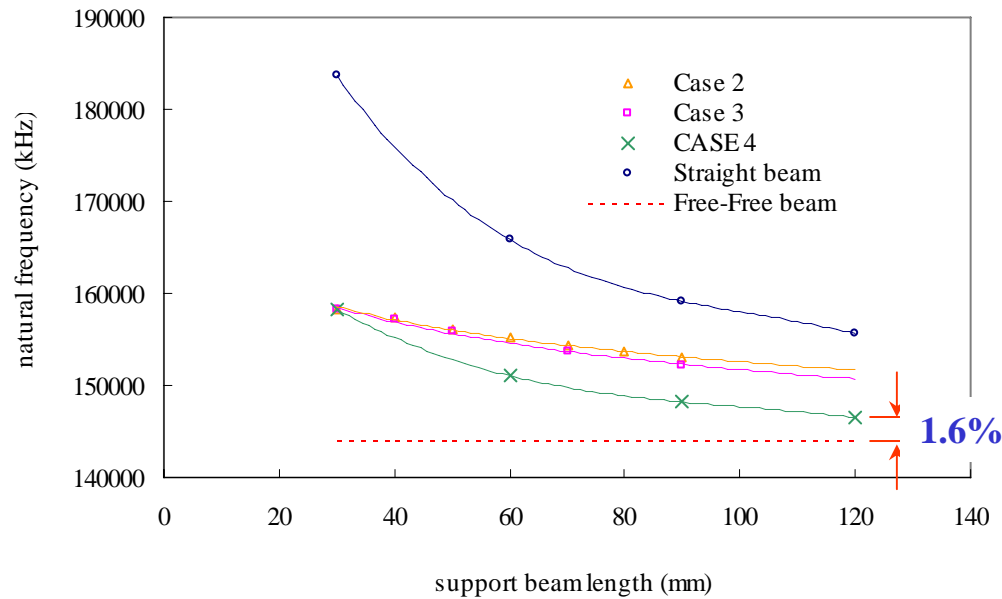
- For shorter etching time - Cantilever is a better test key
- For longer etching time - Free-free beam is a better test key





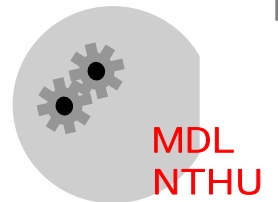


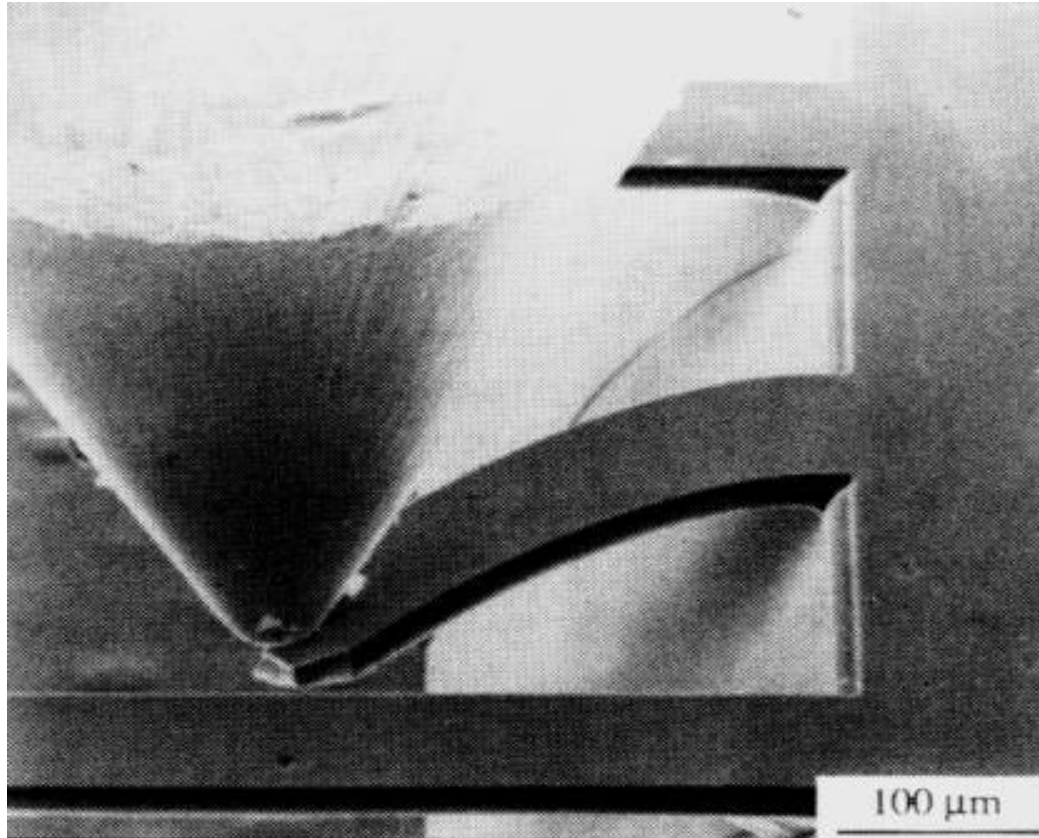
- For surface micromachined beam, the free-free beam can prevent the boundary imperfection due to step





# Improvement of Indentation Test

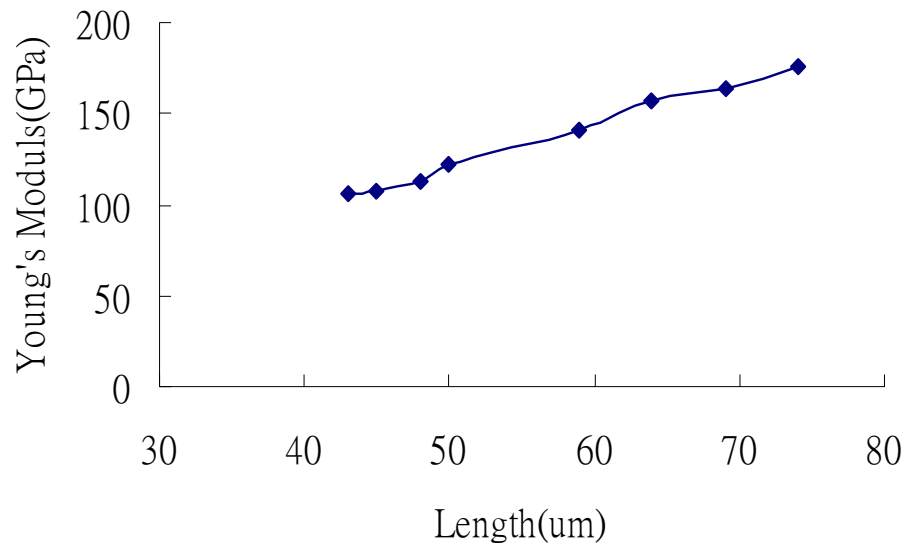




**J.-A. Schweitz, 1992**



- Variation of the Young's modulus with beam length**

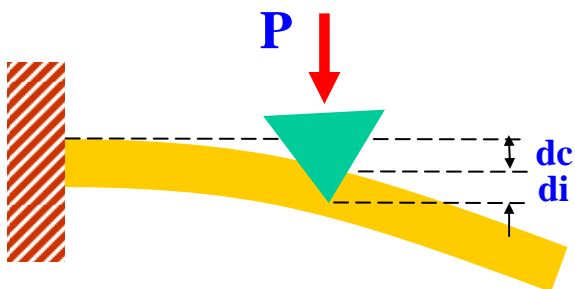
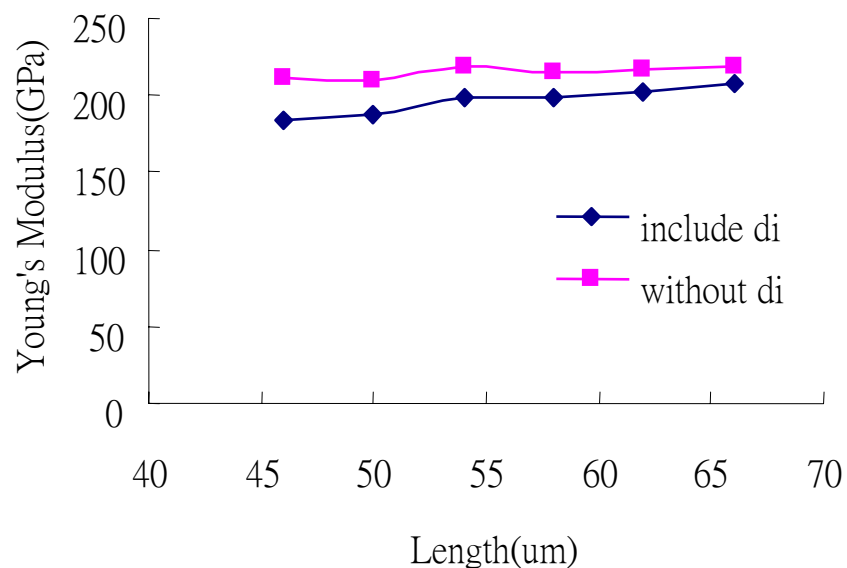


Length	E(loading)
74	175.18
69	163.70
64	156.44
59	140.33
50	121.90
48	113.32
45	107.58
43	105.88



## • The indentation effect – Nickel film

length	E1(include di)	E2(remove di)
66	207.14	218.40
62	203.05	216.24
58	199.36	215.09
54	198.75	218.49
50	187.55	210.11
46	182.93	211.36



$$K = \frac{P}{dc+di}$$



## • The boundary effect – Nickel film

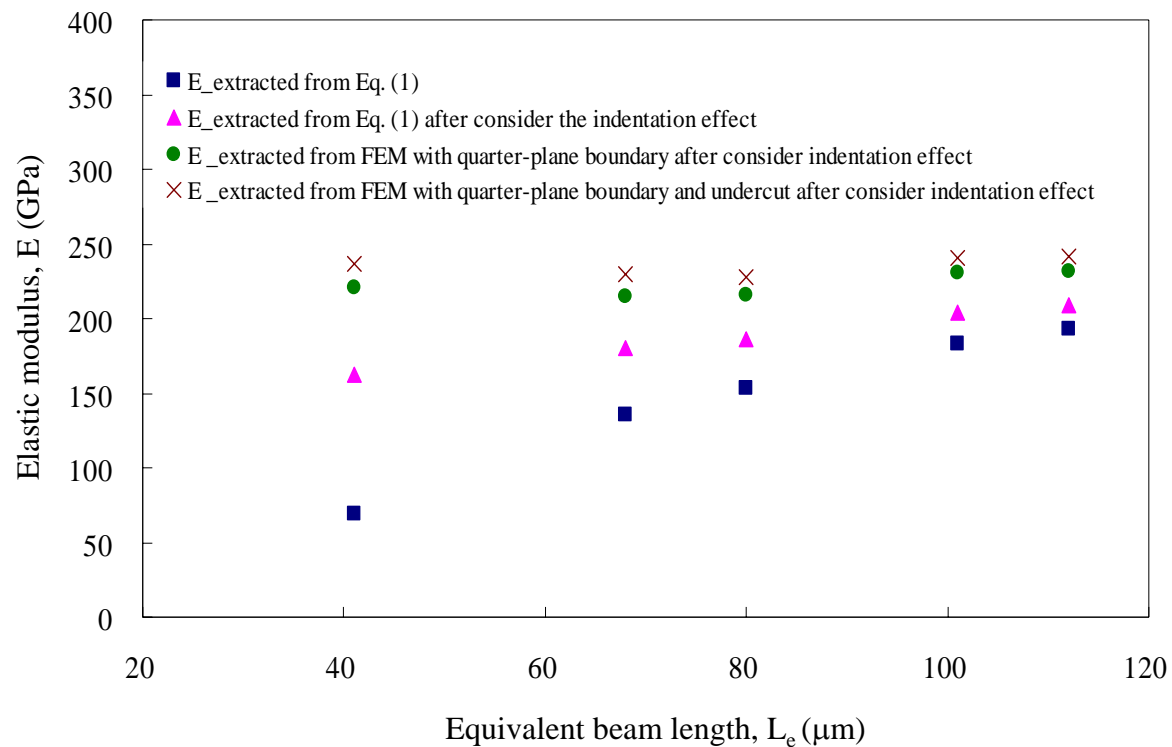
+ Conventional BC



+ MEMS BC

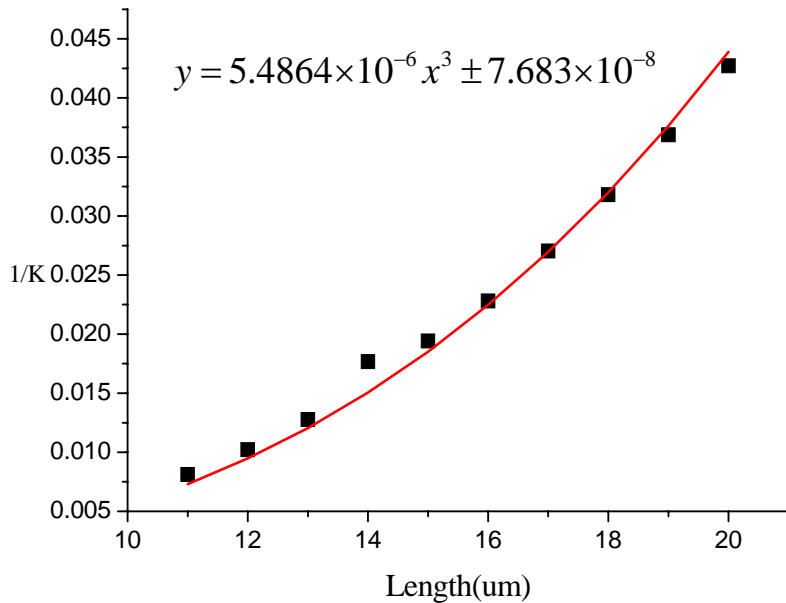
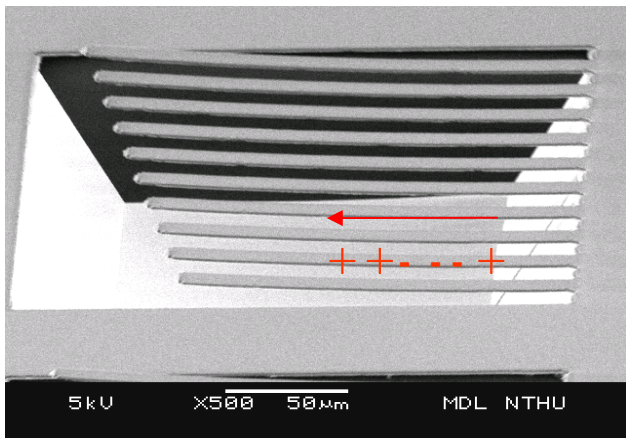
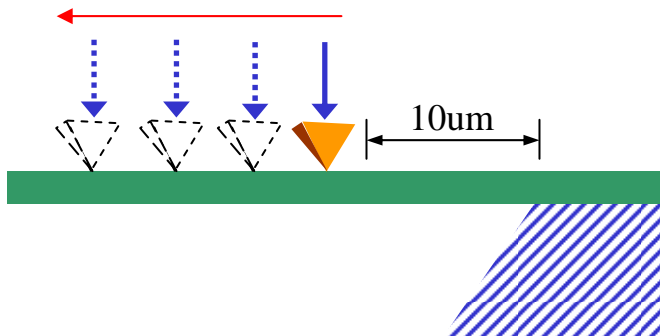


+ BC undercut

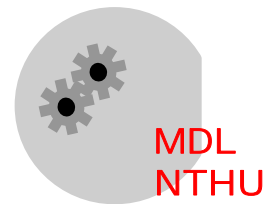




# The elastic modulus of SiO<sub>2</sub> film

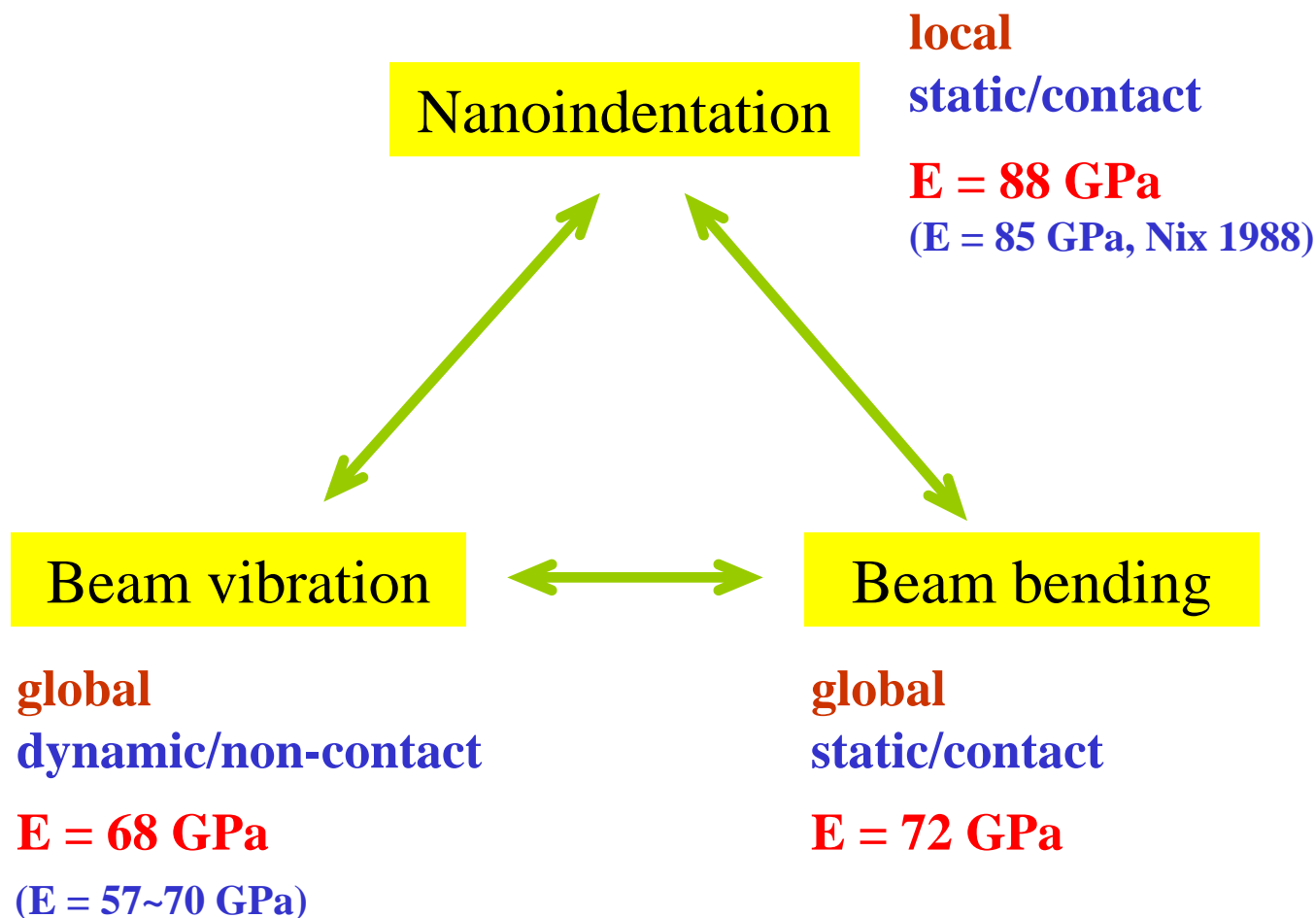


+ E : 71.5 GPa (67.3 ~ 75.9 GPa)





- Elastic modulus of  $\text{SiO}_2$  film from different approaches



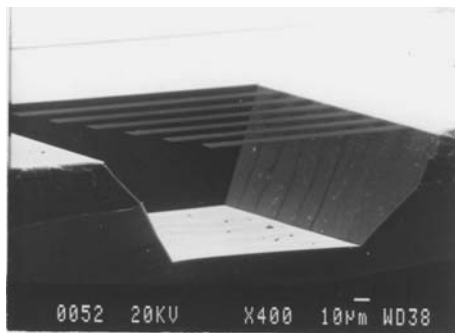




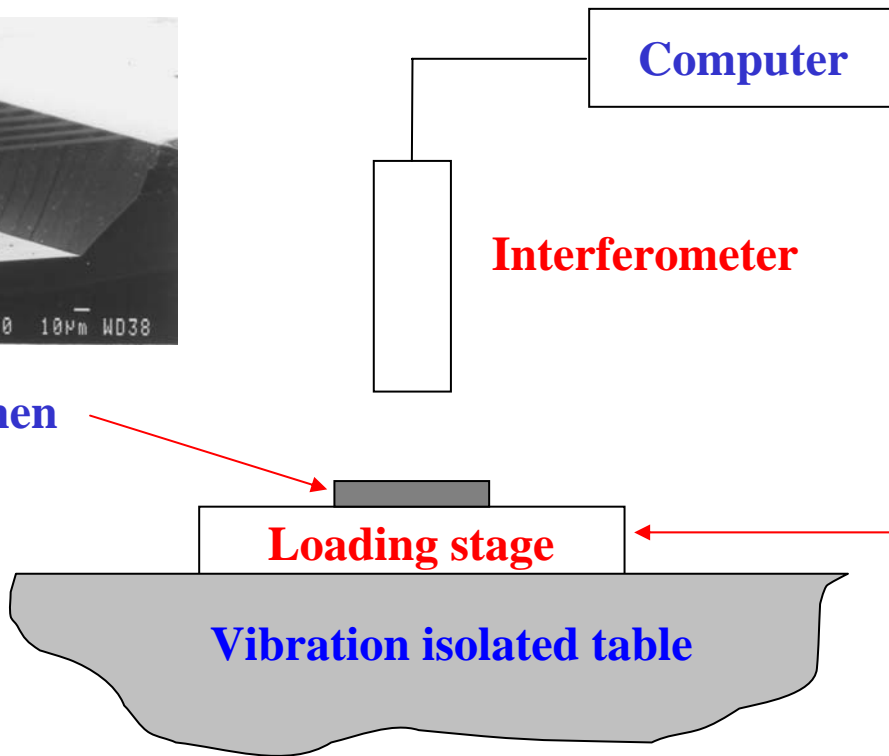
# Residual stresses of thin film



# Static Testing Platform



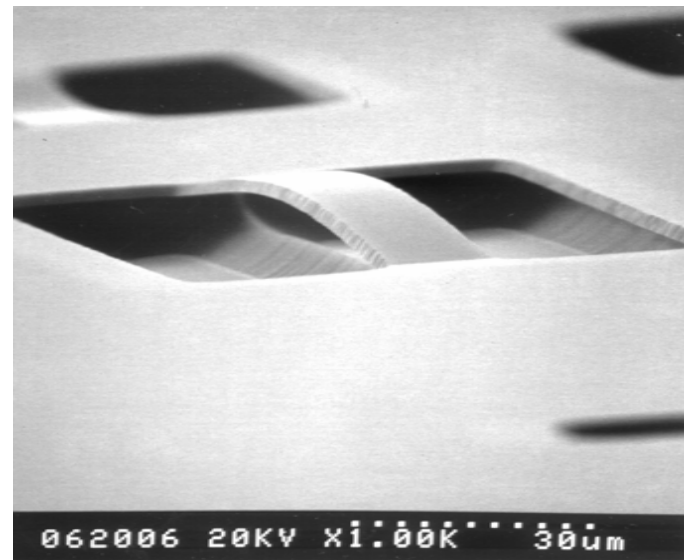
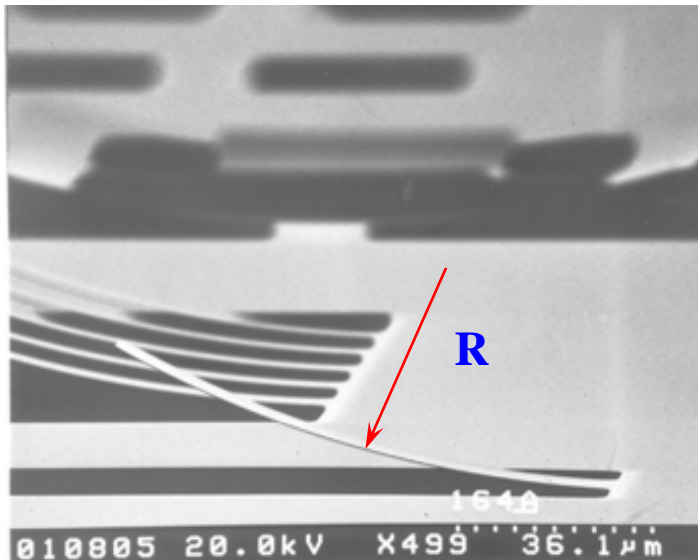
**Specimen**



- Residual stresses**
- Heating stage**
- Electromagnetic stage**
- Pressure source**
- Indenter**



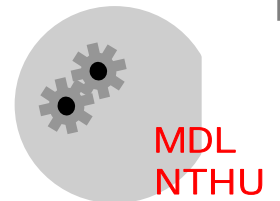
# Residual stress



W. Fang, and J.A. Wickert, *J. of Micromechanics and Microeng.*, 1994

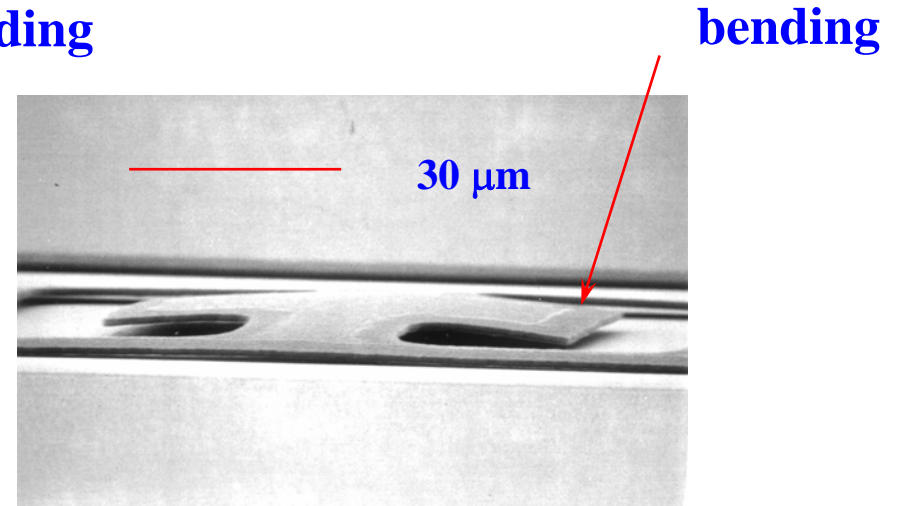
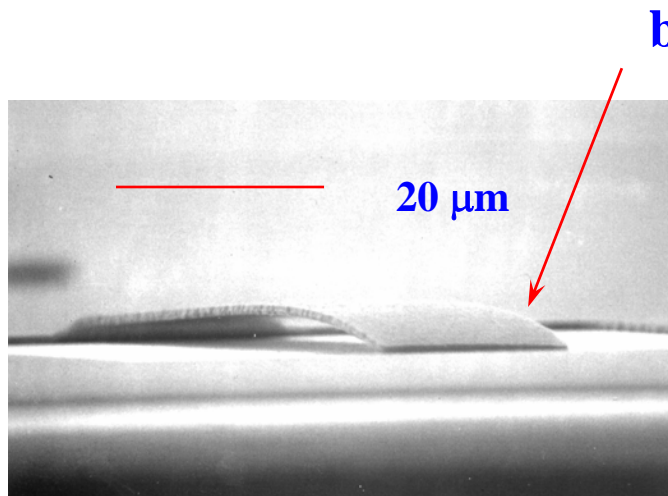
W. Fang, and J.A. Wickert, *J. of Micromechanics and Microeng.*, 1995

W. Fang, and J.A. Wickert, *J. of Micromechanics and Microeng.*, 1996

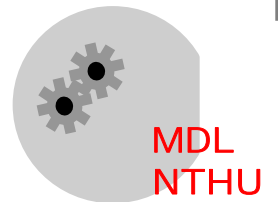




- **Surface micromachined Ti cantilever beam and gimbal suspension**  
+ **The Ti film is deposited by sputtering**



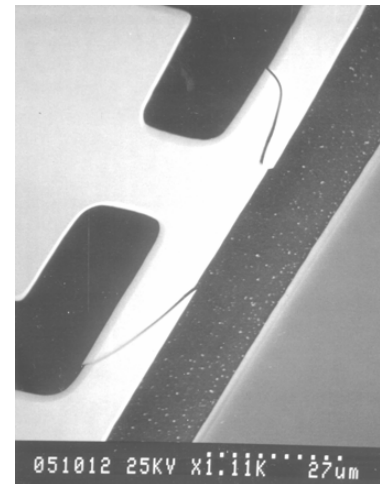
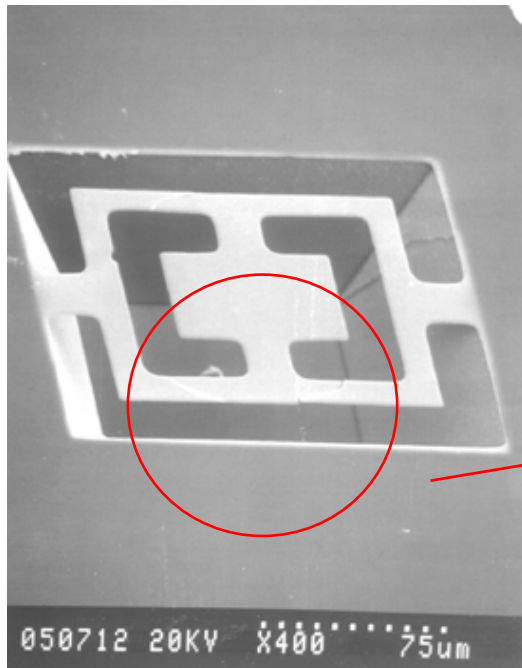
W. Fang and J.A. Wickert, J. of  
Micromech. and Microeng., 1996





- Crack of a bulk micromachined  $\text{SiO}_2$  suspension

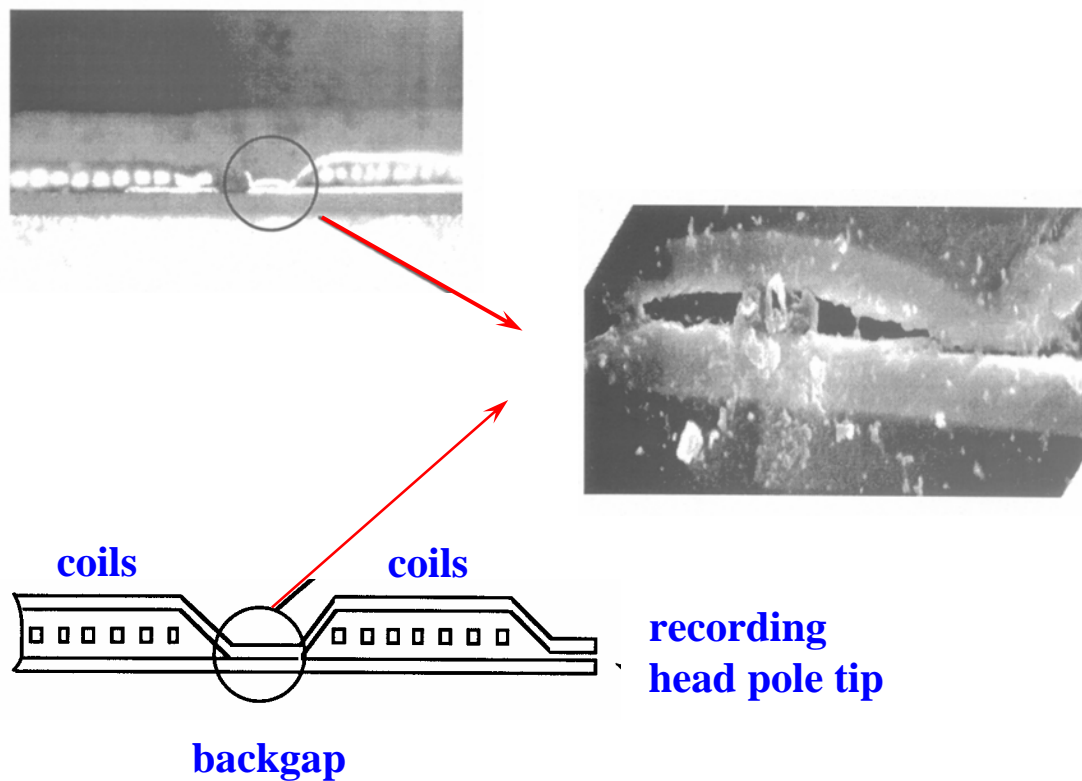
+ The  $\text{SiO}_2$  film is grown thermally



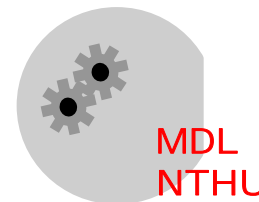
W. Fang, DSSC annual report,  
Carnegie Mellon University, 1993



- Buckling of the **sputtered FeAlN layer** in a thin film recording head by residual stress



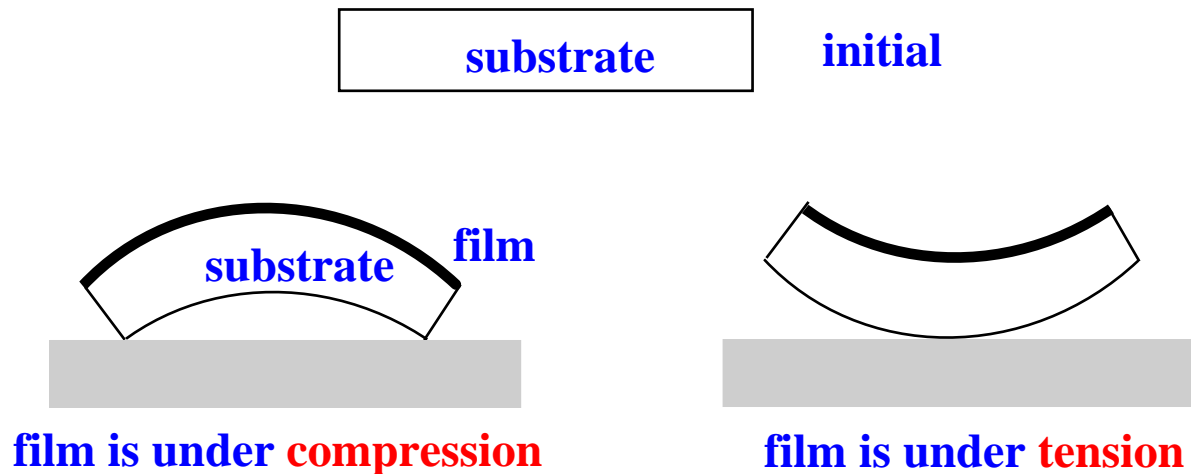
S. Wang and M. Kryder, personal contact, 1993



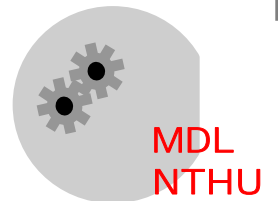


## Wafer curvature technique

- The most common technique to determine thin film residual stresses is measuring **wafer curvature**



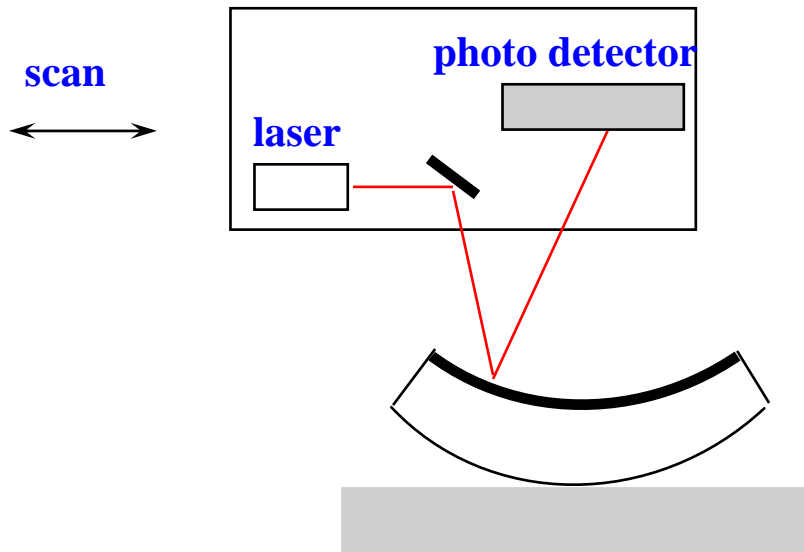
- The **radius of curvature** is varied with the magnitude of residual stresses





- **Stoney's equation**

$$\sigma = \frac{Eh^2}{6Rt(1-\nu)}$$



**$E/(1-\nu)$ : the biaxial elastic modulus of the substrate**

**$h, t$ : the thickness of the film ( $t$ ) and substrate ( $h$ )**

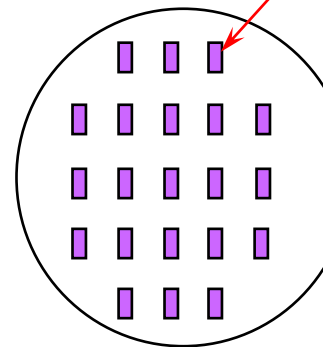
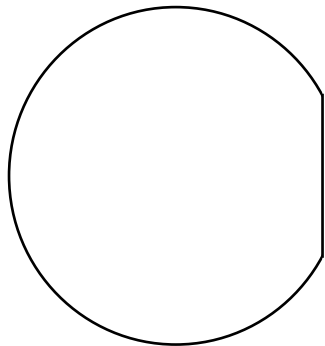
**$R$ : the measured radius of curvature**

**$\sigma$ : the average film stress**

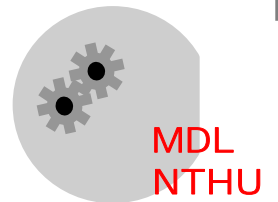




- **The disadvantages of the wafer curvature technique are**
  - + **Not sensitive**
  - + **Average stress of the whole wafer**
- **Stress measurement using micromachined structures**
  - + **Same dimensional scale as thin film - sensitive**
  - + **Local measurement instead of global measurement**



**unit of micromachined structure**



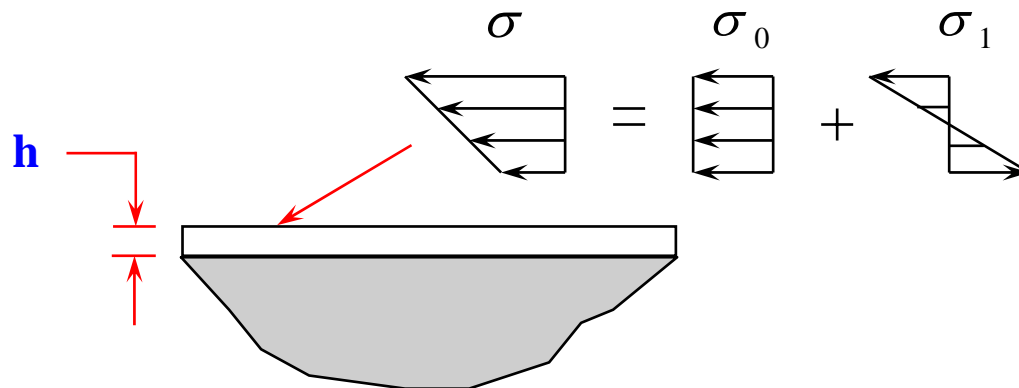


- Residual stress can be represented as a **polynomial**
- For the first approximation, the residual stresses containing **(1) mean**, and **(2) gradient** components

$$\sigma = \sum_{k=0}^{\infty} \sigma_k \left(\frac{y}{h}\right)^k \approx \sigma_0 + \sigma_1 \left(\frac{y}{h}\right)$$

mean residual stress

gradient residual stress





- **Compression  $\sigma_0$**
- **Tension  $\sigma_0$**
- **Gradient  $\sigma_1$**



# Bulk Micromachined Test Structures

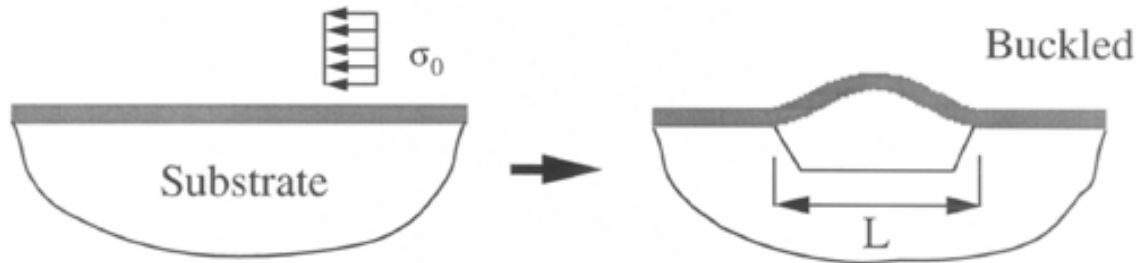




# Critical Buckling Beam Method

Guckel, Randazzo, and Burns, *J. of Applied Physics*, 1985

- Fabricate micromachined beams out of the thin film material for which the residual stress is desired



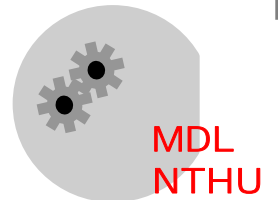
- Idealization: critical beam length

$L < L_{cr}$  unbuckled

$L > L_{cr}$  buckled

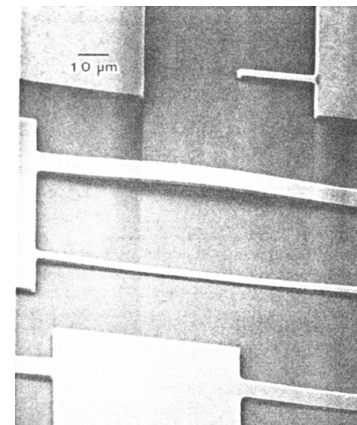
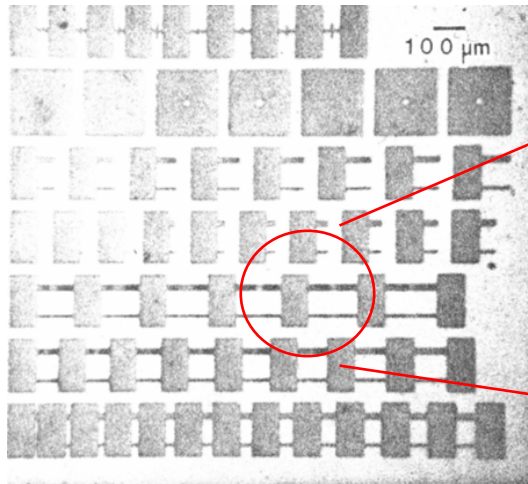
where

$$L_{cr} = 2\pi \sqrt{\frac{EI}{\sigma_0 A}}$$





- **Key processes of this technique**
  - + **Fabrication of micromachined beams with different length**
  - + **Use optical microscope to find the **critical buckling beam length  $L_{cr}$****
  - + **The residual stress is determined from  $L_{cr}$**
- **Disadvantages**
  - +  **$L_{cr}$  is determined subjectively**
  - + **Need very accurate beam thickness to prevent error of residual stress**

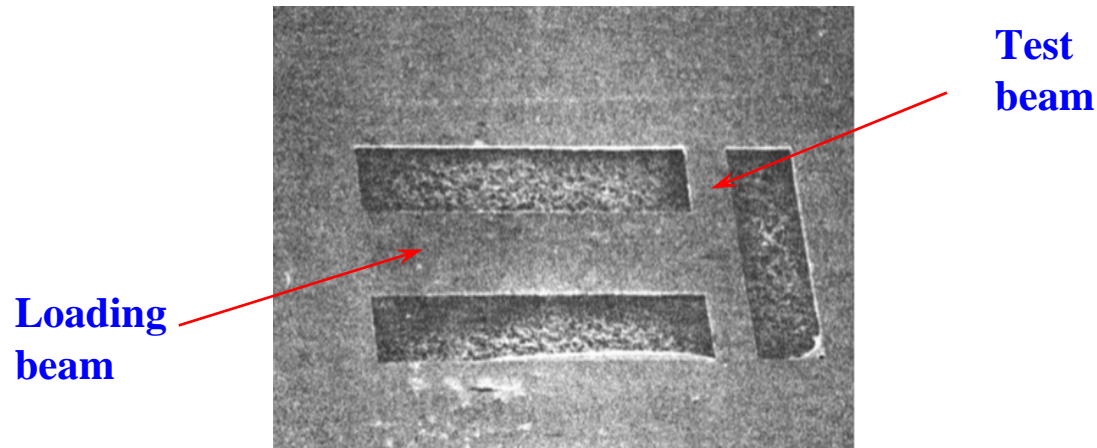




# T-shape Plate Method

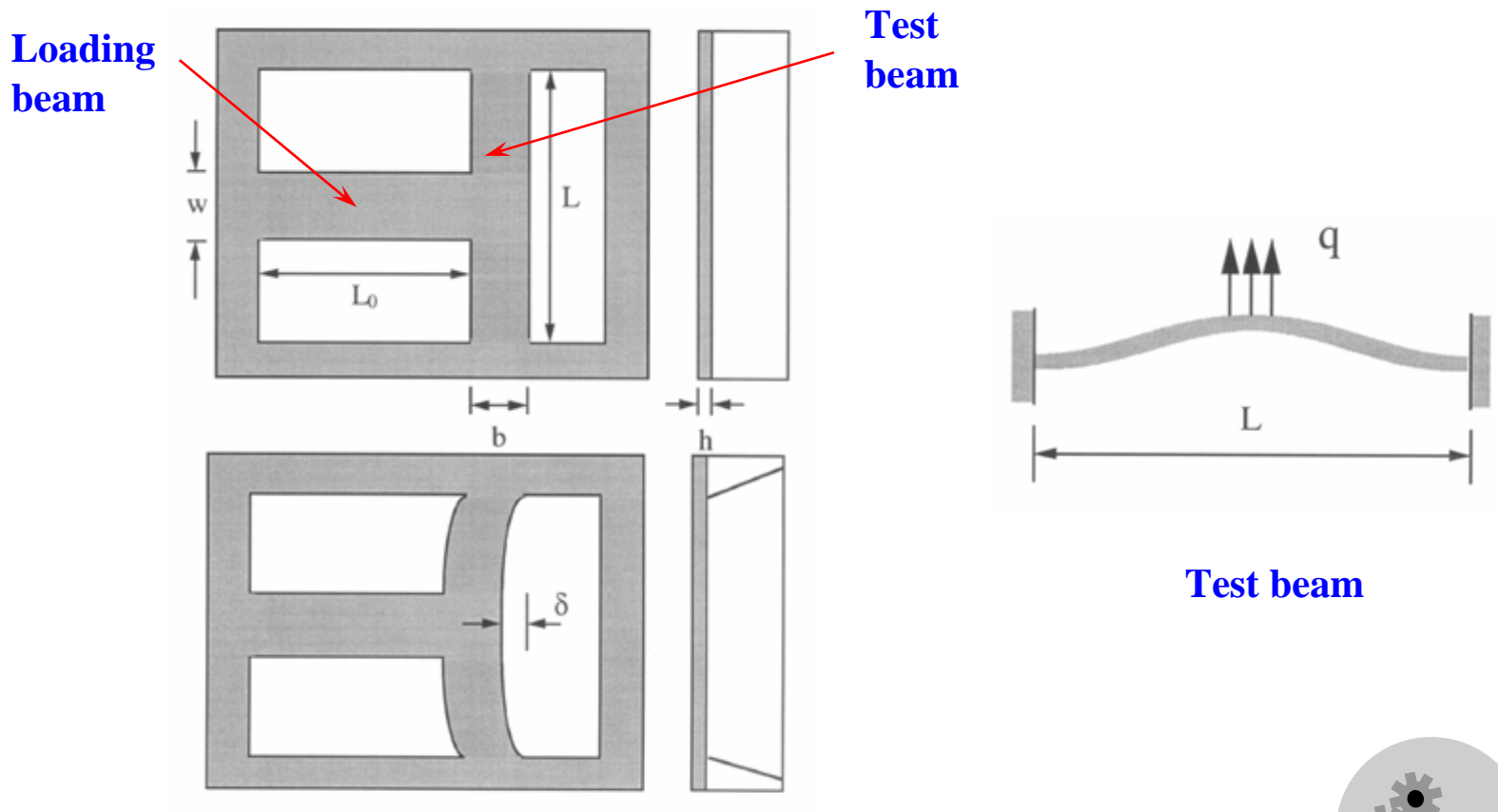
M. Mehregany, R.T. Howe, and S.D. Senturia, J. of Applied Physics, 1987

- In general, **tensile residual stress** will not lead an **out of plane** deformation to the micromachined structures
- **T-shape structure** is designed to give a significant deflection,  $\delta$ , under the relief of **tensile residual stress**





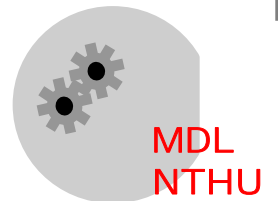
- Configuration of the T-shape diagnostic structure before and after the relief of tensile residual stress







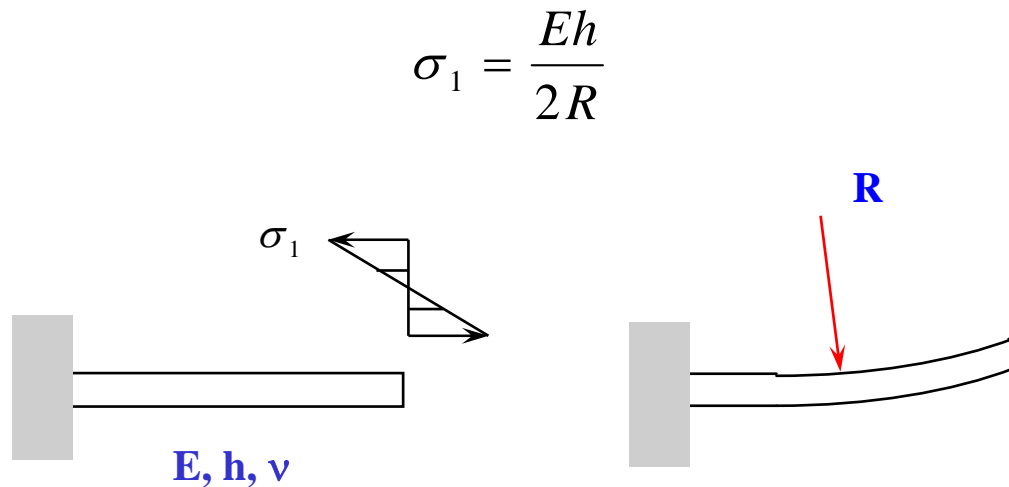
- **Disadvantages of this technique**
  - + **Large structure** is required to provide a measurable deflection amplitude for the optical microscope
  - + The **initial tension of the test beam** has been ignored
  - + **Boundary condition** of the test beam
  - + The loading beam also gives a constraint to the deflection of at the contact region
- **Comment: a simple structure can (1) reduce the error arrived from modeling, and (2) simplify the analytical model**

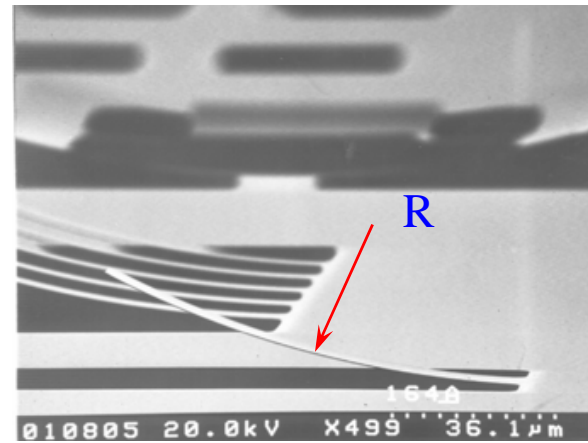
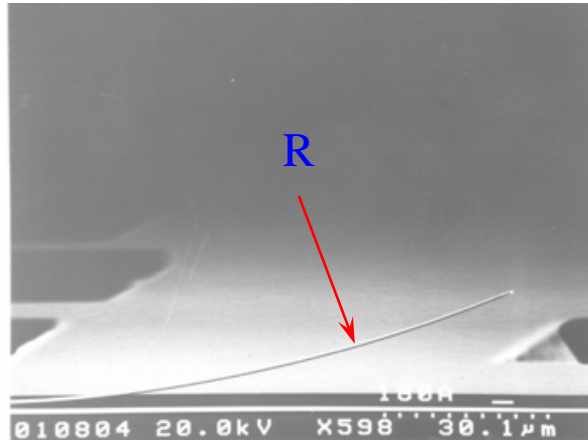




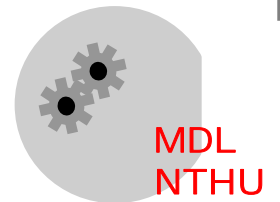
## Cantilever Beam Method

- The relief of a **gradient residual stress**  $\sigma_1$  will lead to a **bending moment** applying on the thin film cantilever
- The gradient residual stress can be determined by the **radius of curvature**  $R$  of the bent cantilever beam





Y.-L. Chen, J.-S. Shie, and W. Fang, 1997

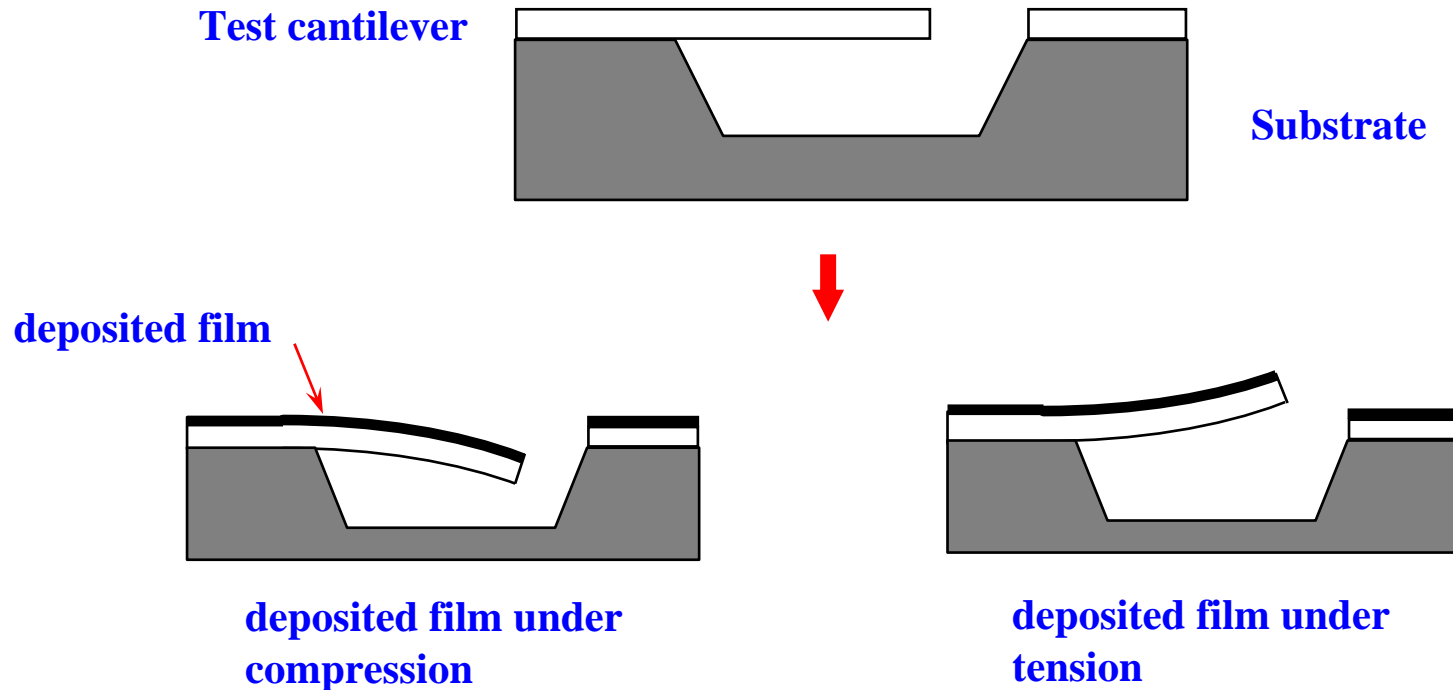




# Bilayer beam technique

W. Fang and J.A. Wickert, J. of Micromech. and Microeng.,1995

- Deposit the film on top of a test cantilever to form a **bilayer beam**, therefore the residual stress of the film can be measured by **the deflection of the bilayer cantilever**

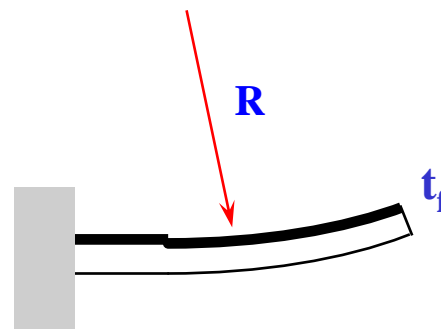
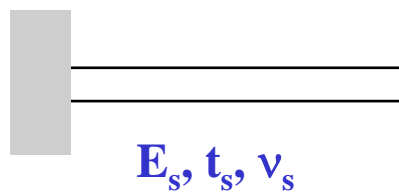




- **Stoney equation**

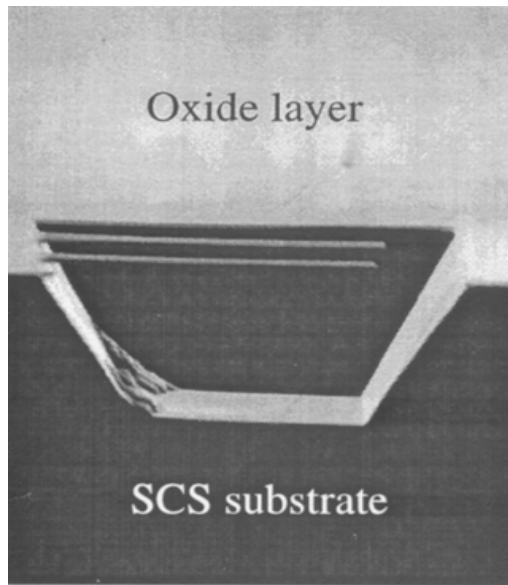
$$\sigma_0 = \frac{E_s (t_s)^2}{6R t_f (1 - \nu_s)}$$

**measured**

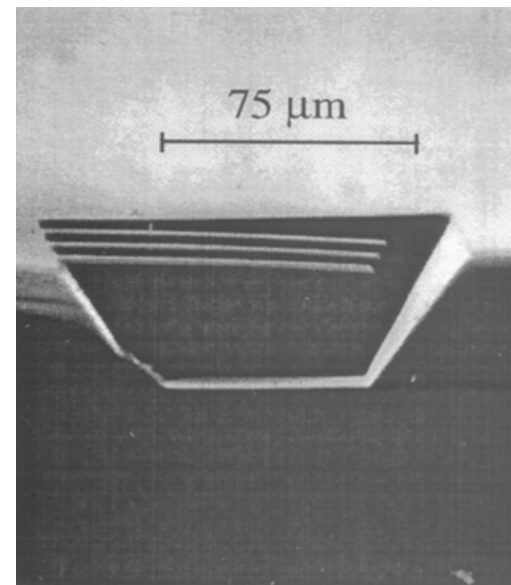




- **Bilayer beam technique can be applied to measure residual stress of thin films whose thickness are too small to fabricate micromachined structures**

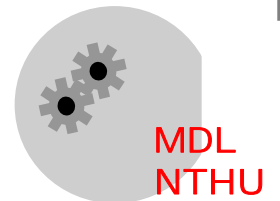


**SiO<sub>2</sub> test cantilever**



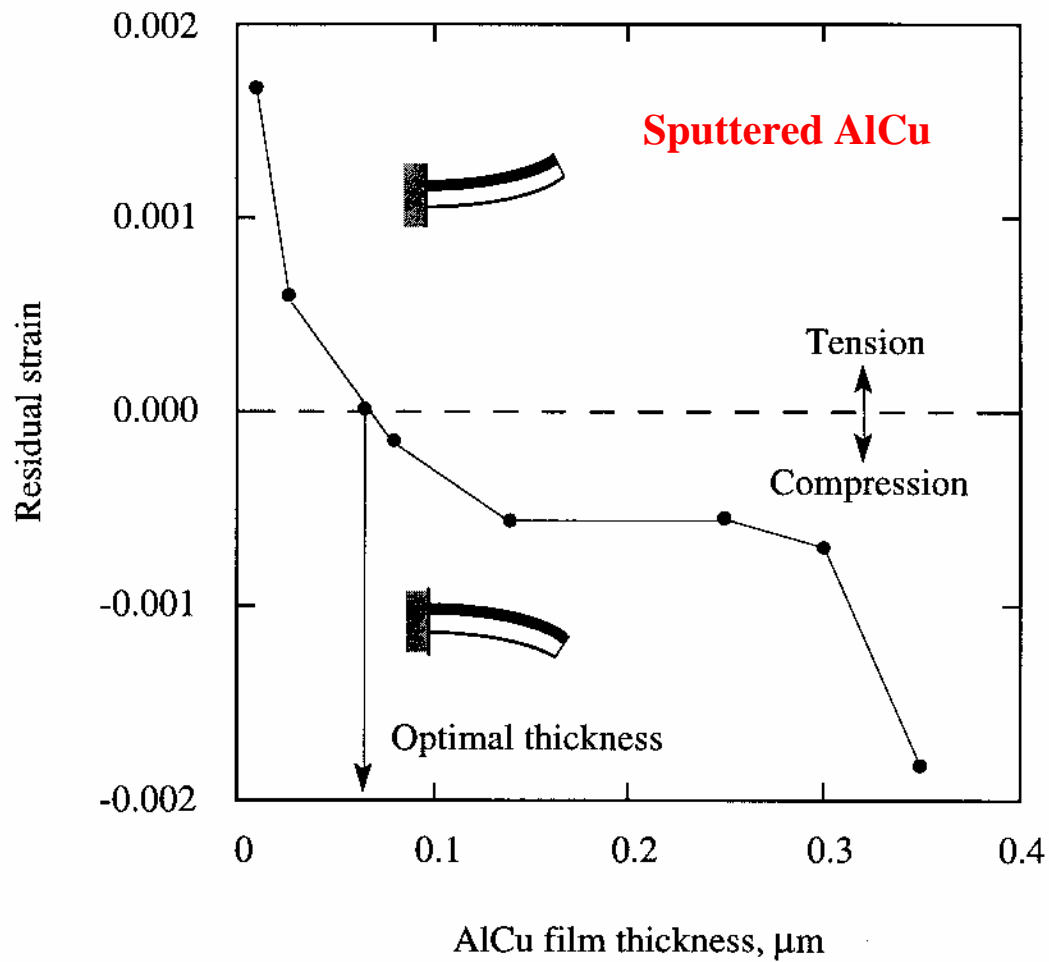
**Test cantilever deposited with a 15 nm thick *DLC* film**

**W. Fang and J.A. Wickert, *J. of Micromechanics and Microengineering*, 1995**





- Variation of the residual strain with the thickness of *AlCu* film

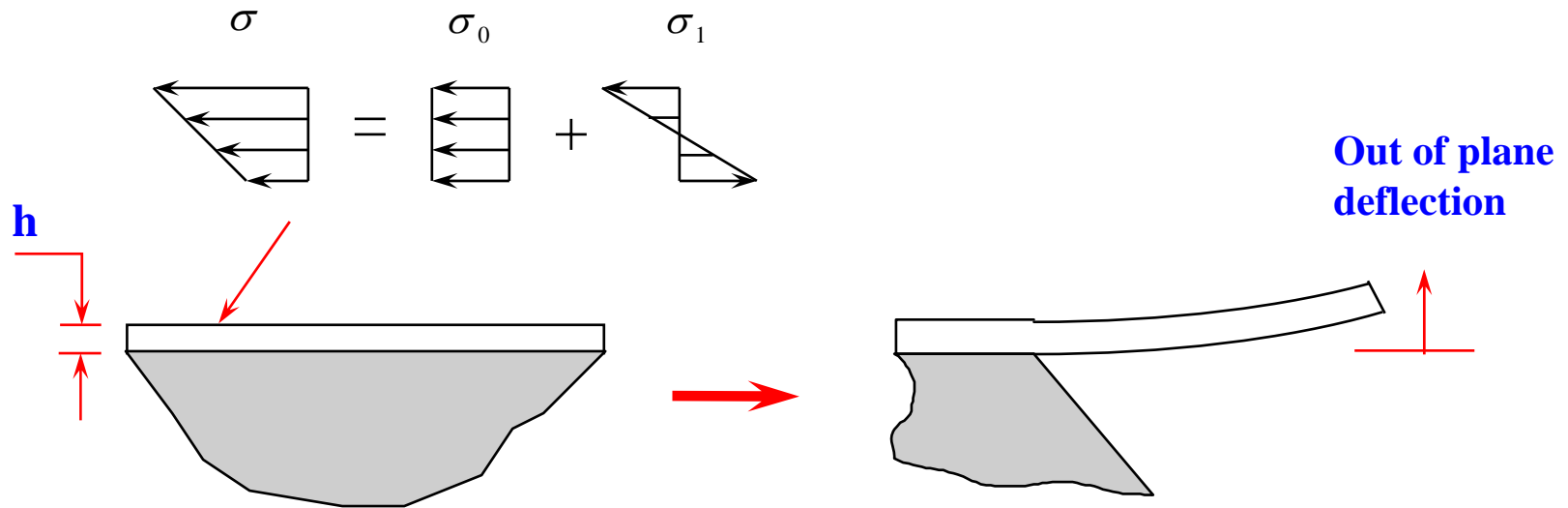




# Boundary rotation method

W. Fang and J.A. Wickert, J. of Micromechanics and Microengineering, 1996

- The **mean** and **gradient** residual stresses are determined simultaneously by an **out of plane deformed** cantilever beam

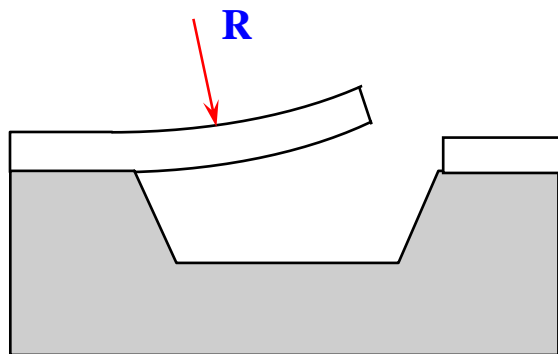




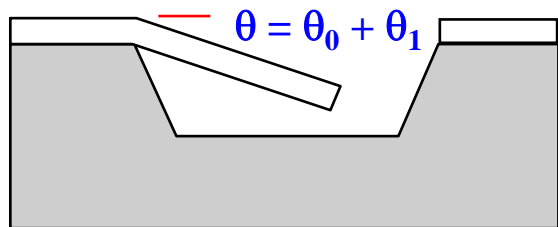


- In short, the beam will be deflected with **curvature** by  $\sigma_1$ , and **slope** by  $\sigma_1$  and  $\sigma_0$

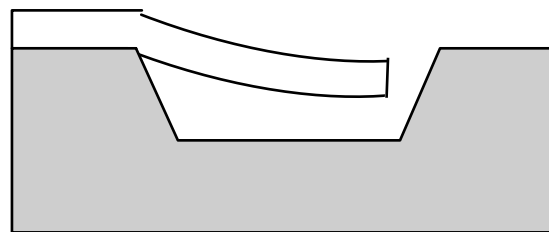
- The total deflection profile is,  $y = \theta x + \frac{x^2}{2R}$



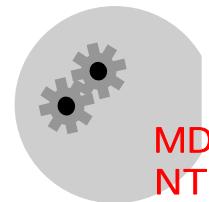
$$y = \frac{x^2}{2R}$$



$$y = \theta x$$

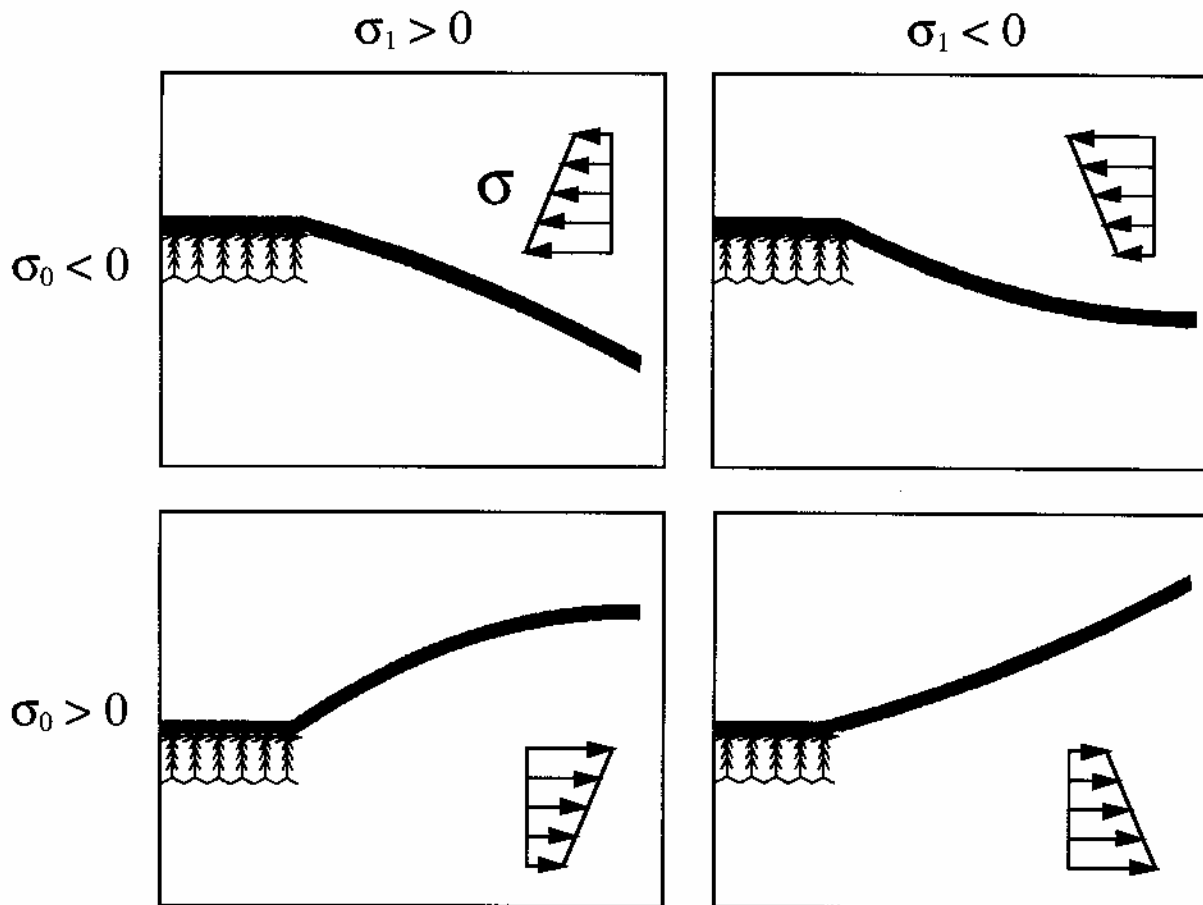


$$y = \theta x + \frac{x^2}{2R}$$

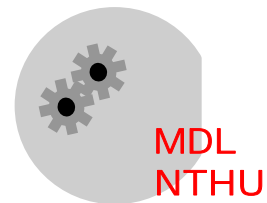




- Deformation profile for the four possible stress states



Fang and Wickert, J. of Micromechanics and Microengineering, 1996





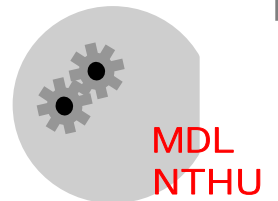
- **FEM analysis**

+ **The angular deflection due to the mean residual stress**

$$\theta_0 = \frac{\sigma_0}{E} (1.33 + 0.45\nu)(-0.014h + 1.022)$$

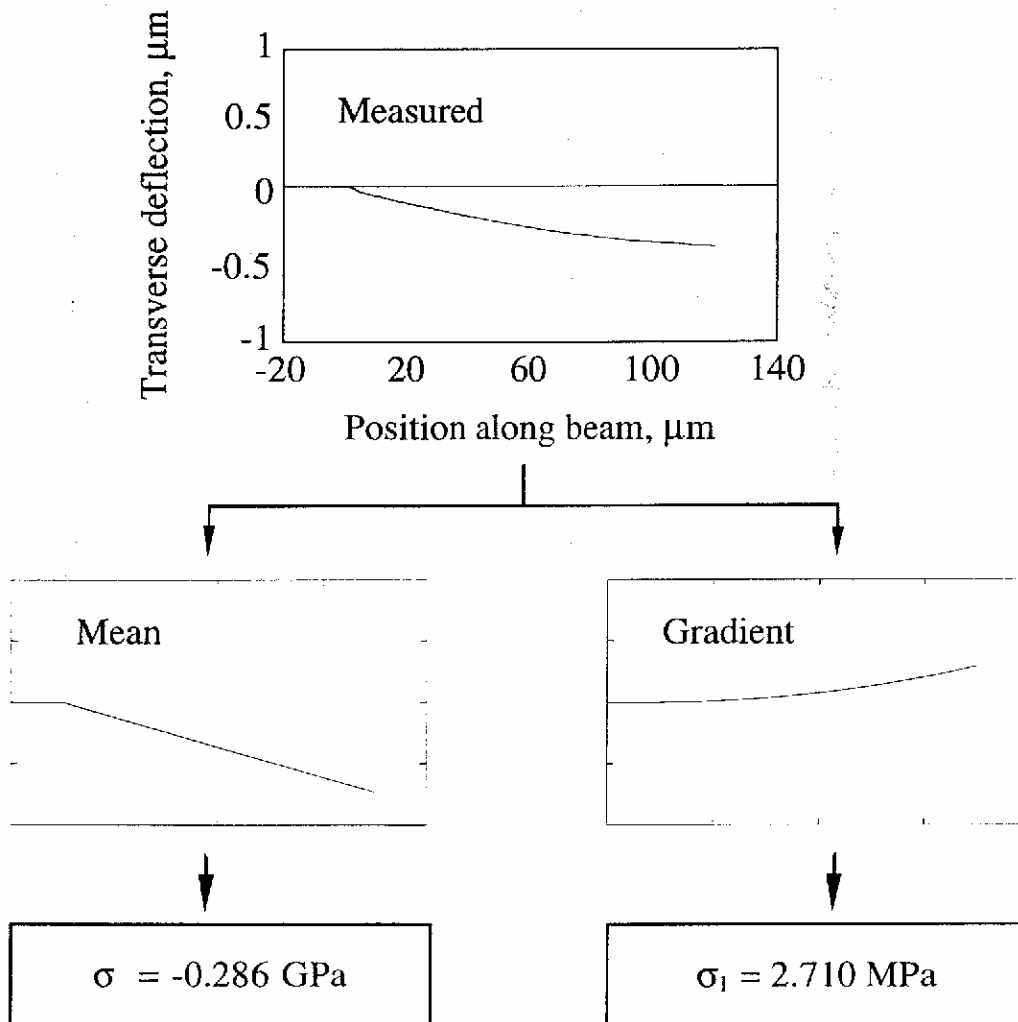
+ **The angular deflection due to the gradient residual stress**

$$\theta_1 = \frac{\sigma_1}{E} (0.0086h^2 - 0.047h + 0.81)$$



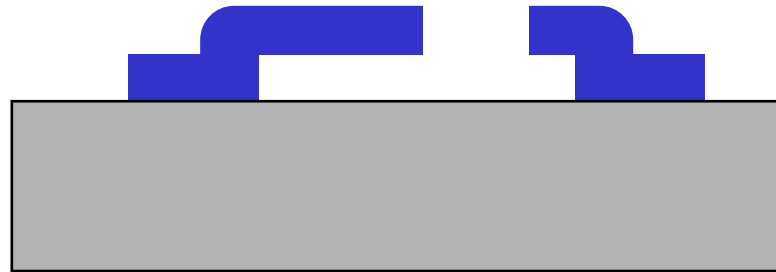


- Application : 1  $\mu\text{m}$  thick thermal silicon dioxide beam





# Surface Micromachined Test Structures





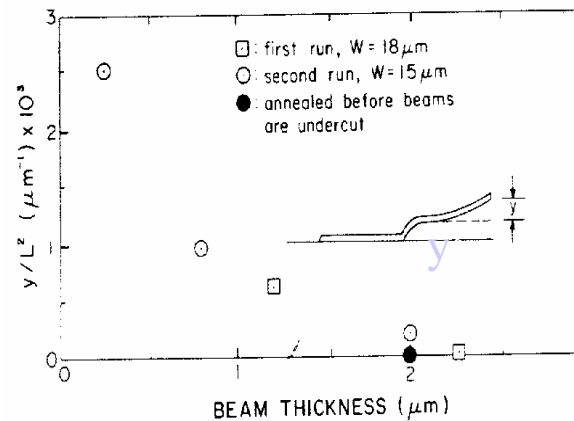
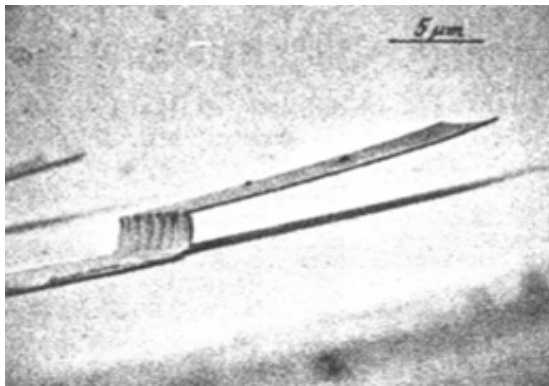
# Surface Micromachined Cantilever

R.T. Howe and R.S. Muller, J. Electrochem. Soc., 1983

- The relation between tip deflection  $y$  and the bending moment  $M$  arrived by **the gradient residual stress** is

$$y = 6ML^2/(Eh^3)$$

+ This equation is the same as the equation  $\sigma = Eh/(2R)$



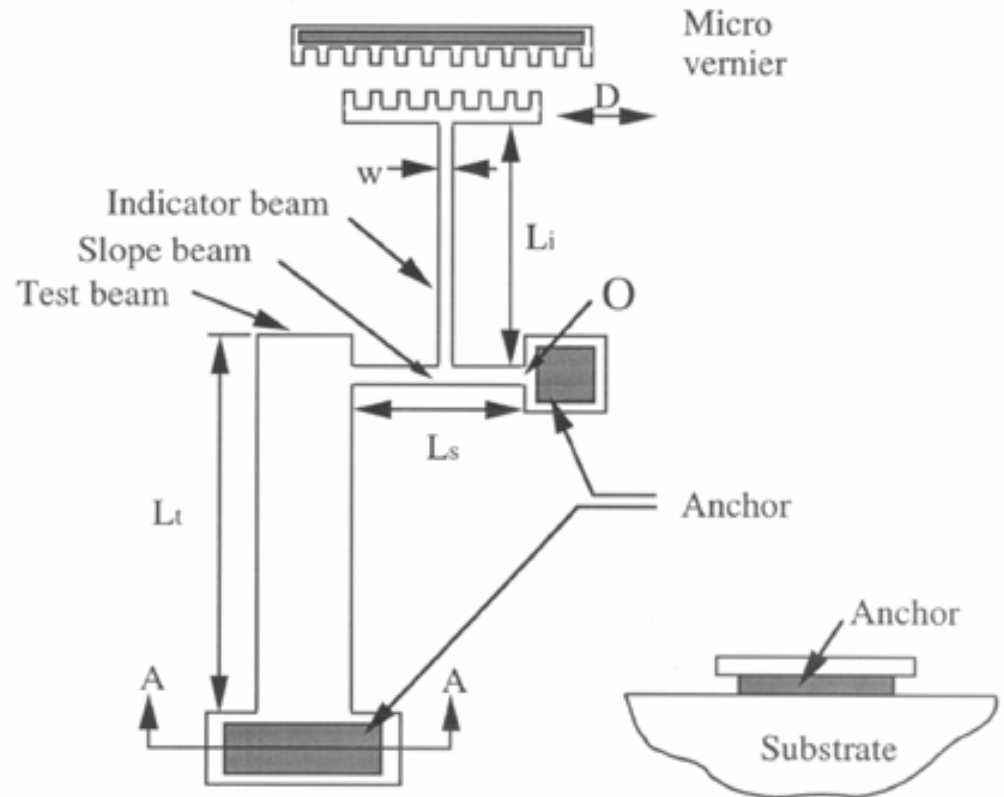


# Micro Vernier Technique

L. Lin, et.al., *Proc. of the 6th IEEE MEMS Workshop, 1993*

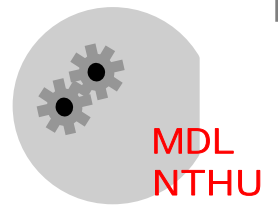
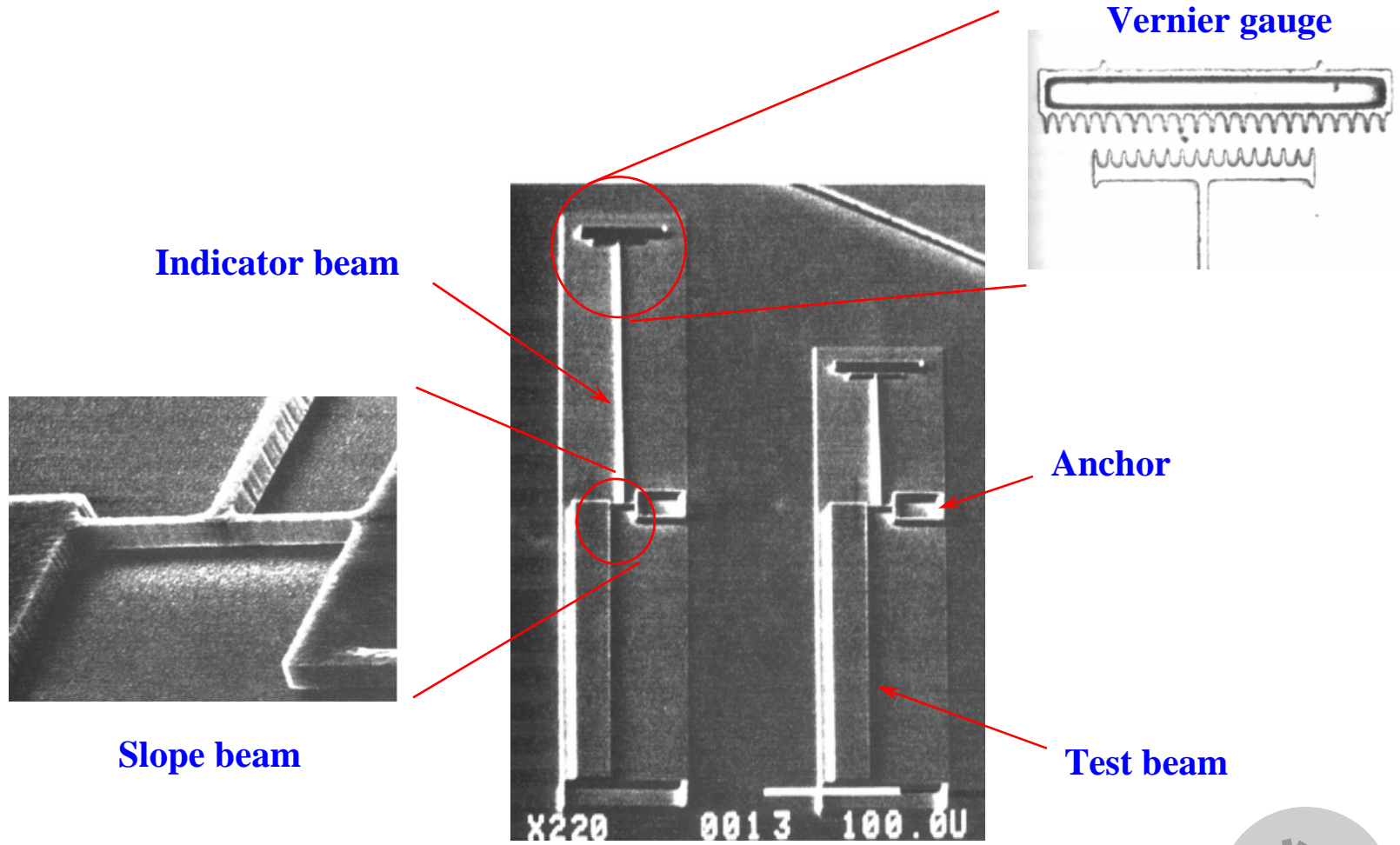
- Configuration of the micro vernier structure (**in-plane deformation magnification mechanism**)

- + The **test beam** length will be changed when the residual stress is relief
- + Thus, the **slope beam** will rotate about point O
- + The **indicator beam** will also rotate





- SEM photo of the micro vernier







- The deflection angle at the center of the **slope beam** is

$$\theta = \frac{3\delta}{2L_s} \frac{(1 - d^2)}{(1 - d^3)} \quad (1)$$

$$\text{where, } d = \frac{w}{L_s}$$



displacement of  
the **test beam**

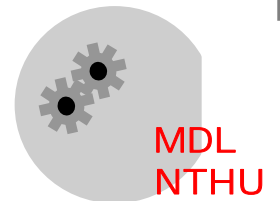
- The displacement measured by the vernier is

$$e = L_i \theta \quad (2)$$

- Since the residual strain is the ratio of  $d$  and  $L_t$ , the residual strain can also be rewritten as an equation with measurable parameters

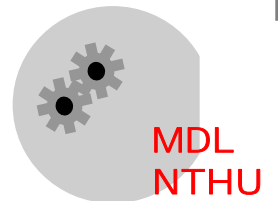
$$\varepsilon = \frac{\delta}{L_t} = \frac{2L_s e}{3L_i L_t} \frac{(1 - d^2)}{(1 - d^3)}$$

Measured





- **Many design issues need to be considered**
  - + **Large structure** is necessary to provide a large deflection amplitude which can be measured easily by **optical microscope**
  - + The residual stress of the **slope beam**
  - + The stiffness of the **slope beam**
  - + **Buckling of the test and slope beam**
  - + The application of this technique is limited to the thin film which used to fabricate **surface micromachined structures**

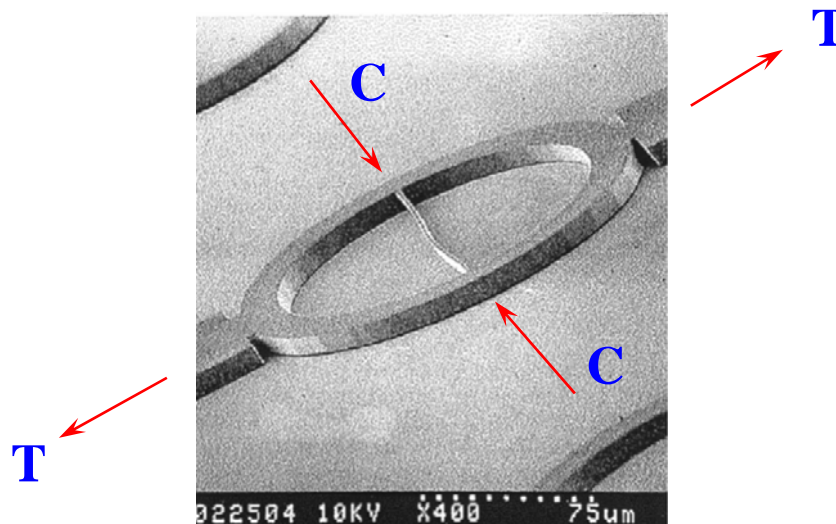




# Ring Structure

H. Guckel, et.al., J. of Micromechanics and Microengineering, 1992.

- Diagnostic structures of greater complexity are designed to measure **tensile residual stress**
- When the film is under tension, the ring structure will applied a compression on the thin beam inside the ring to cause the beam **buckle**

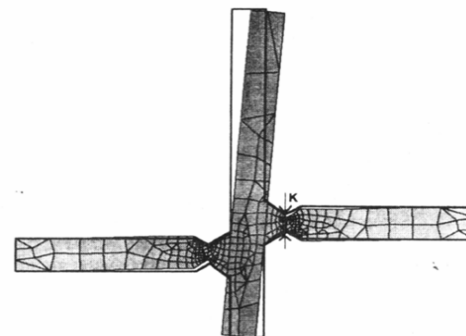
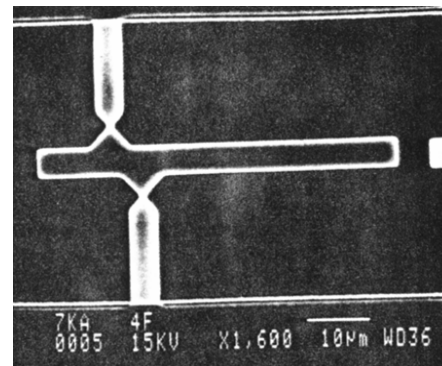
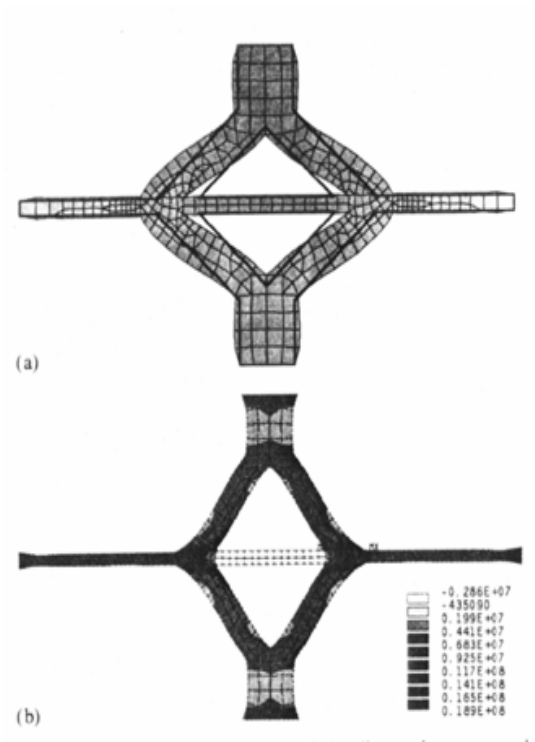




# Other Surface Structures

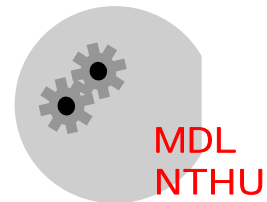
B.P. van Drienuizen, et.al., Sensors and Actuators, 1993.

- **Micromachined complicated diagnostic structures**





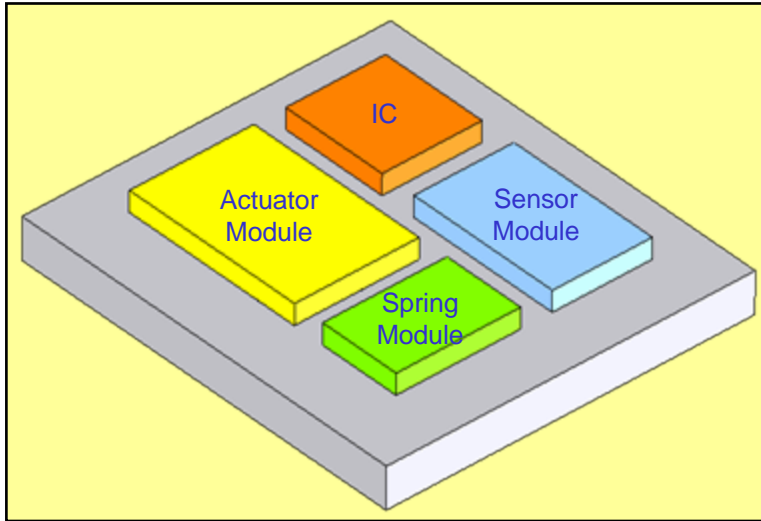
# On-chip Micro Instrument



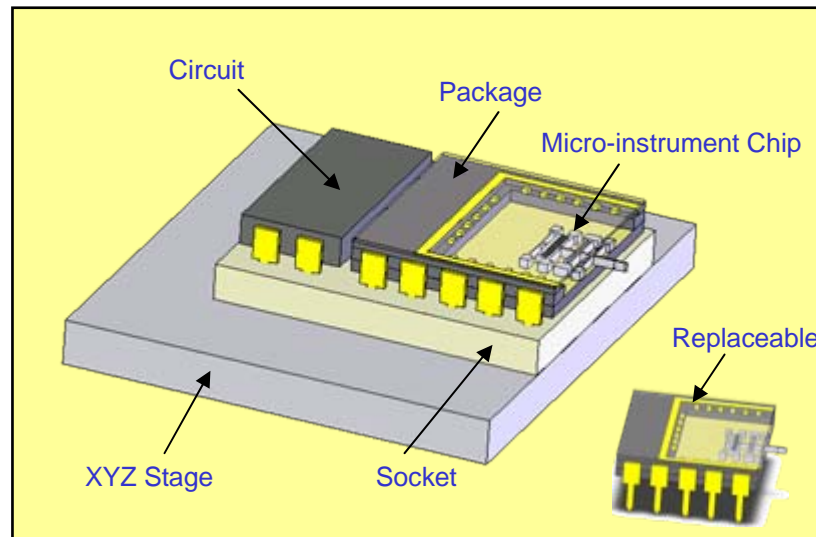
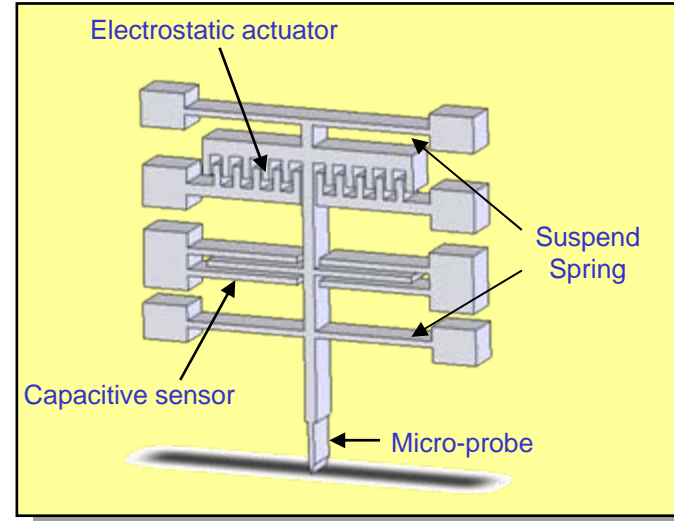


# Concept

## • Option requirement for end users

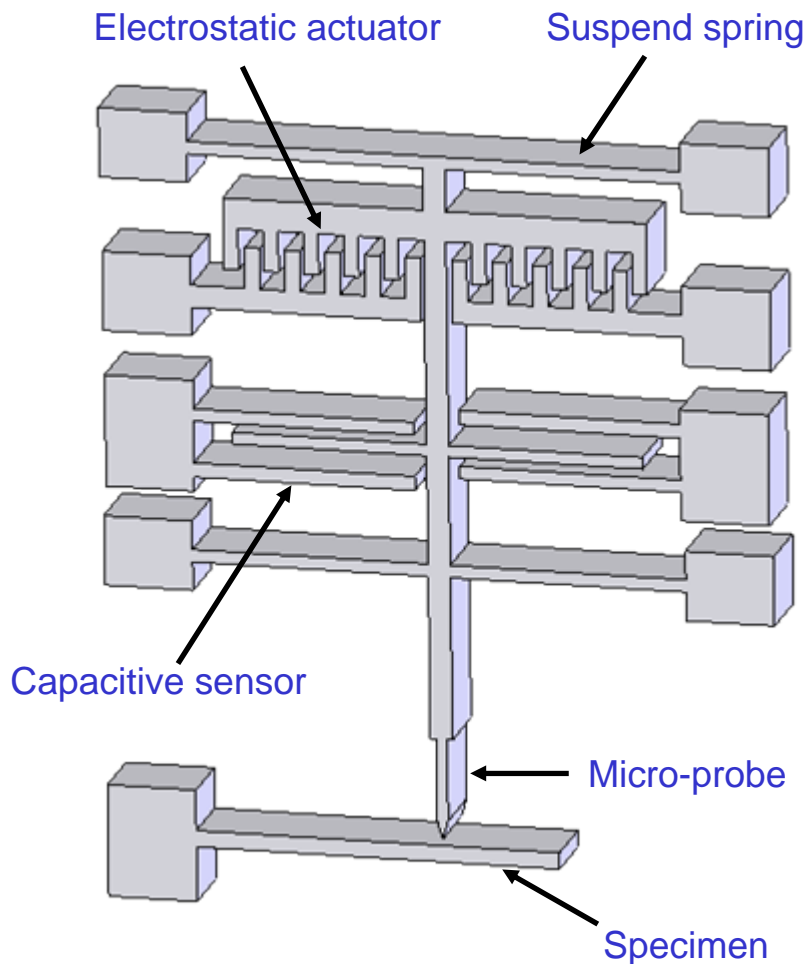


## • Micro-instrument Chip





# Design Issues



- Force on Specimen

$$F_s = F_a - K_y \cdot y$$

Actuator force      Stiffness of spring      Displacement sensing

- Suspended Spring

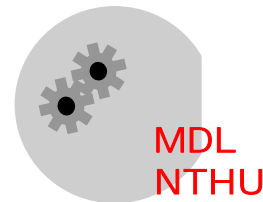
- Linear spring, and stiffness ratio is enough

- Electrostatic Actuator

- Constant force

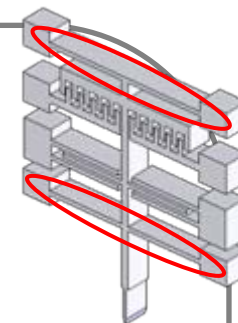
- Capacitive Sensor

- Linearity, min. initial capacitance, resolution

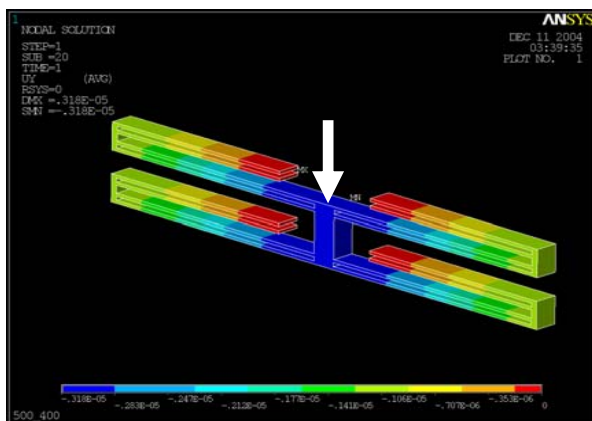




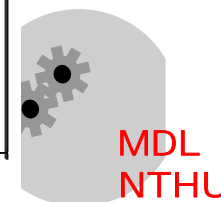
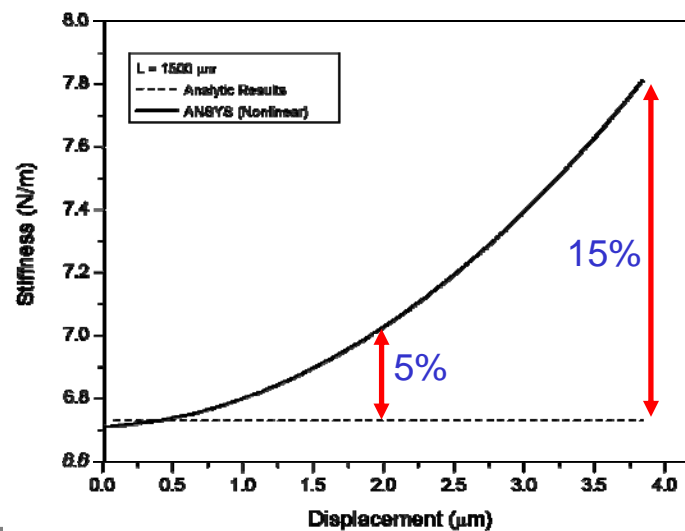
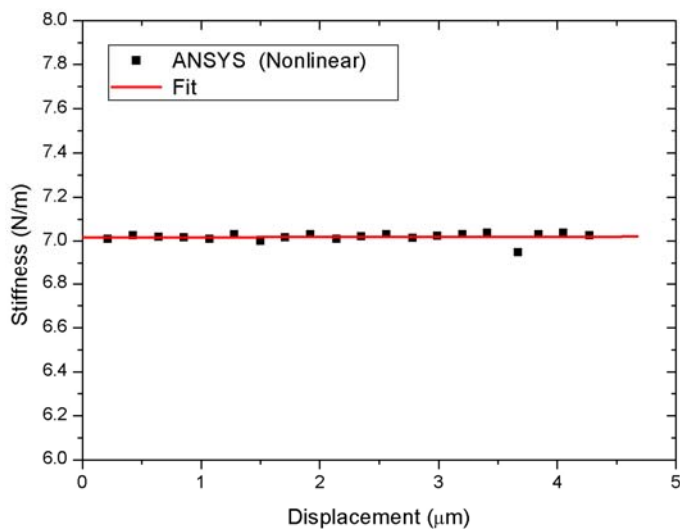
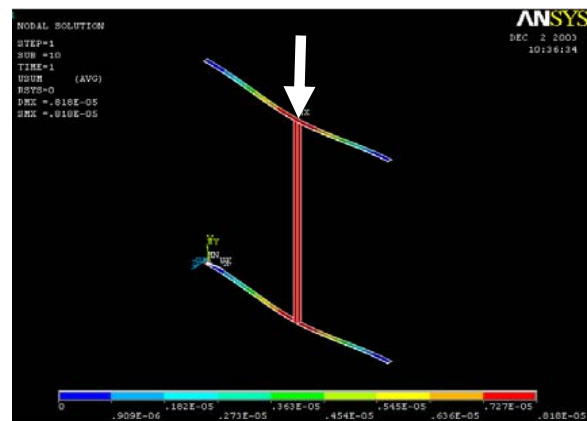
# Support Spring



- Folded beam



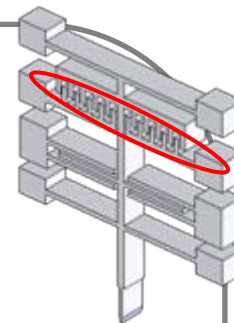
- Clamped beam





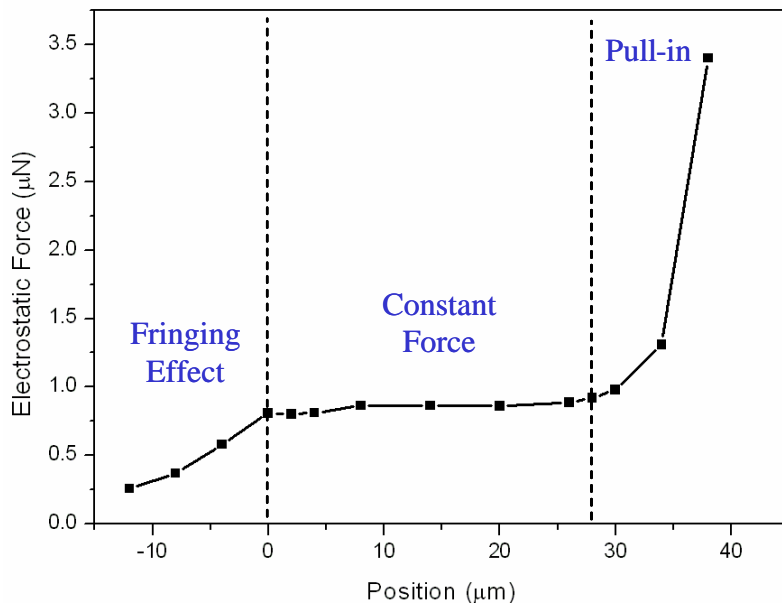
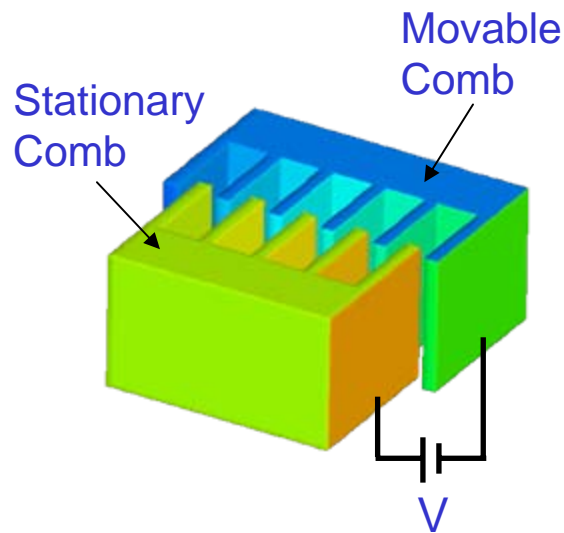
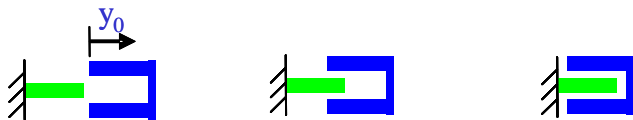


# Comb Actuator

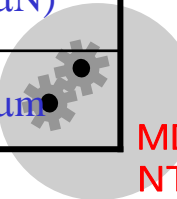


- Analytic Analysis
- Numerical Analysis
  - Commercial software Coventorware

$$F_a = N \frac{\epsilon t}{g} V^2$$

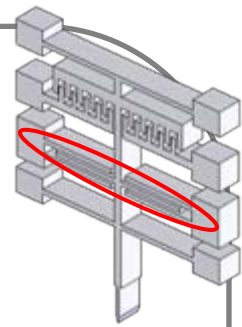


N	5
Voltage	50 (V)
Ideal Force	0.78 (µN)
Simulation Force	0.86 (µN)
Operation range	0-28 µm



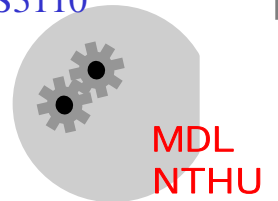
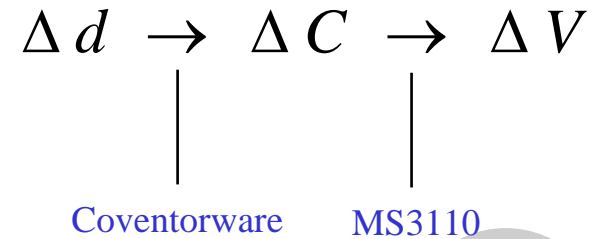
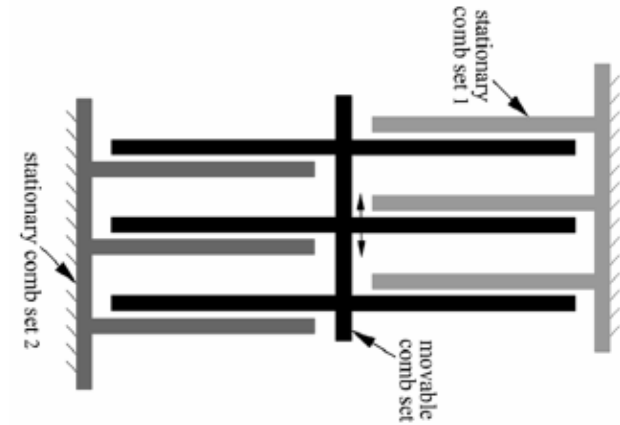
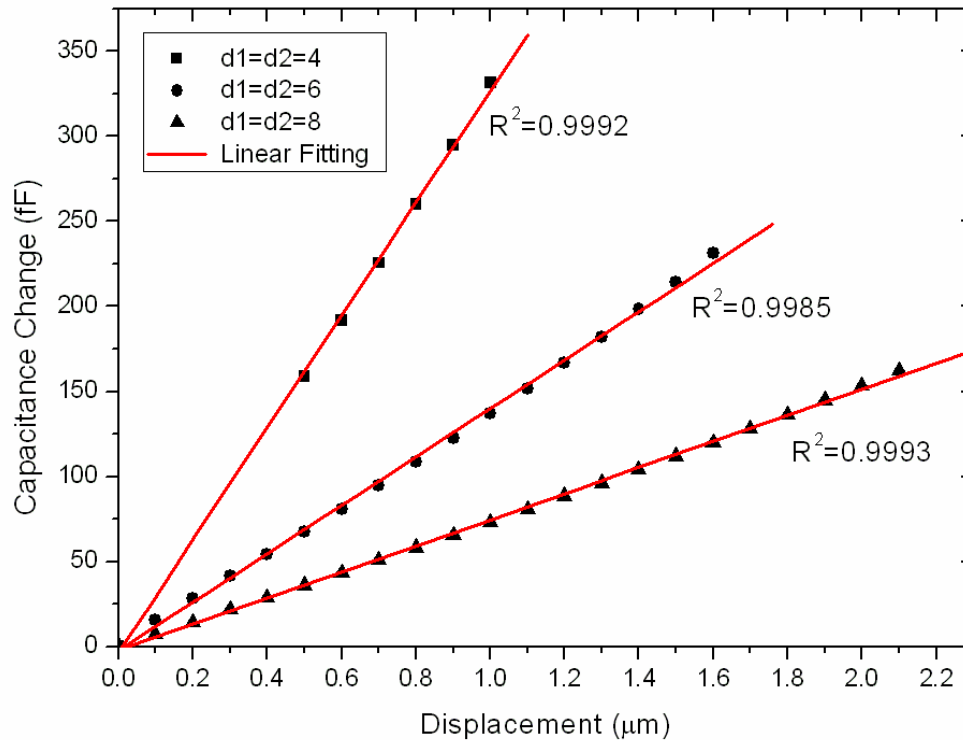


# Capacitive Sensor



- Analytic Analysis
- Numerical Analysis

$$\Delta C = C_0 \frac{d \cdot \Delta d}{d^2 - \Delta d^2}$$

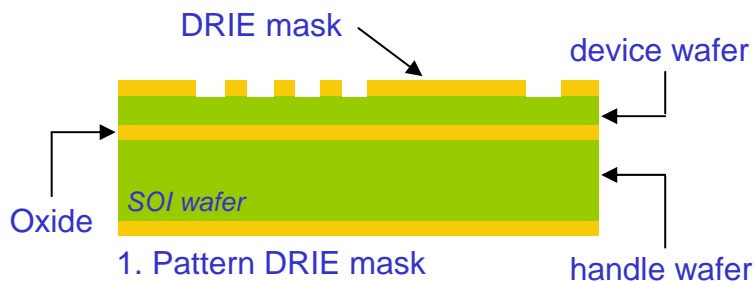




# Process Flow

- Microfabrication Processes

- Micro-instrument



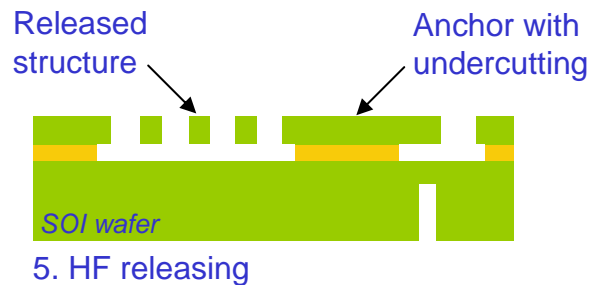
2. Pattern dicing mask



3. DRIE etching



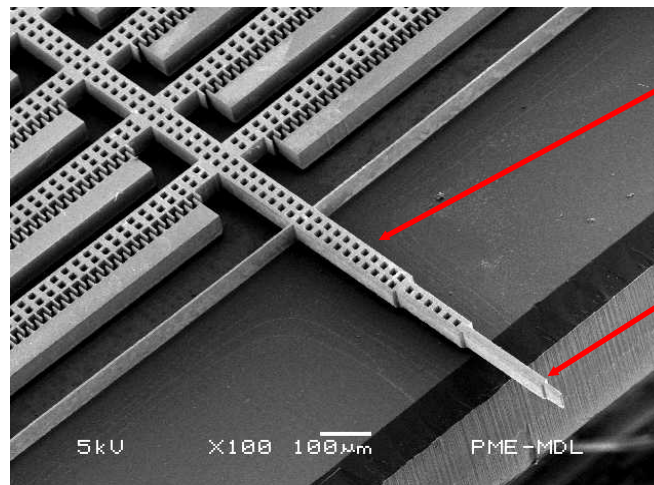
4. Dicing (200µm)



5. HF releasing

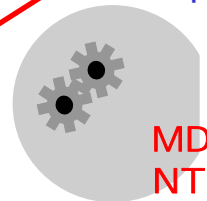


6. The probe freely hangs in air



Micro-instrument

Micro-tip

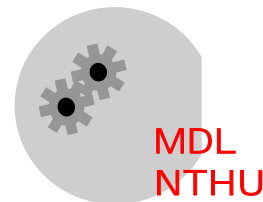
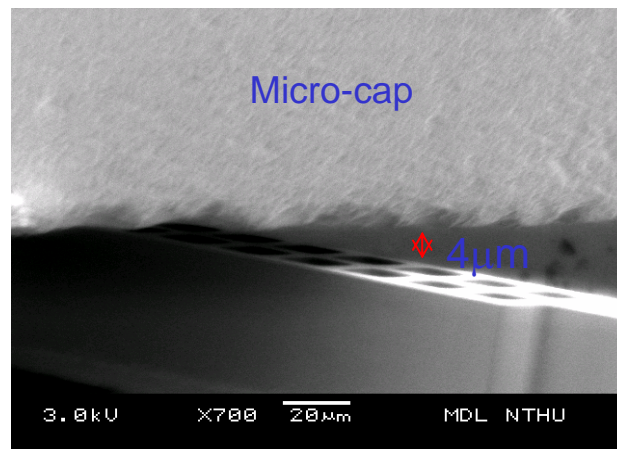
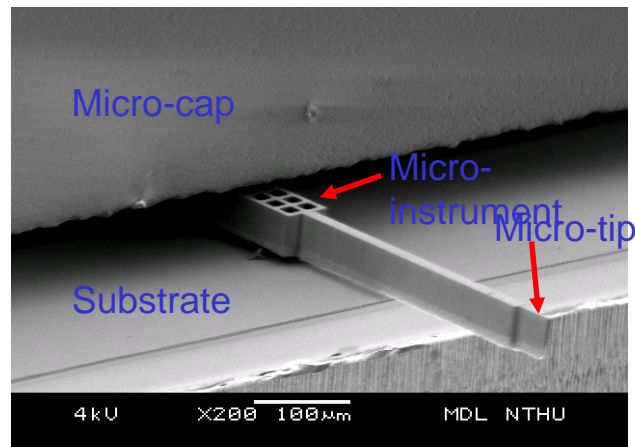
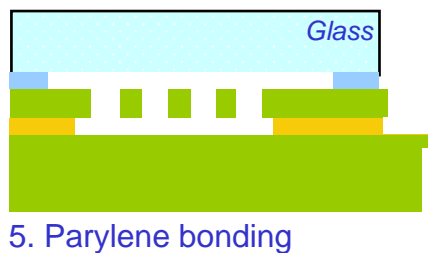
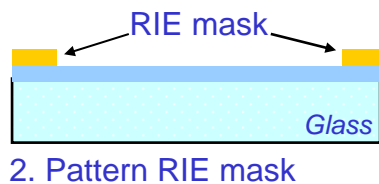




# Process Flow

- Microfabrication Processes

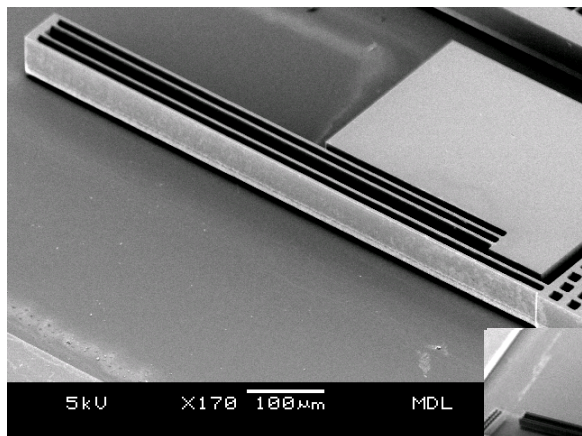
- Micro-cap



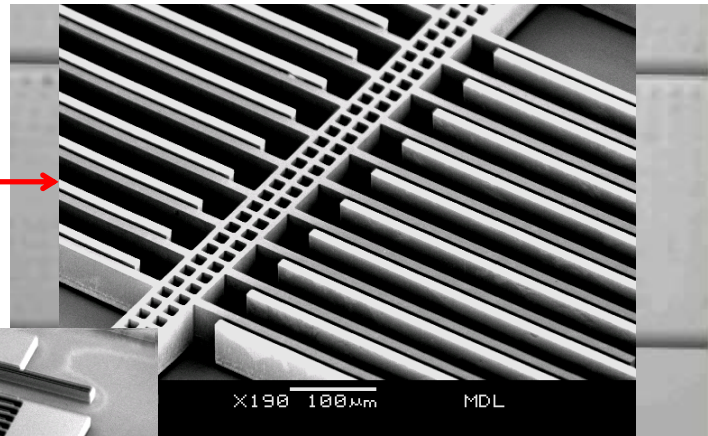
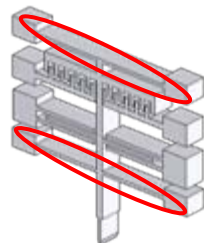




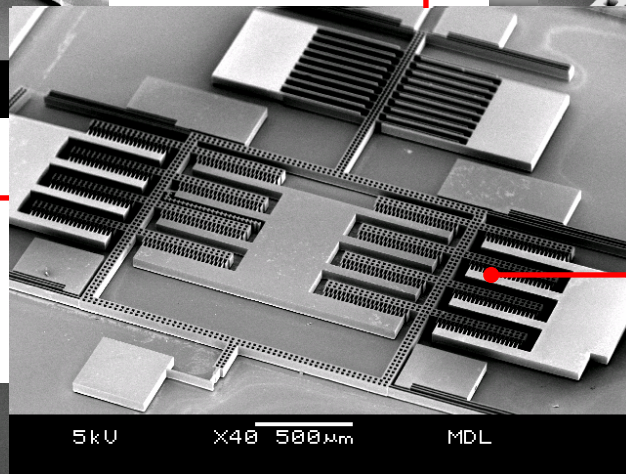
# Fabrication Results



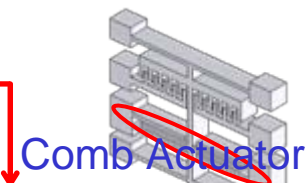
Support Spring



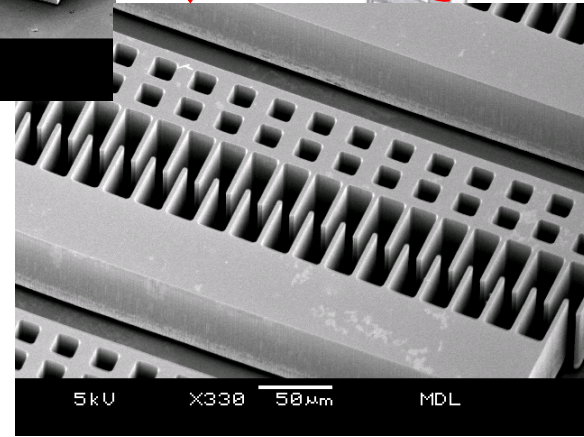
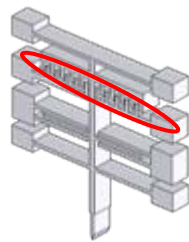
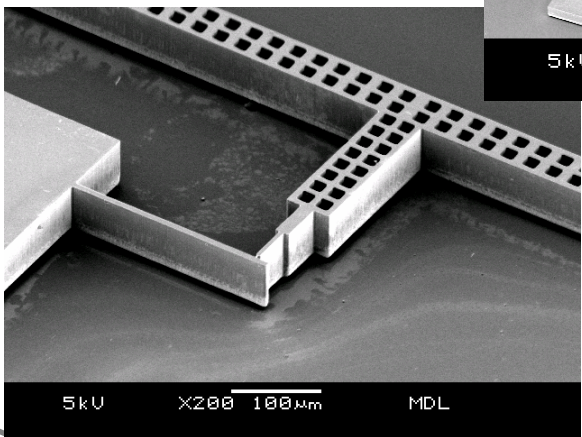
Capacitive Sensor



Bending Test

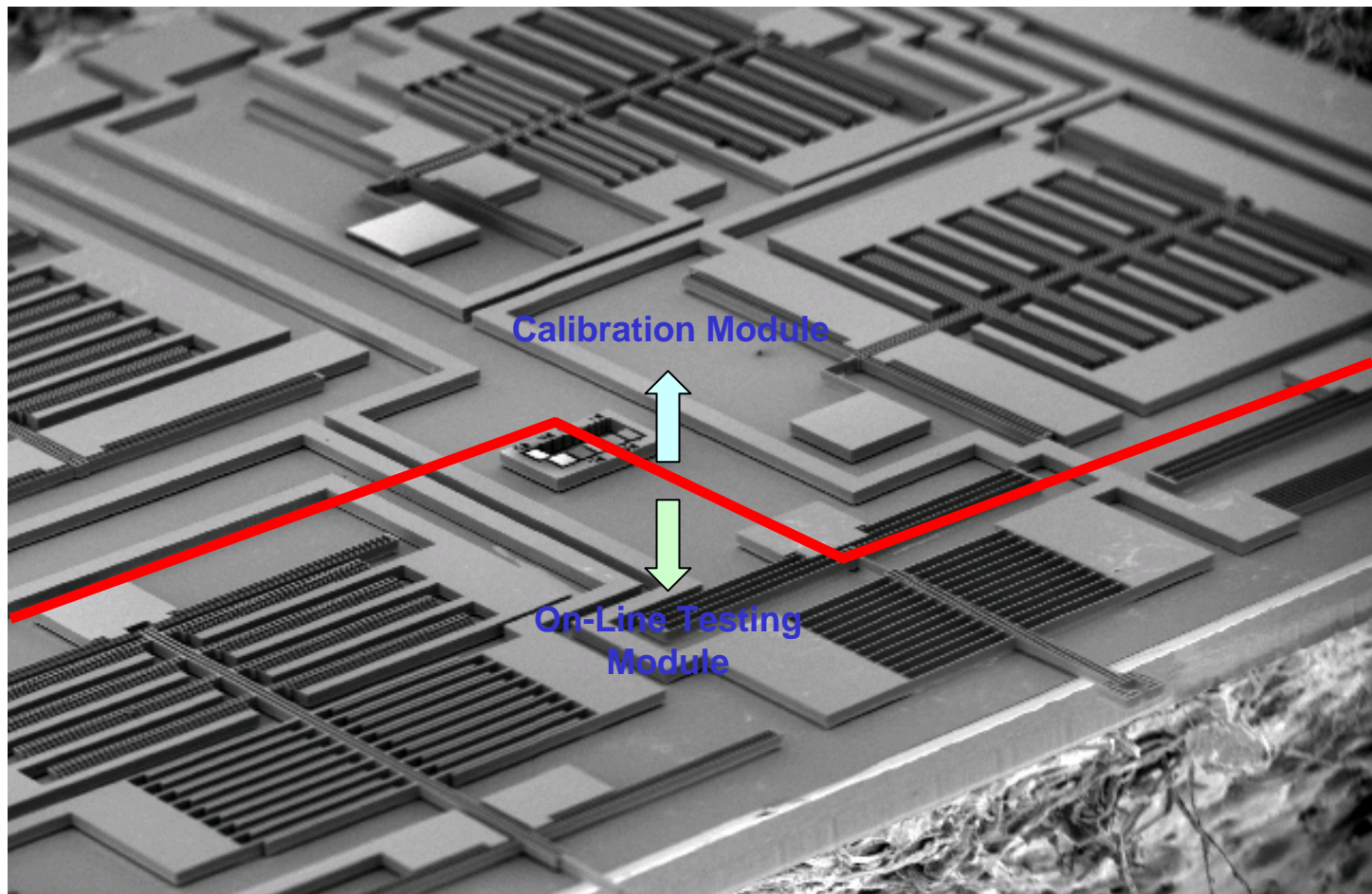


Comb Actuator





# Fabrication Results



5kV

X25

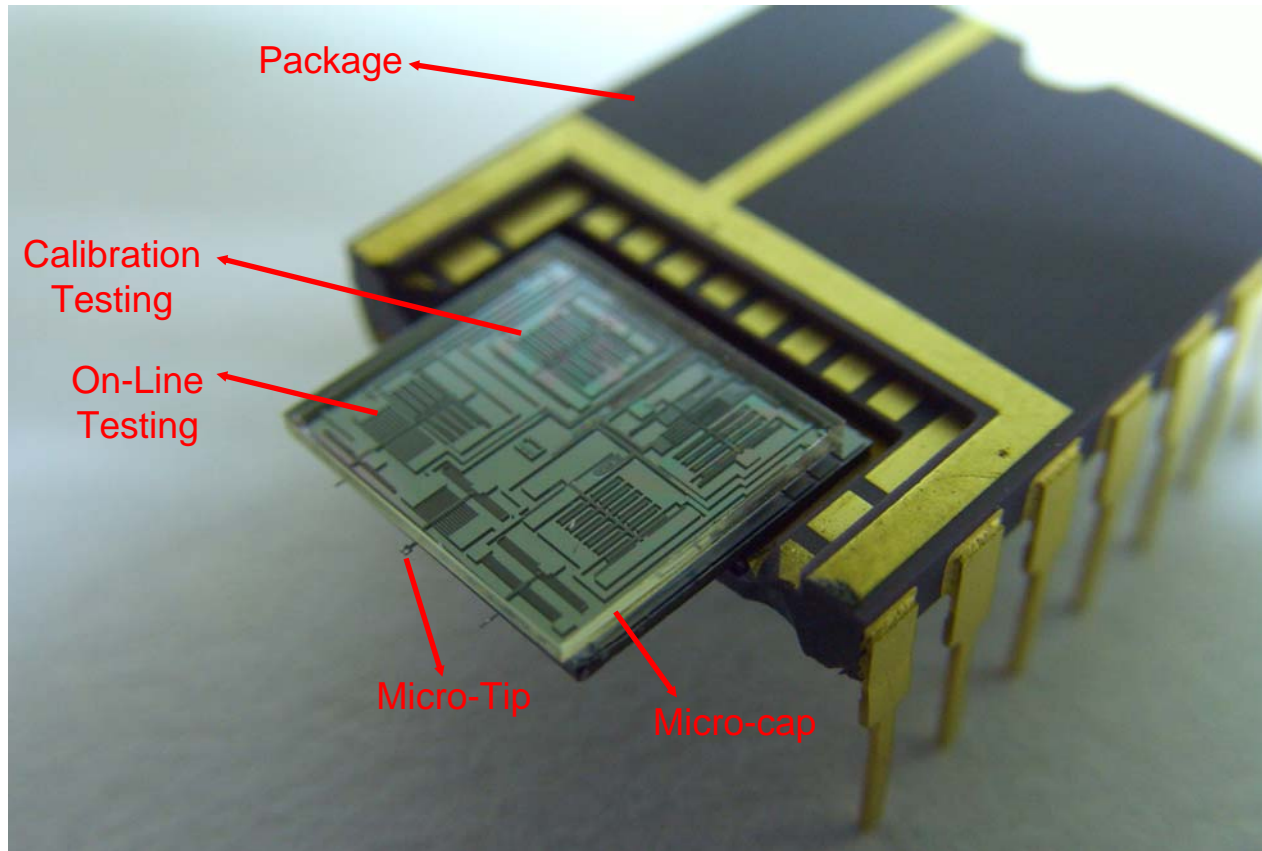
1mm

MDL NTHU





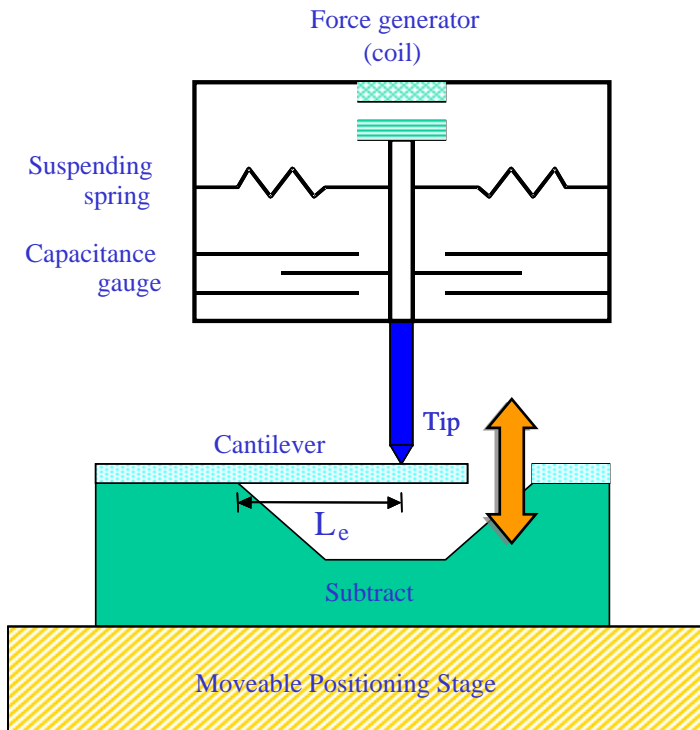
# Package



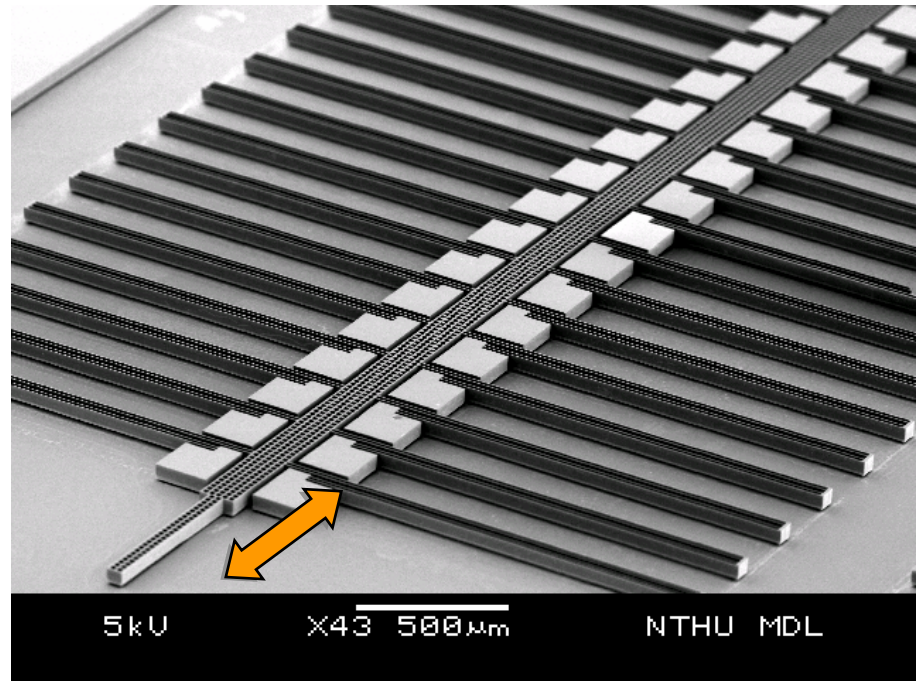


# Stiffness Calibration

- The out-of-plane stiffness of cantilever can be measured by nanoindenter.
- How to measure in-plane stiffness of folded beam ?



Out-of-plane motion



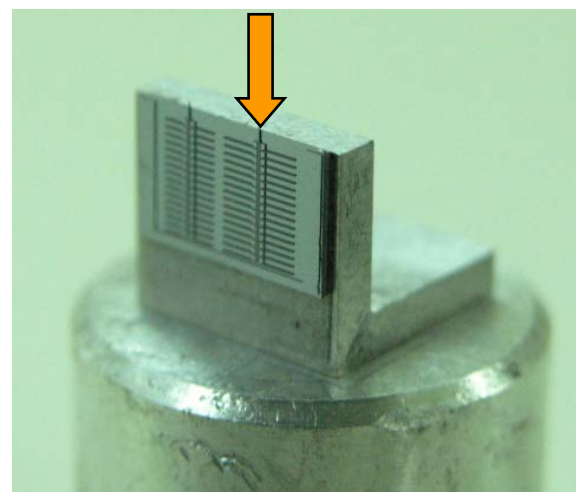
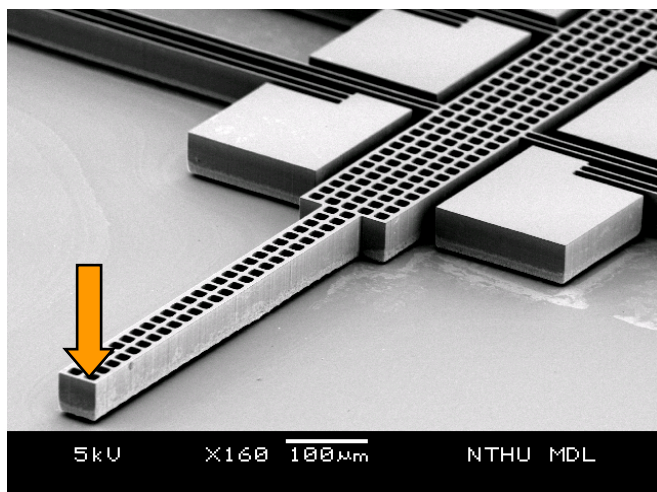
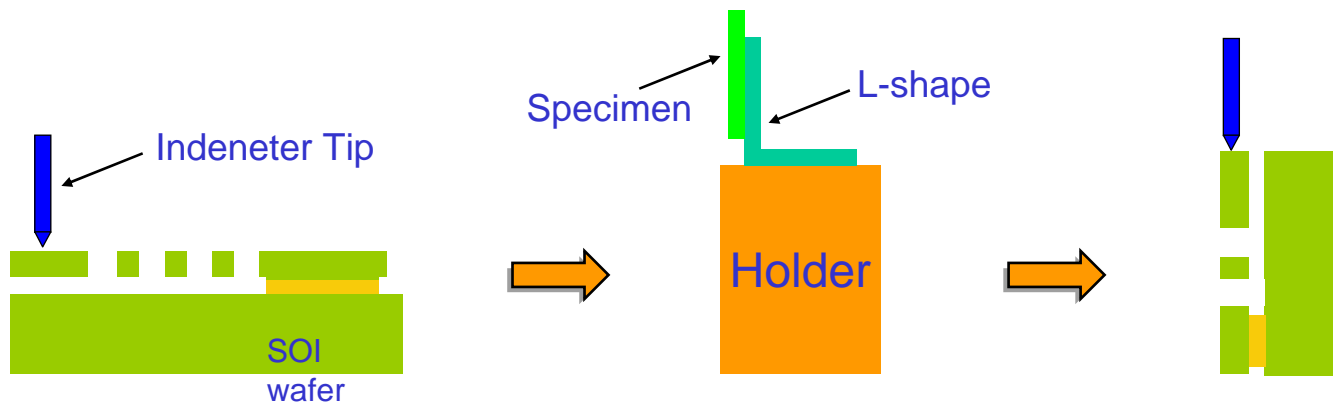
In plane motion





# Stiffness Calibration

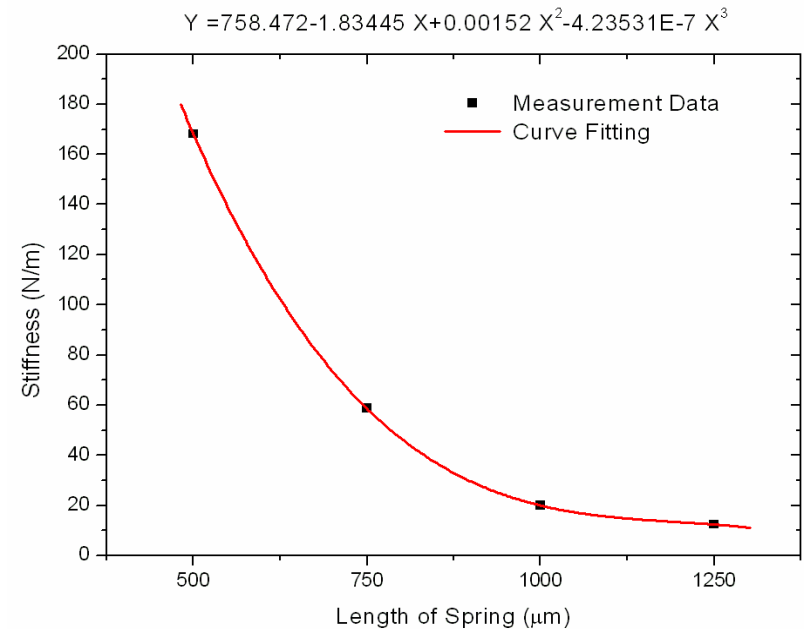
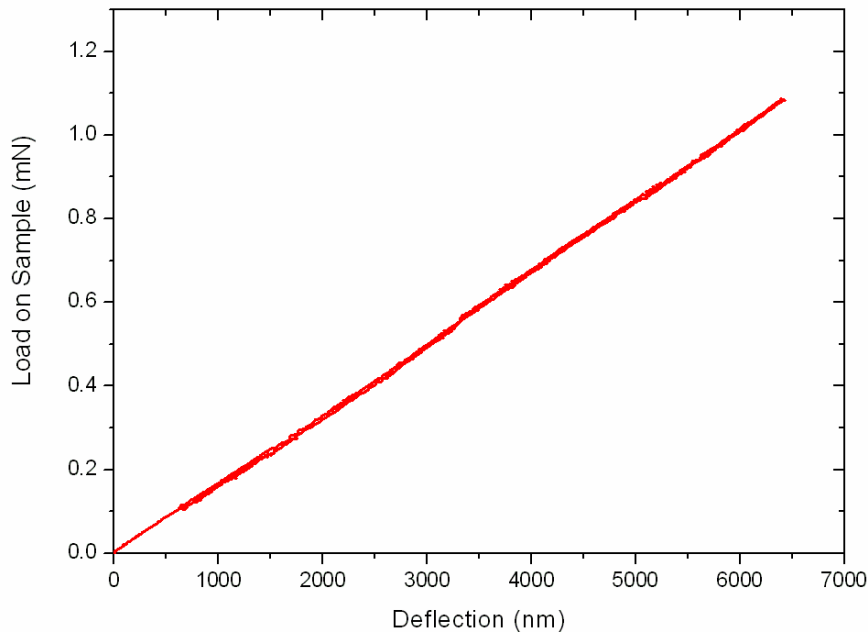
- Set-up photograph
- Transfer in-plane motion into out-of-plane motion using L-shape holder.





# Stiffness Calibration

- Typical load-deflection relationship for 500  $\mu\text{m}$  of folded beam
- Stiffness : 168 N/m

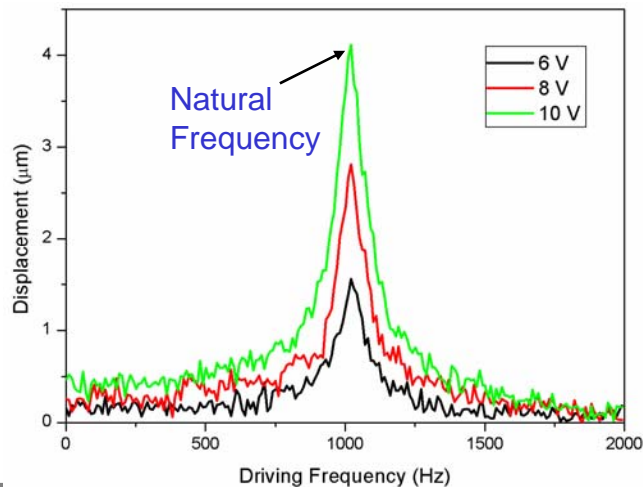
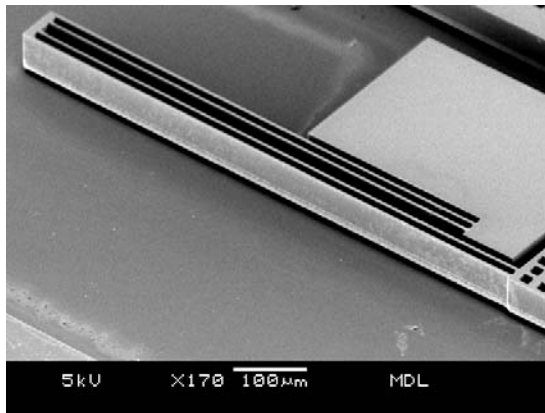




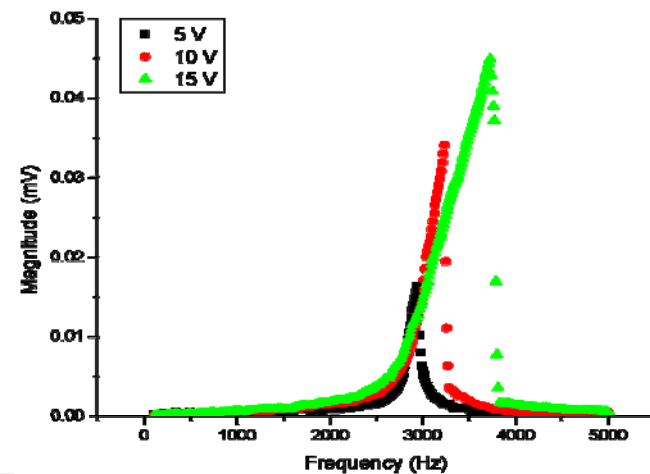
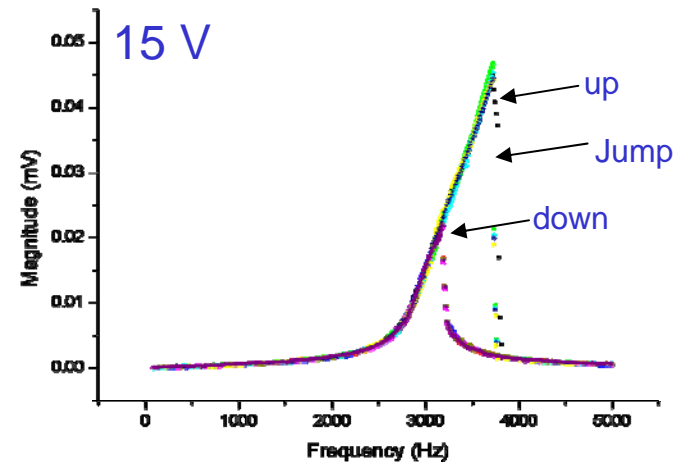
# Dynamic Response

- Dynamic Measurement - Frequency Response

- Folded beam



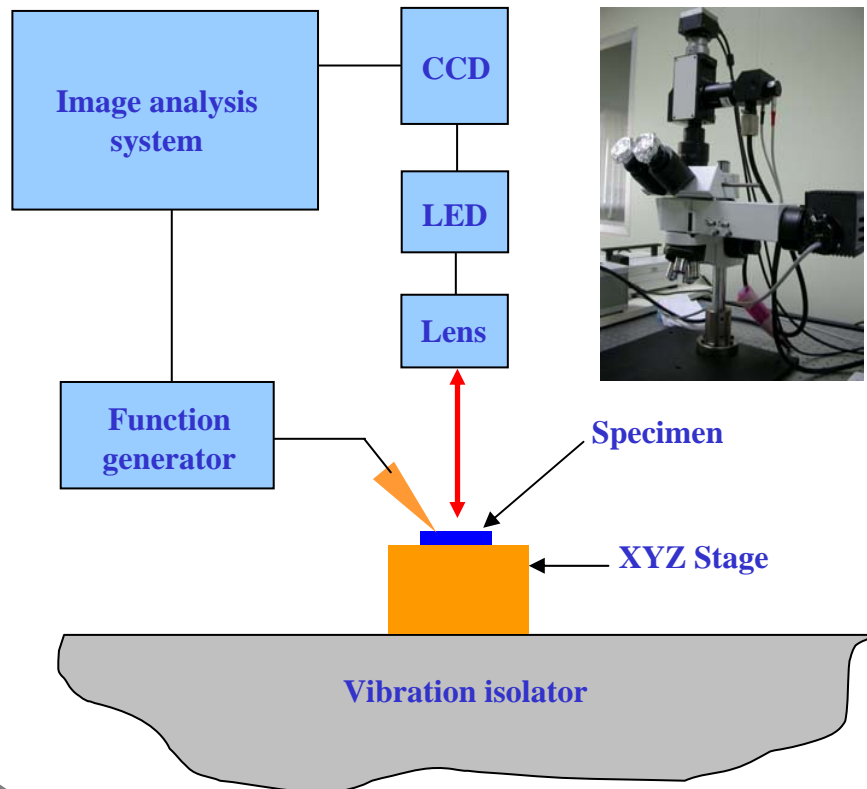
- Clamped beam - Jump phenomenon



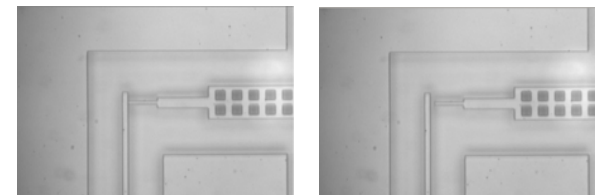
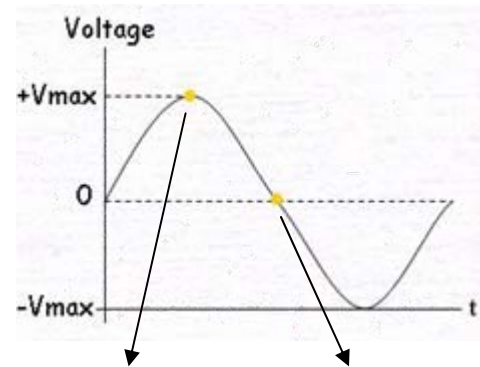


# Force Calibration

- Experimental setup by MMA(MEMS Motion Analyzer)
- In-plane motion is measured



- Specifications
  - Measured by image capture
  - Frequency range : 1 Hz ~ 10MHz
  - In-plane motion resolution : 20nm



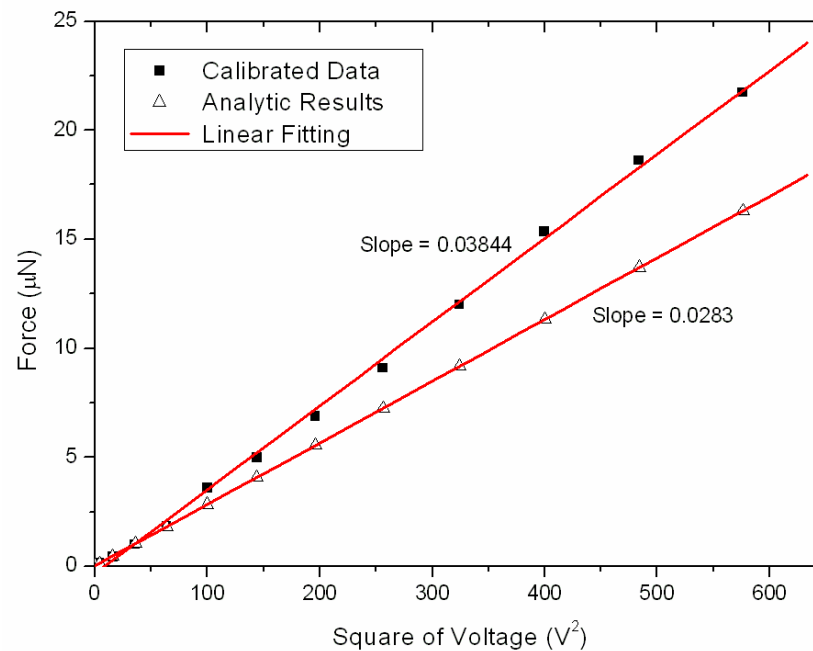
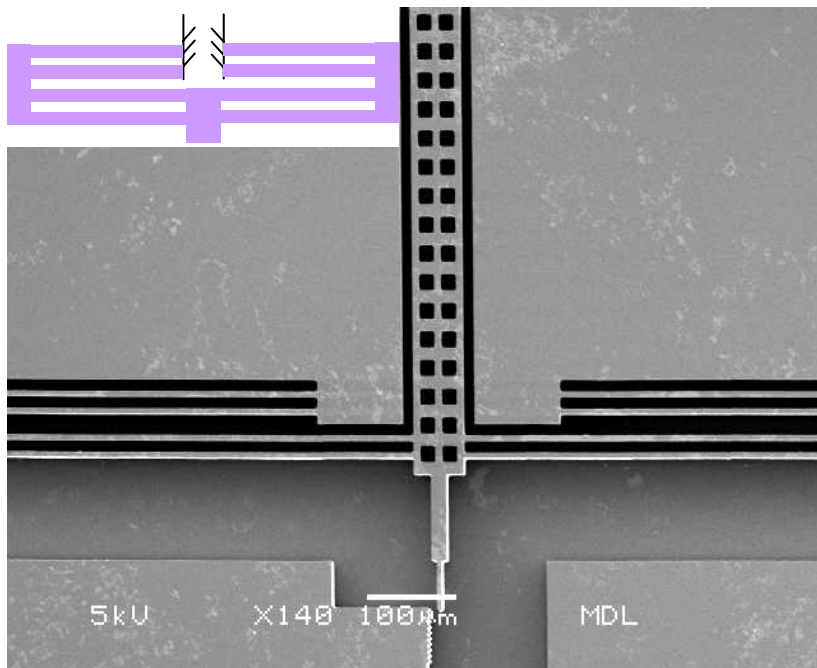


# Force Calibration

- 1 Hz frequency simulate static load-deflection relationship

- Folded beam

$$F_a = N \frac{Et}{g} V^2 = K_y \cdot y \rightarrow \text{MMA Measurement}$$

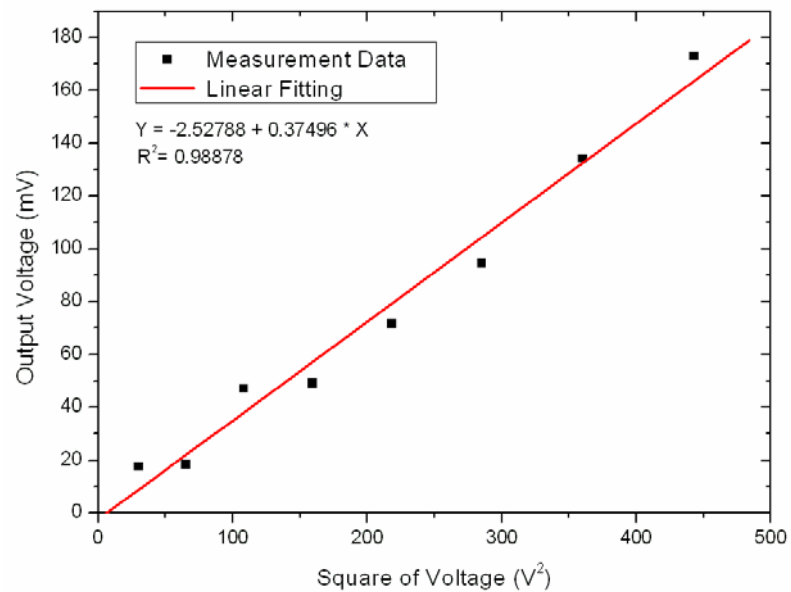
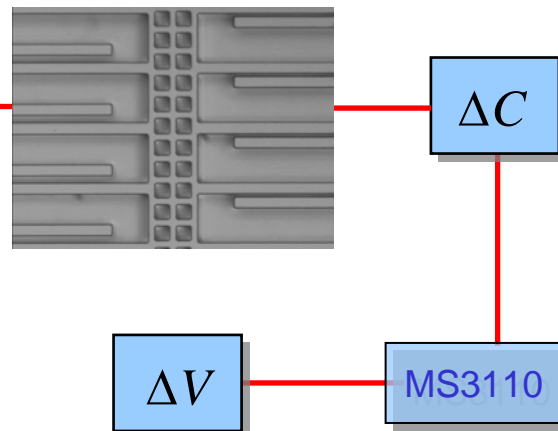
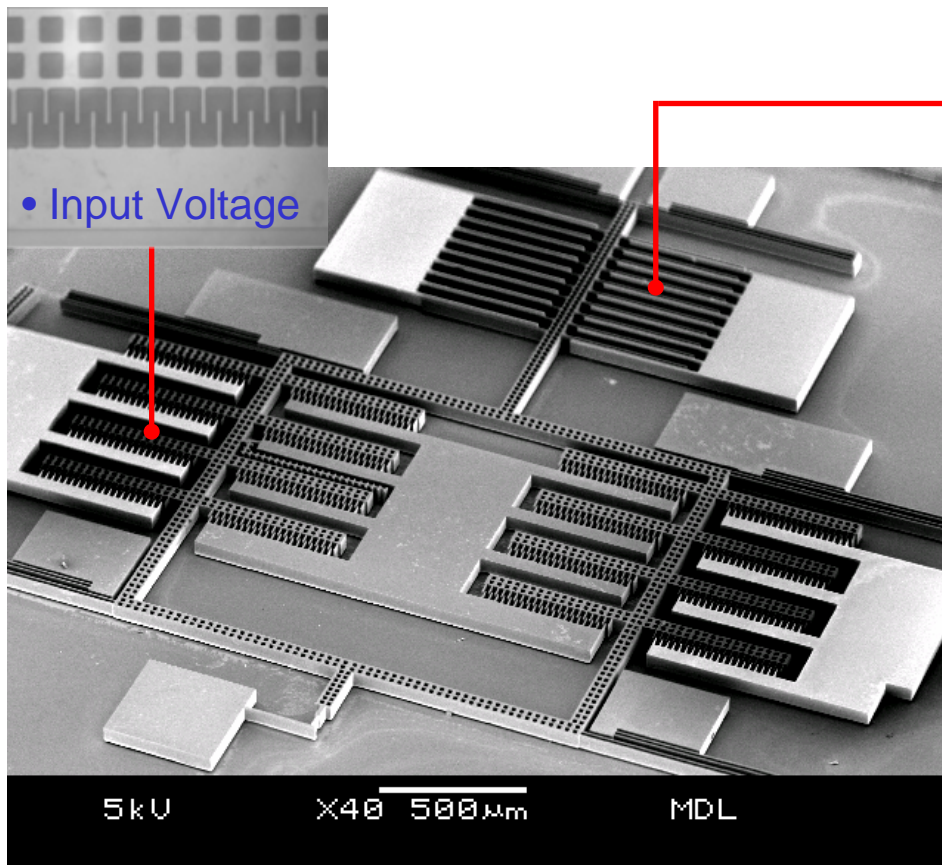








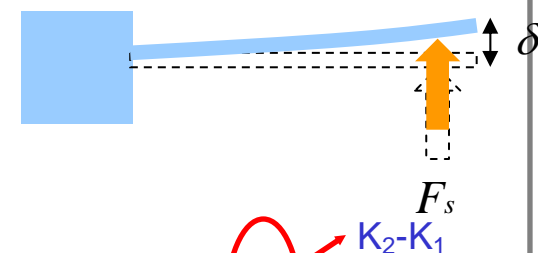
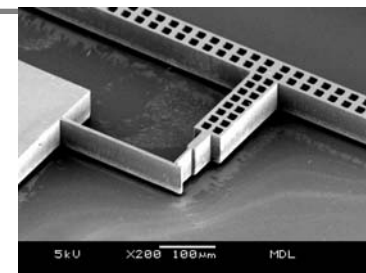
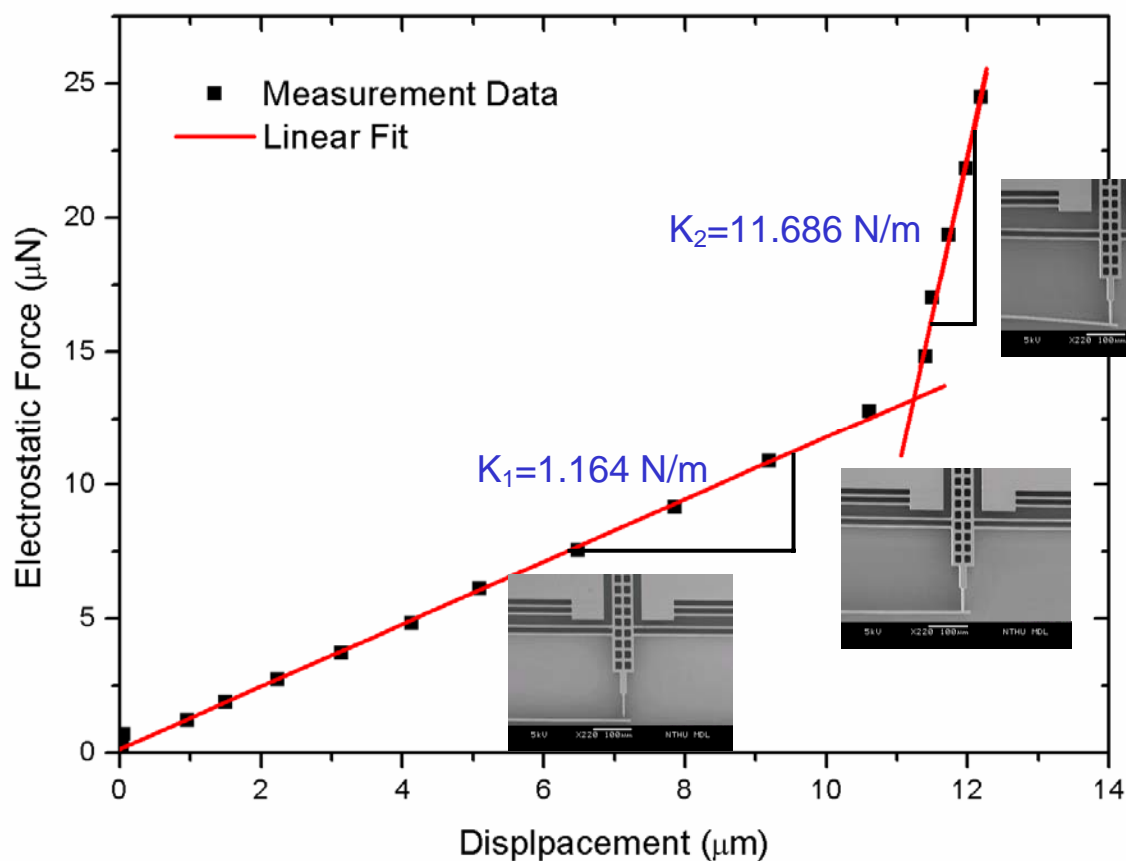
# Electrical Output





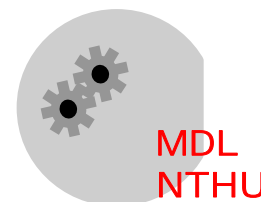
# Applications

- Extract Young's Modulus
- There exist a error deviation on bending test using the micro-instrument and textbook about 4.8 %.



$$E_s = \frac{4l^3}{hb^3} \cdot \frac{F_s}{\delta}$$

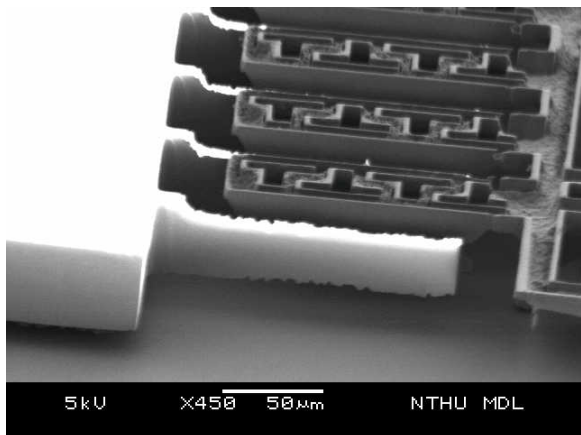
$\Rightarrow E = 173 \text{ GPa}$



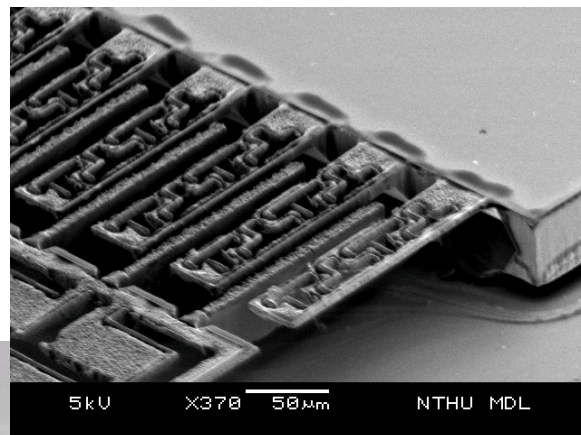




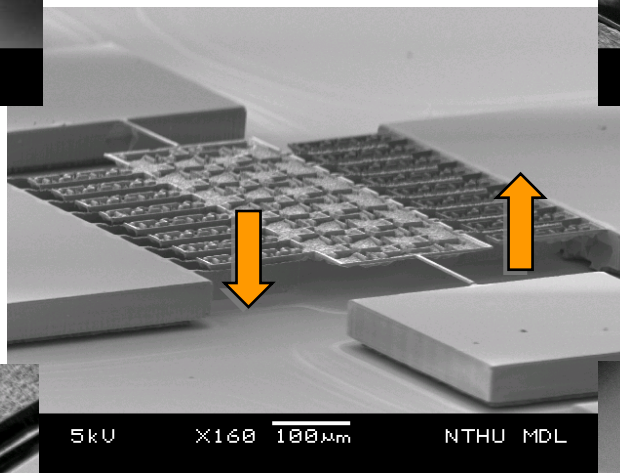
# Other Available Instrument



Vertical Comb  
(downward actuation)

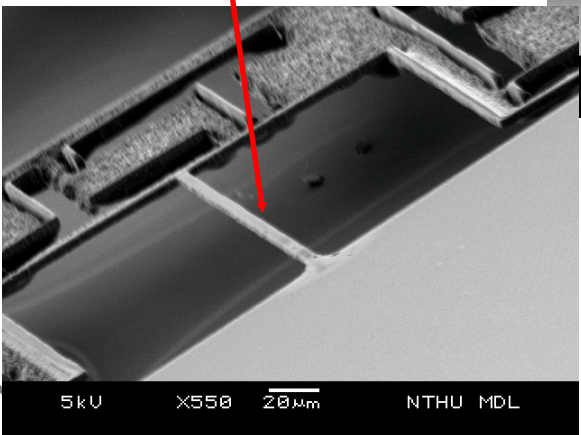


Vertical Comb  
(upward actuation)

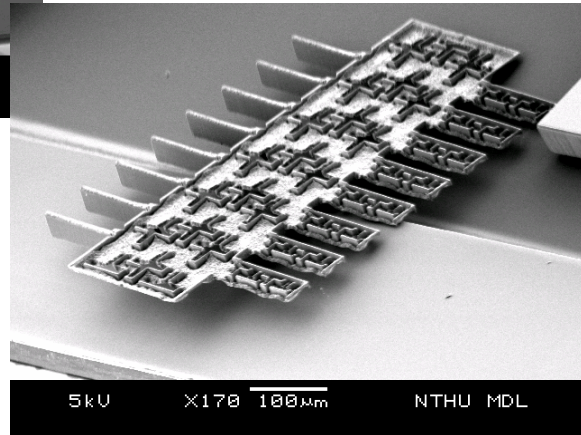


Torsion Specimen

Rein-force Structure

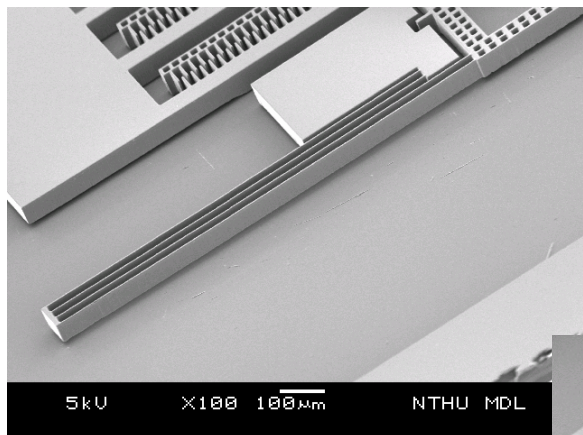


Pure Torsion Testing

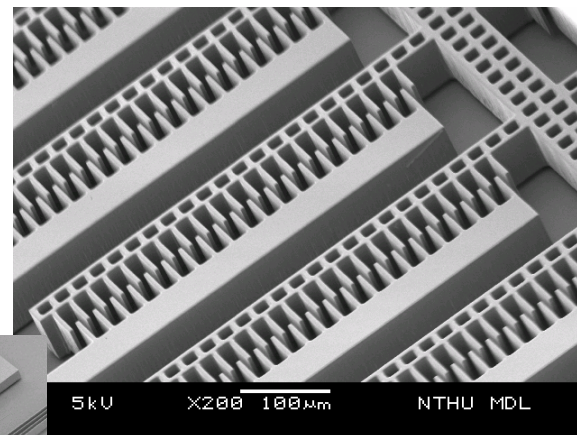




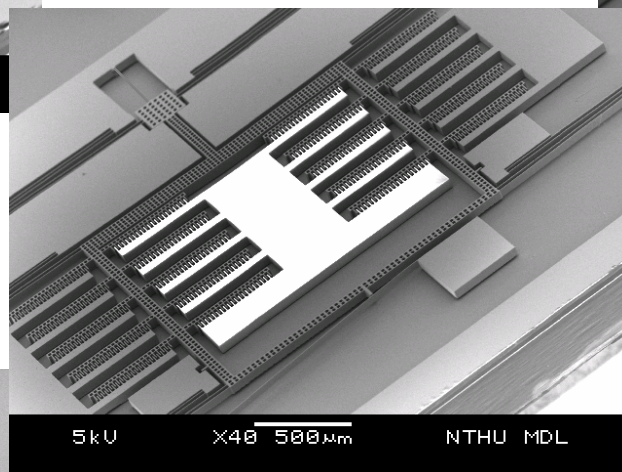
# Other Available Instrument



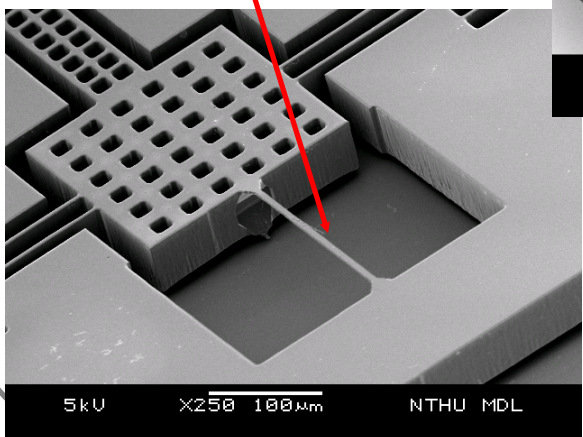
Support Spring



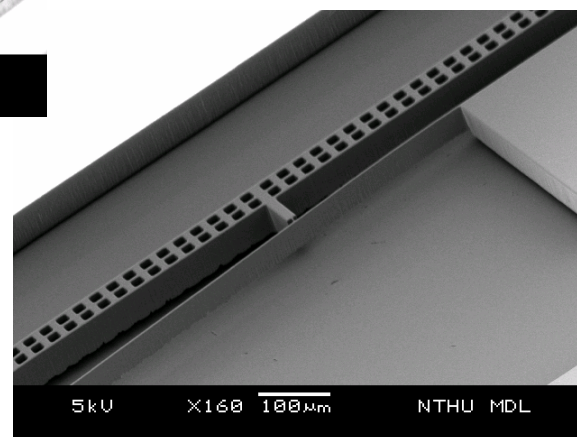
Comb Actuator



Tensile Testing



Tensile Specimen



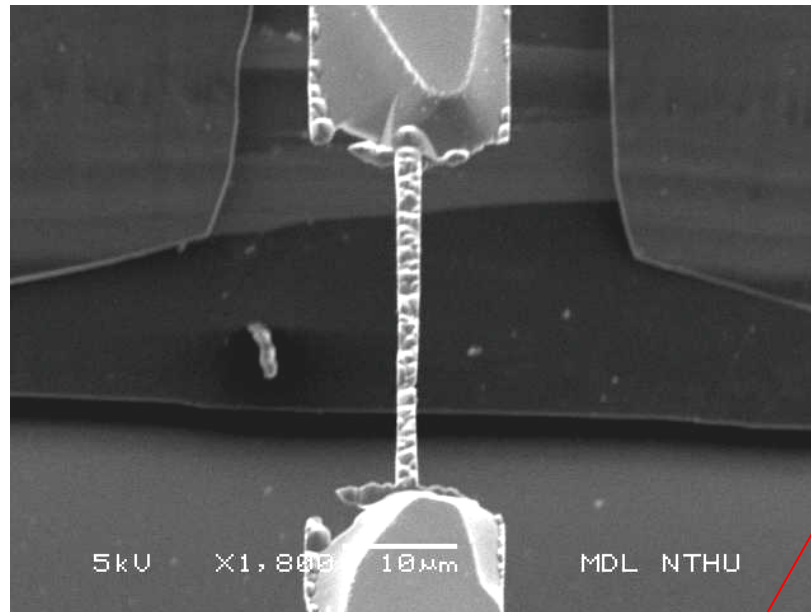
Motion Amplification



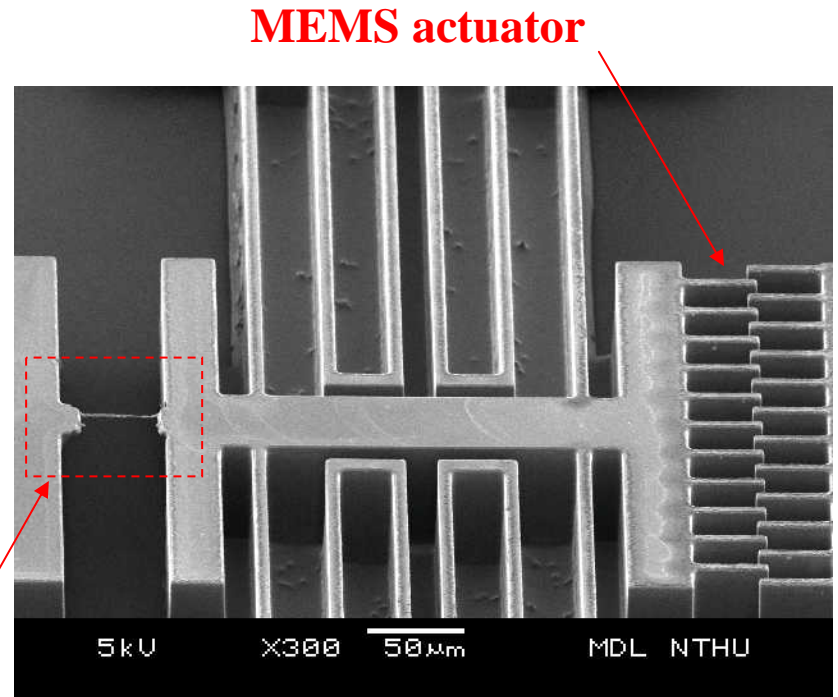


# Integration of N/MEMS

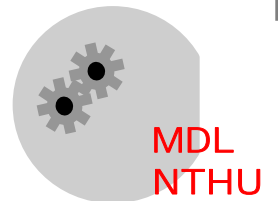
- Nano structure testing



**Nano structure/sample holder**



H.-Y. Chu, and W. Fang, *IEEE MEMS'04*, the Netherlands, 2004

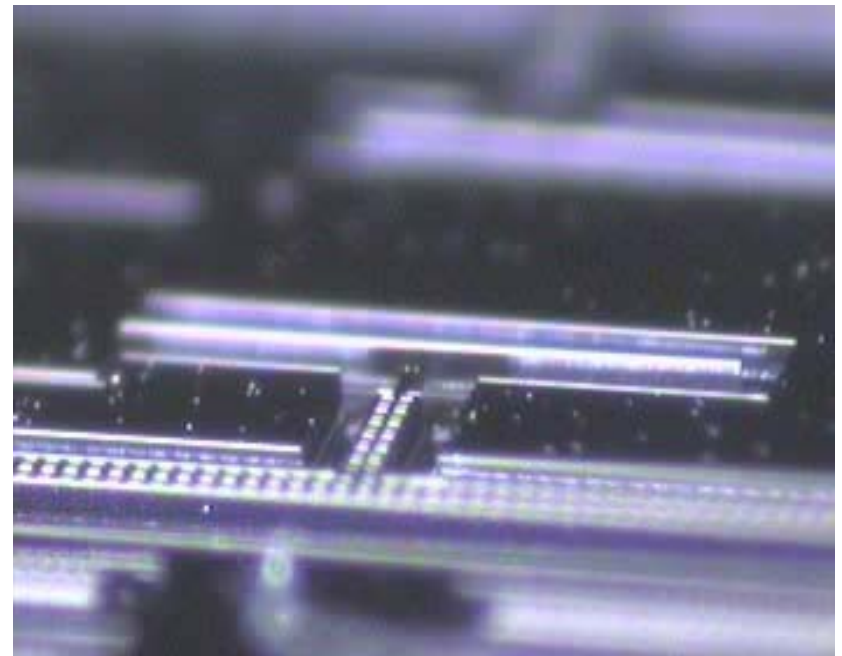
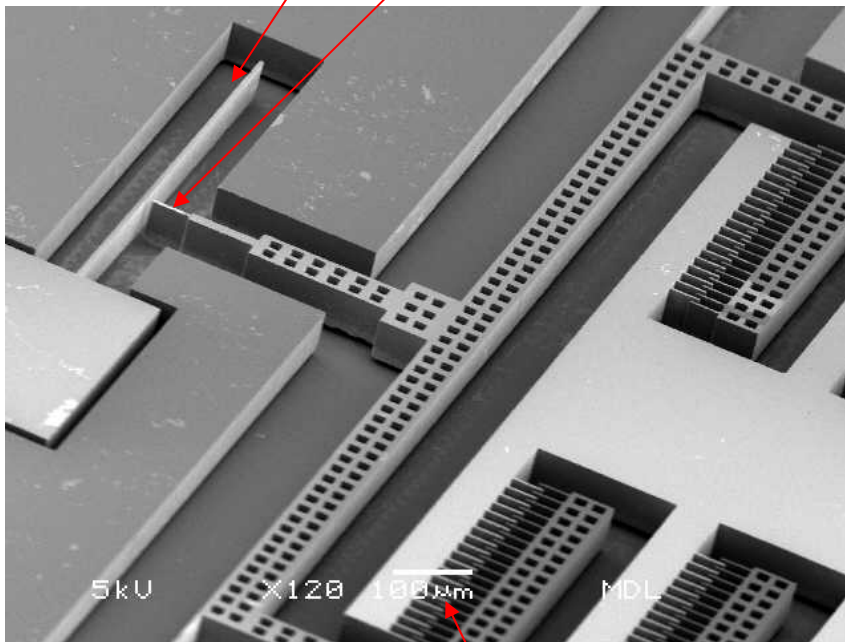




# Integration of N/MEMS

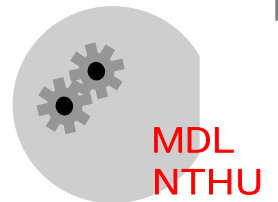
- Nano structure testing

**Nano/micro test specimen**  
**Micro probe**



**MEMS linear actuator**

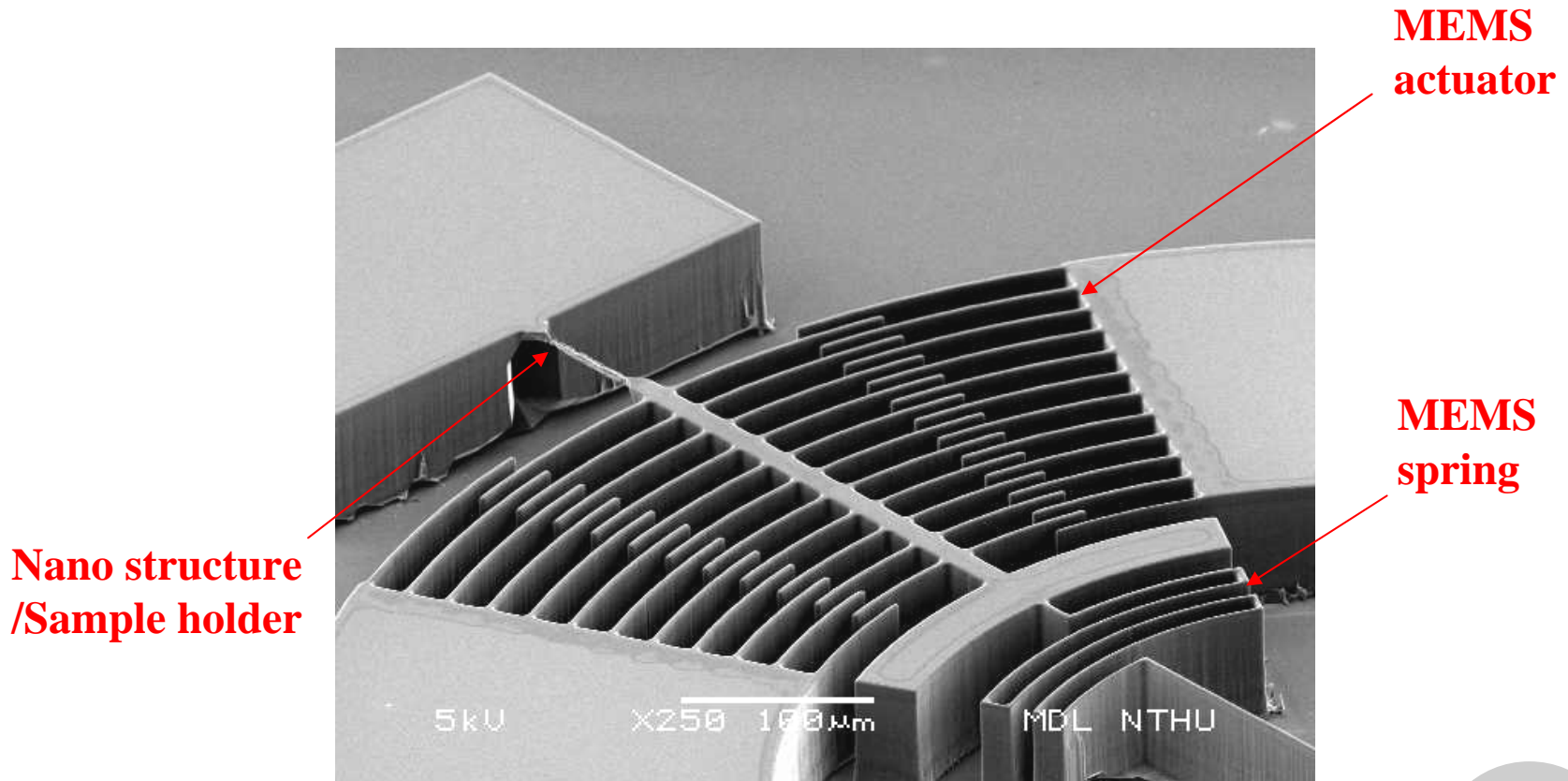
C. Chang, H.-Y. Chu, and W. Fang, 2004



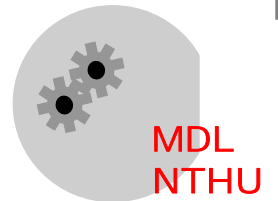


# Integration of N/MEMS

- Nano structure testing



H.-Y. Chu, and W. Fang, *IEEE MEMS'04*, the Netherlands, 2004

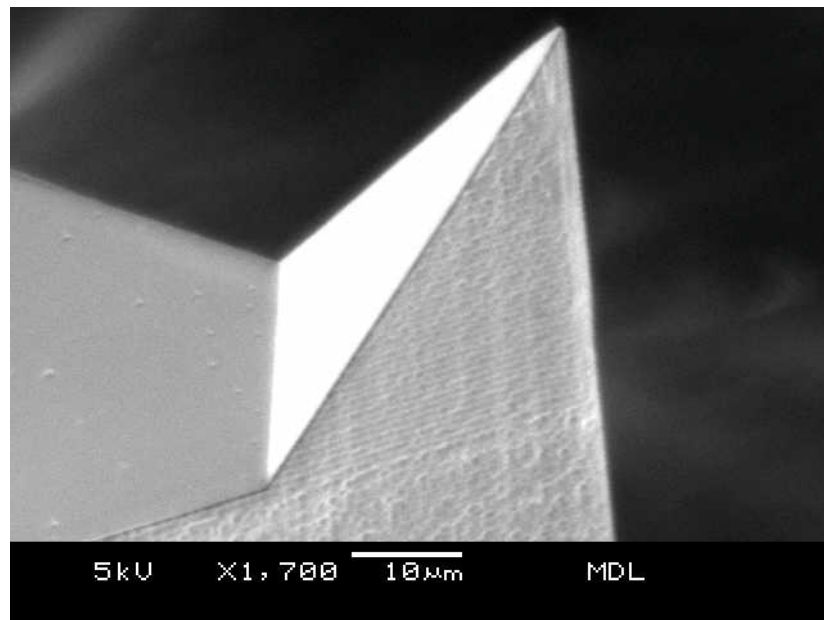
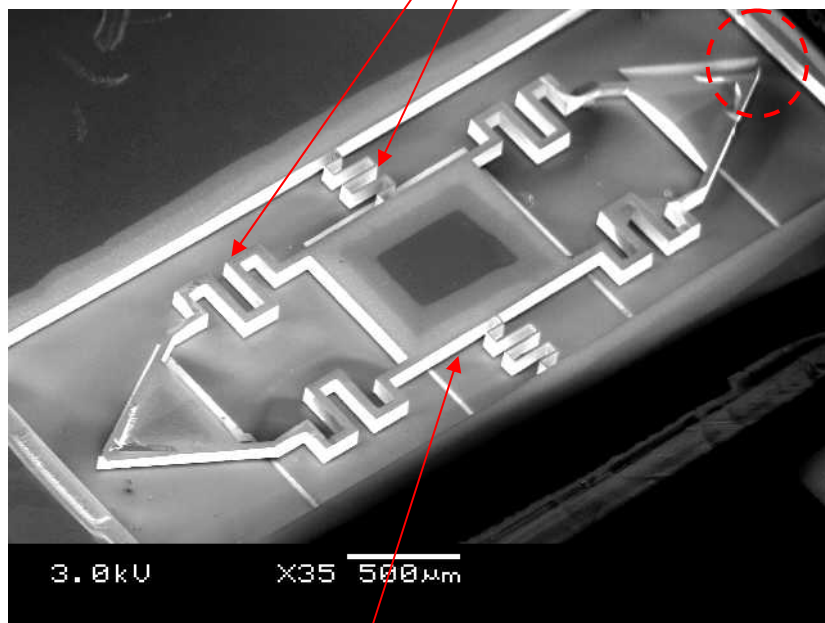




# Integration of N/MEMS

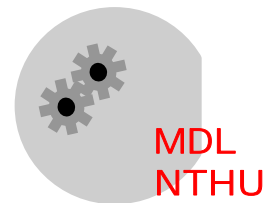
- Nano structure testing

**Spring**



**Electrostatic actuator**

B. Chang, H.-Y. Chu, and W. Fang, 2004





# Conclusions

- On-chip micro-instrument for thin film and micro-structures testing.
- Standard testing platform for micro/nano structures

